

Electronic Structure of Rocksalt Copper Monoxide: A Proxy for High Temperature Superconductivity

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Matteo Cococcioni, U Minn
Nicola Marzari, MIT
Axel Kohlmeyer, U Penn
Evyaz Isaev, MISA
Tone Kokalj, Ljubljana
...e tutto di consorzio
“Quantum Espresso,” ICTP

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22 Years Ago...

Possible High T_c Superconductivity in the Ba – La – Cu – O System

J.G. Bednorz and K.A. Müller

IBM Zürich Research Laboratory, Rüschlikon, Switzerland

Received April 17, 1986

...Still No Theory!

Agenda

- ...Still No Theory
- Structural Issues
- “Experimental Apparatus”
- Band Structure, DOS and Fermiology
- Superconductivity
- The da Vinci Code
- Conclusions/Homework

Theory of Everything

Bob Laughlin's "Theory of Everything" (that matters)

$$\mathcal{H} = - \sum_j \frac{\hbar^2}{2m} \nabla_j^2 - \sum_\alpha \frac{\hbar^2}{2M_\alpha} \nabla_\alpha^2 - \sum_{j,\alpha} \frac{Z_\alpha e^2}{|r_j - R_\alpha|} + \sum_{j,k} \frac{e^2}{|r_j - r_k|} + \sum_{\alpha,\beta} \frac{Z_\alpha Z_\beta e^2}{|R_\alpha - R_\beta|}$$

- | | | |
|--------------------|-----------------|-----------------|
| • Hydrogen atom | • Proteins | • Flowers |
| • Methane molecule | • DNA | • Trees |
| • Water | • Viruses | • Cows |
| • Air | • Bacteria | • Cheese |
| • Rocks | • Yeast | • Sauce Bernais |
| • Concrete | • Slime mold | • Computers |
| • Steel | • Butterflies | • Television |
| • Glass | • Sharks | • Cars |
| • Plastic | • Rats | • Jots |
| • Buildings | • Lawyers | • Lawnmowers |
| • Cities | • Ebola virus | • Sewage |
| • Continents | • Legislatures | • Spotted Oats |
| | • Civilizations | ... |

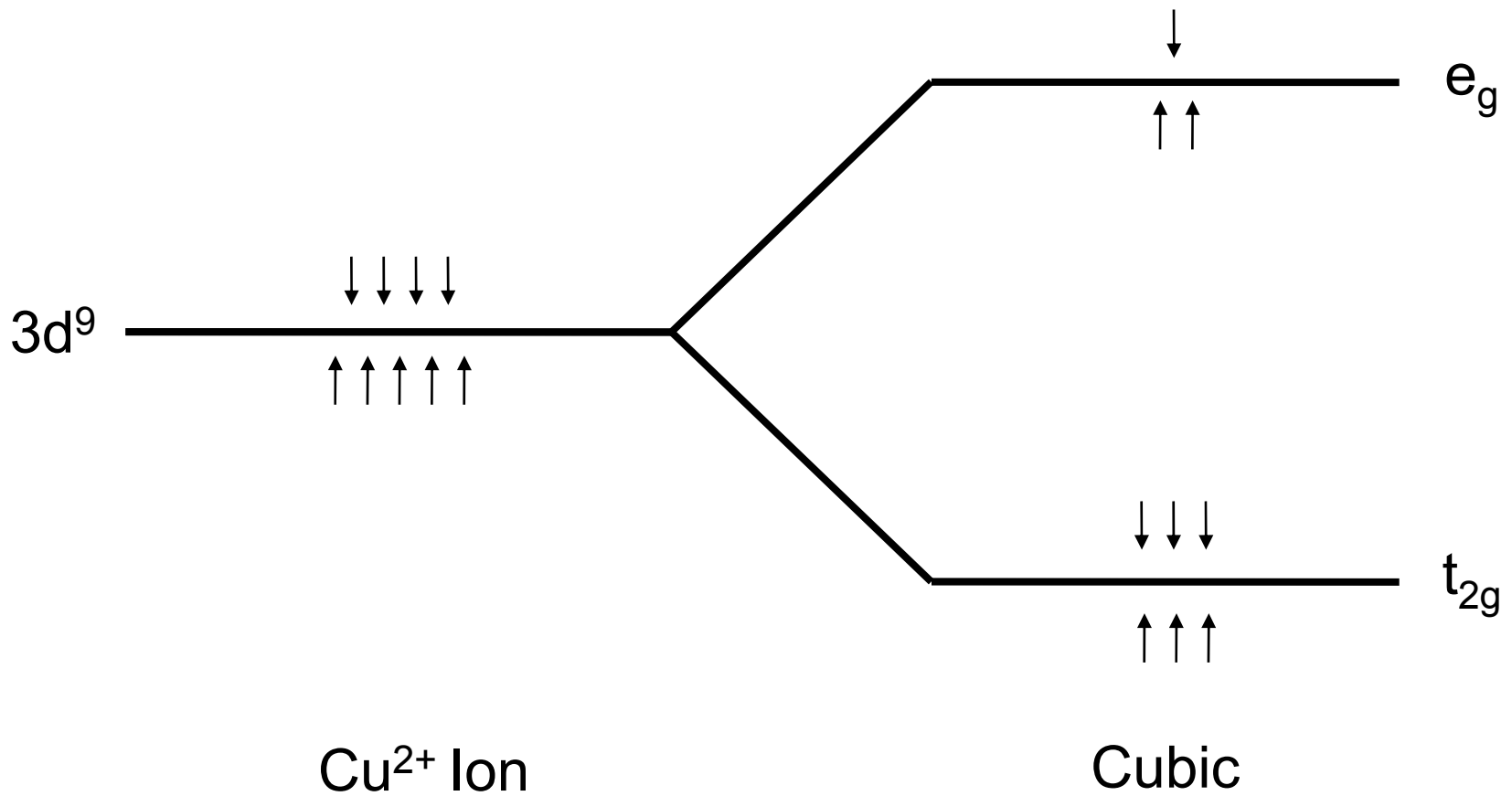
Should use the many body Dirac equation!

And Add Maxwell, Boltzman and Gibbs, and Newton

The crunch comes when \sum_i with $i \geq 3 \rightarrow$ "thermodynamic limit."

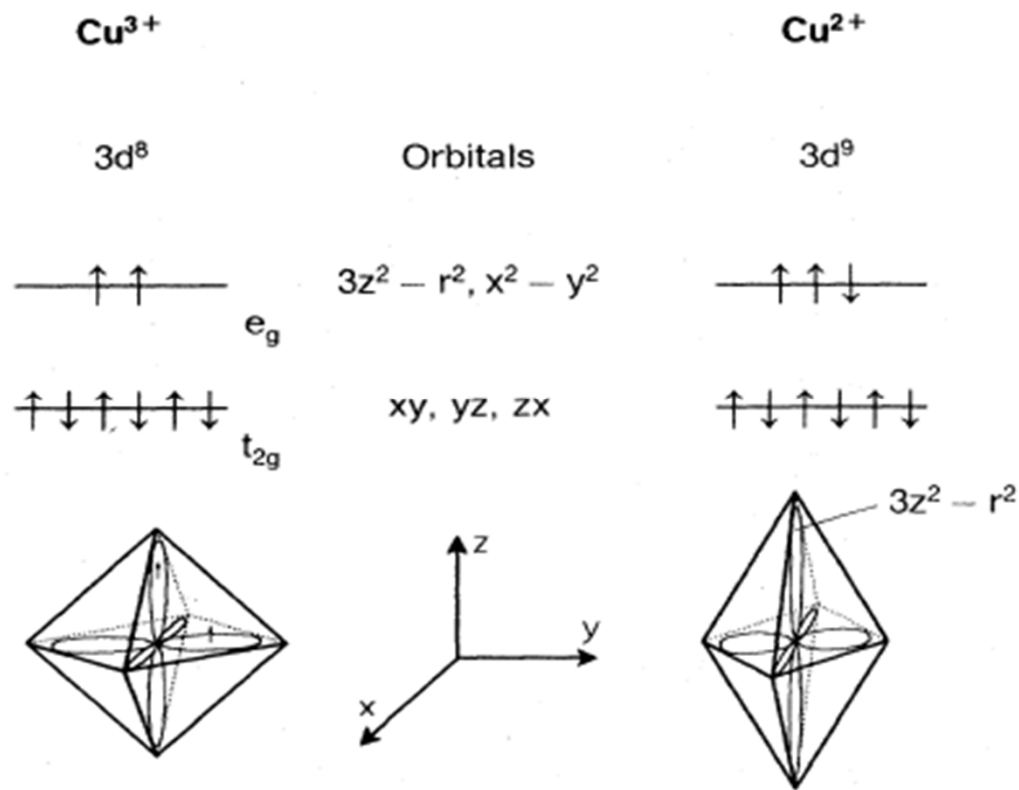
"Size Matters !"

Cu²⁺ 3d Multiplet Splitting (Cubic)

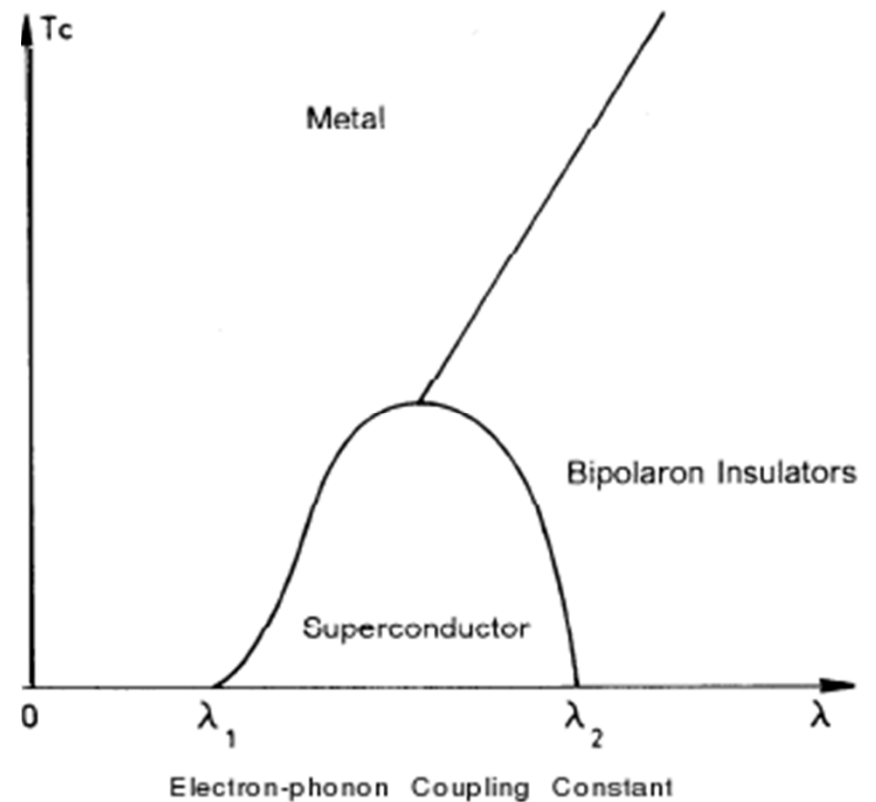


Bednorz-Mueller Nobel Lecture

Copper Ions in the Oxide Octahedron



*Jahn-Teller Effect:
Elongation of
the Octahedron*



After Chakravarty, (1979)

Hubbard Theory

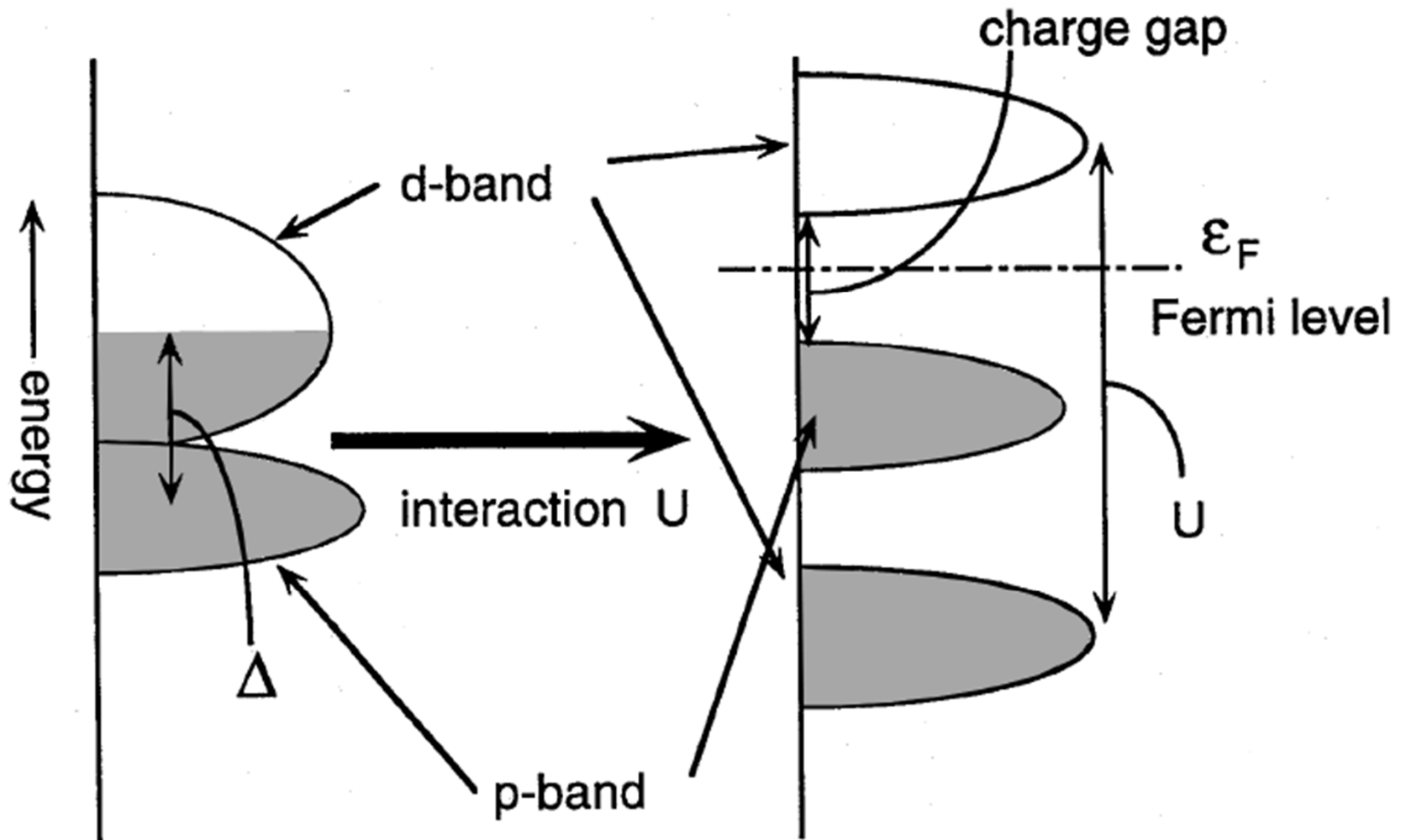
$$H = \sum_{\langle ij \rangle, \sigma} t_{ij} c_{i\sigma}^\dagger c_{j\sigma} + U \sum_i n_{i\downarrow} n_{i\uparrow} + \frac{V}{2} \sum_{\langle ij \rangle, \sigma, s} n_{i\sigma} n_{js}$$

One-electron
"band" term

On-site "Hubbard"
double occupation
coulomb repulsion

Off-site
repulsion

Charge Transfer Insulator



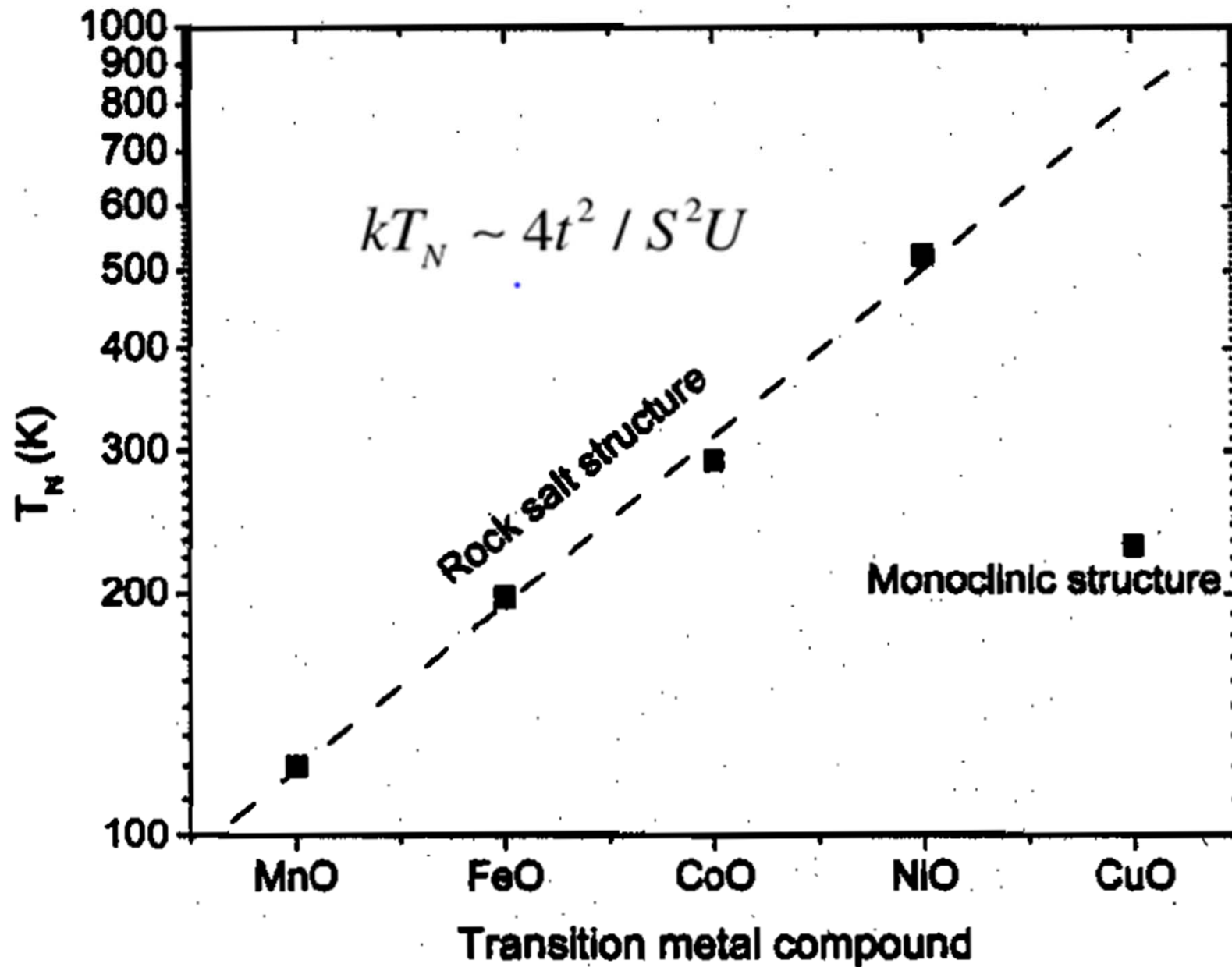
After Imada, et al, RMP 70, 1039 (1998)

Cubic Rocksalt Divalent TMOs

<u>TMO</u>	<u>3d Config</u>	<u>Properties</u>
MnO	5	MH-CTI (5.6)
FeO	6	MH-CTI (5.9)
CoO	7	MH-CTI (6.3)
NiO	8	MH-CTI (6.5)
CuO	9	<i>XX Doesn't Exist!</i>

See Imada, Fujimore,
Tokura, RPM 70 (1988)

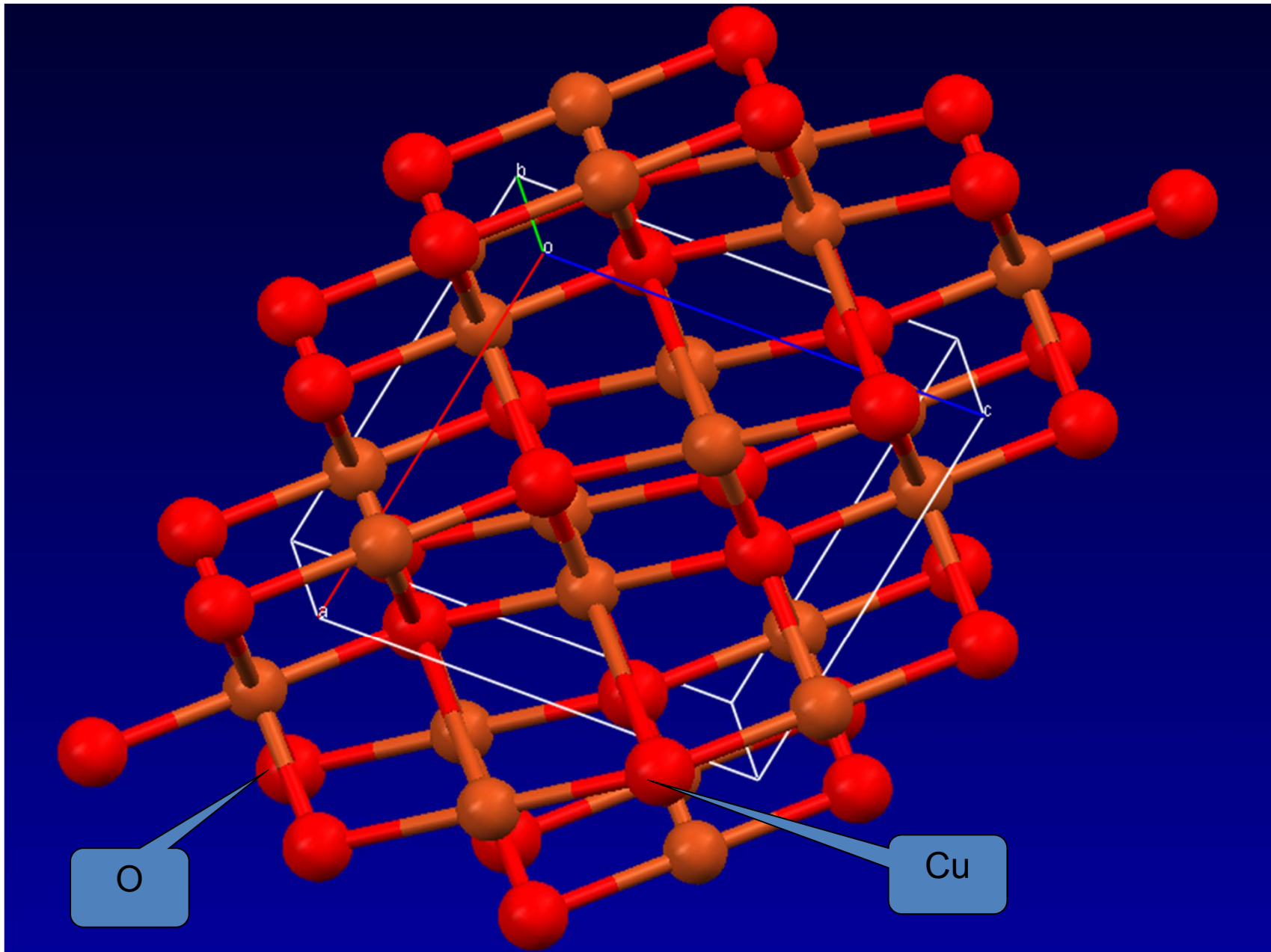
Néel Temperature vs. TMO Atomic Number



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Tenorite (Monoclinic CuO)



DFT & (LDA + U)

$$E_{\text{LDA+U}}[n(\mathbf{r})] = E_{\text{LDA}}[n(\mathbf{r})] + E_{\text{HUB}}\left[\left\{n_m^{l\sigma}\right\}\right] - E_{\text{DC}}\left[\left\{n^{l\sigma}\right\}\right]$$

- Implemented in LMTO by Anisimov, et al, JPCM 2, 3973 (1990)
 - Applied to NiO, MnO, FeO, CoO and La₂CuO₄
- Plane-Wave Pseudopotential Implementation by Cococcioni and de Gironcoli, PRB 71, 035105 (2005)
 - Applied to FeO and NiO
 - Download open-source package from <http://www.pwscf.org>

Experimental Equipment (Software)

- QUANTUM-ESPRESSO Suit of Codes
 - DFT (LDA+U) plus electron-phonon
 - Graphics by Tone Kolalij (XCrysDen)
 - www.quantum-espresso.org
- “Dial-in” Parameters
 - $G^2 = 40 \text{ Ry}$ $\rho = 320 \text{ Ry}$
 - Convergence $\leq 10^{-6} \text{ Ry}$
 - “Smearing” = Methfessel-Paxton
 - Pseudopotentials: Ultrasoft, XC = Perdew-Zunger
Cu: $3d^9 4s^2$ O: $2s^2 2p^4$

Experimental Equipment (Hardware)

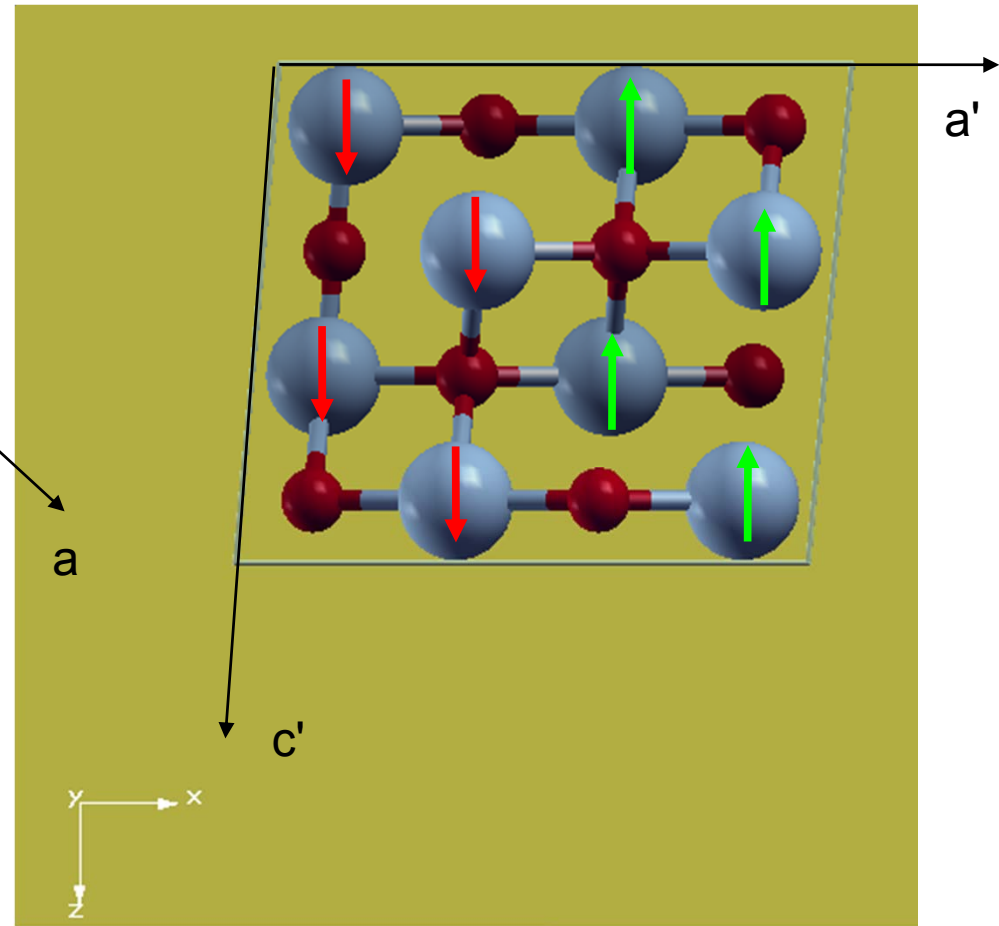
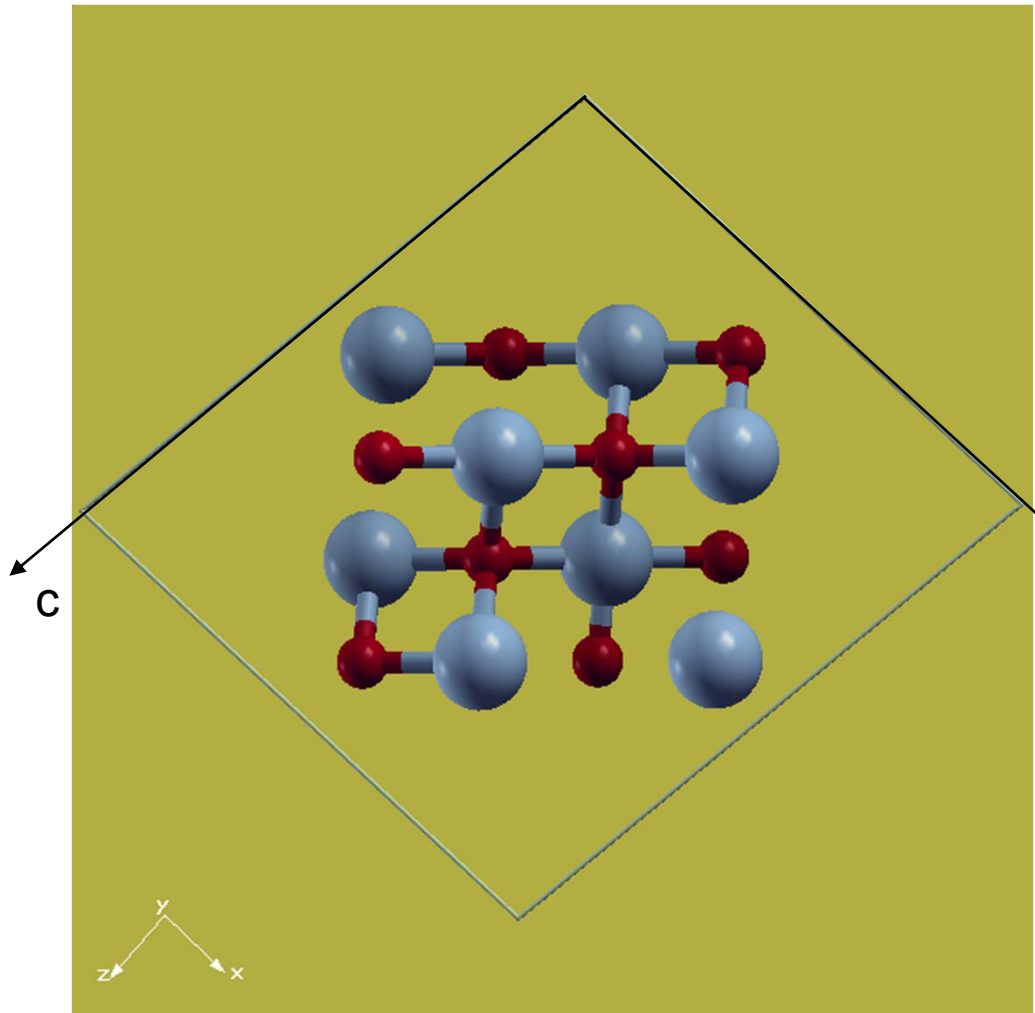
3-Cluster Home Network: AMD64 dual 3.5 GHz, 12 GB +
IBM-X41 +...



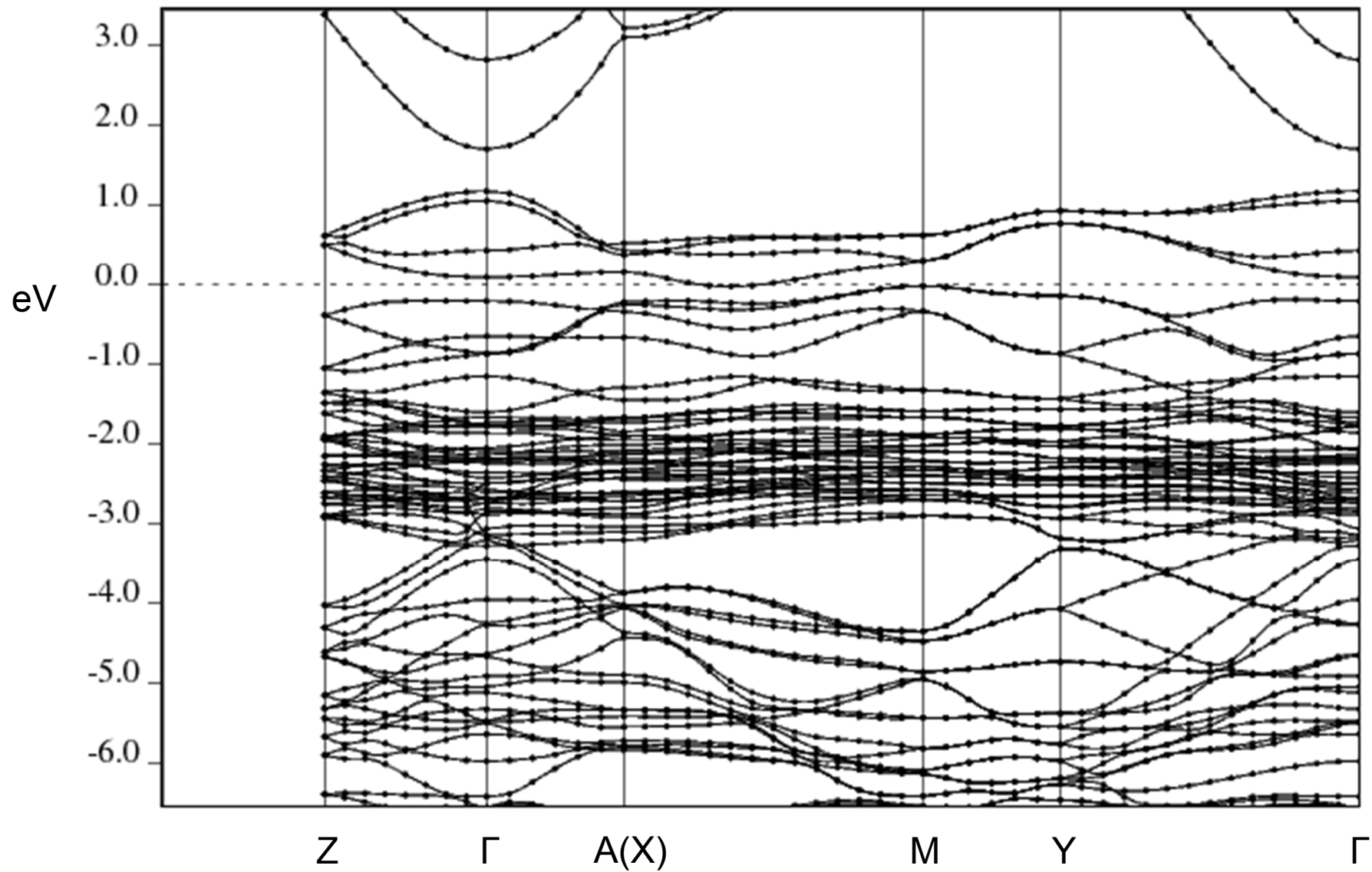
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nm & af Unit Cells

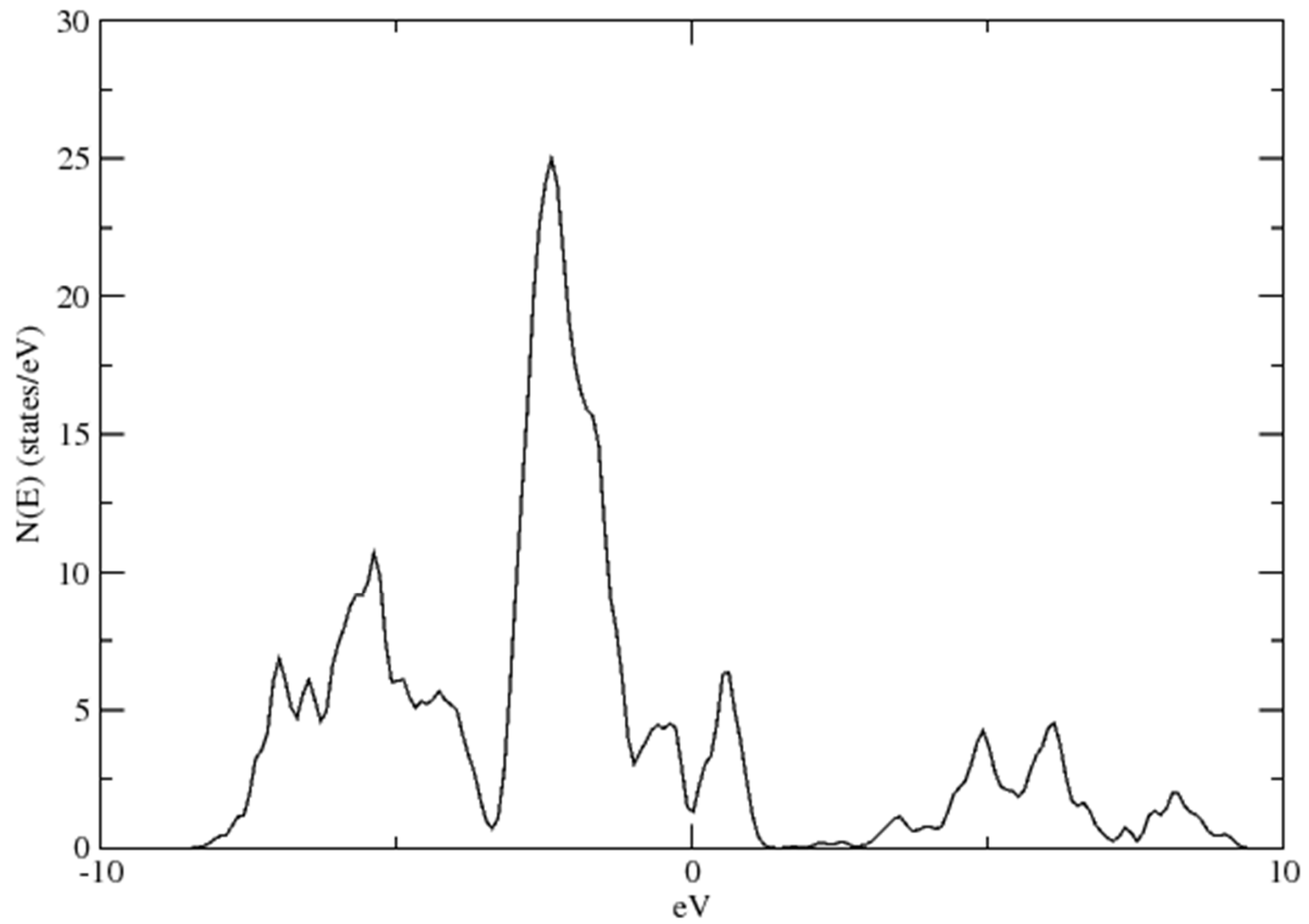


Tenorite ($U = 0$)

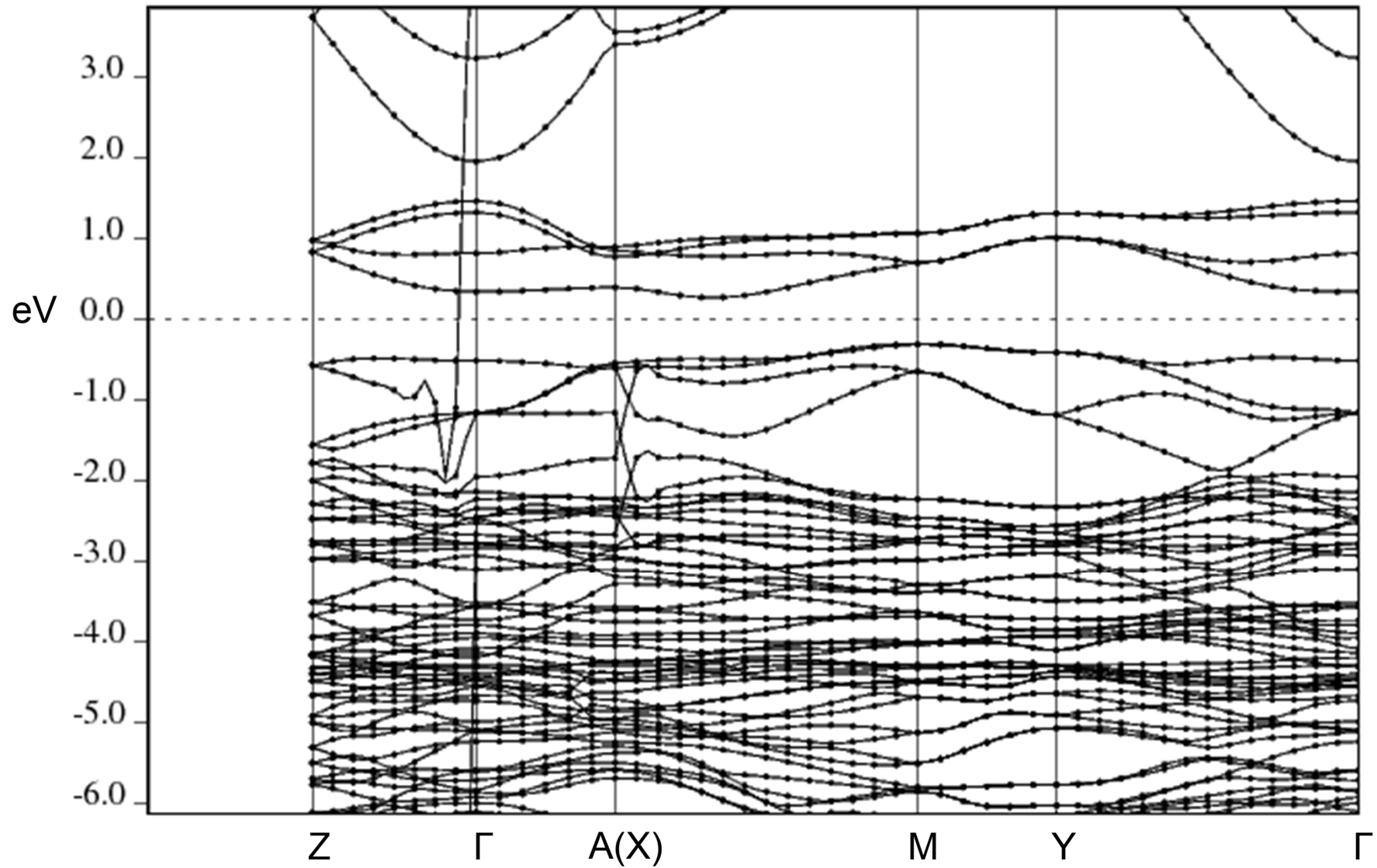


af-Tenorite DOS Plot

$U = 1.d-7$ $E_f = 10.5211$

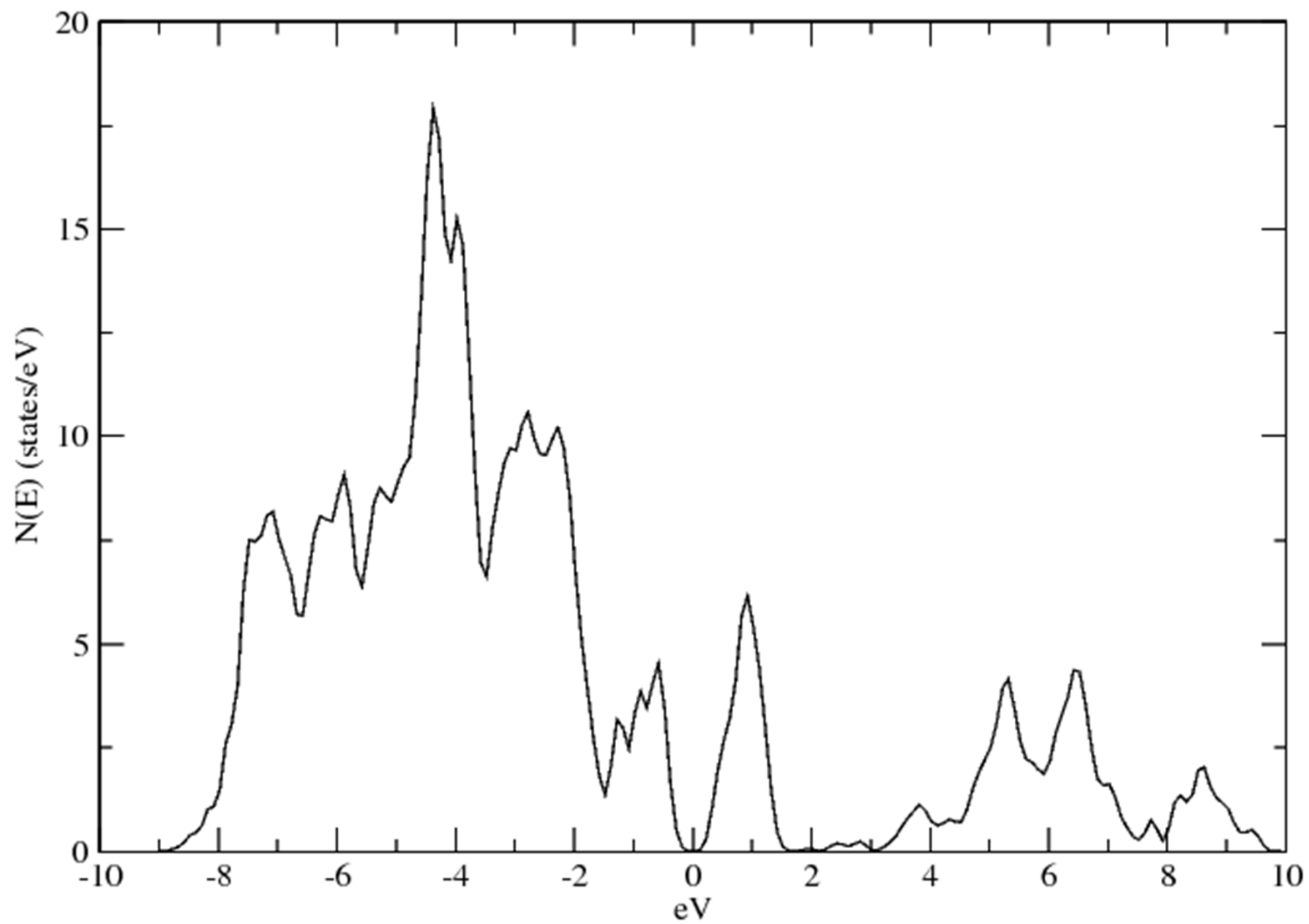


Tenorite ($U = 5$)



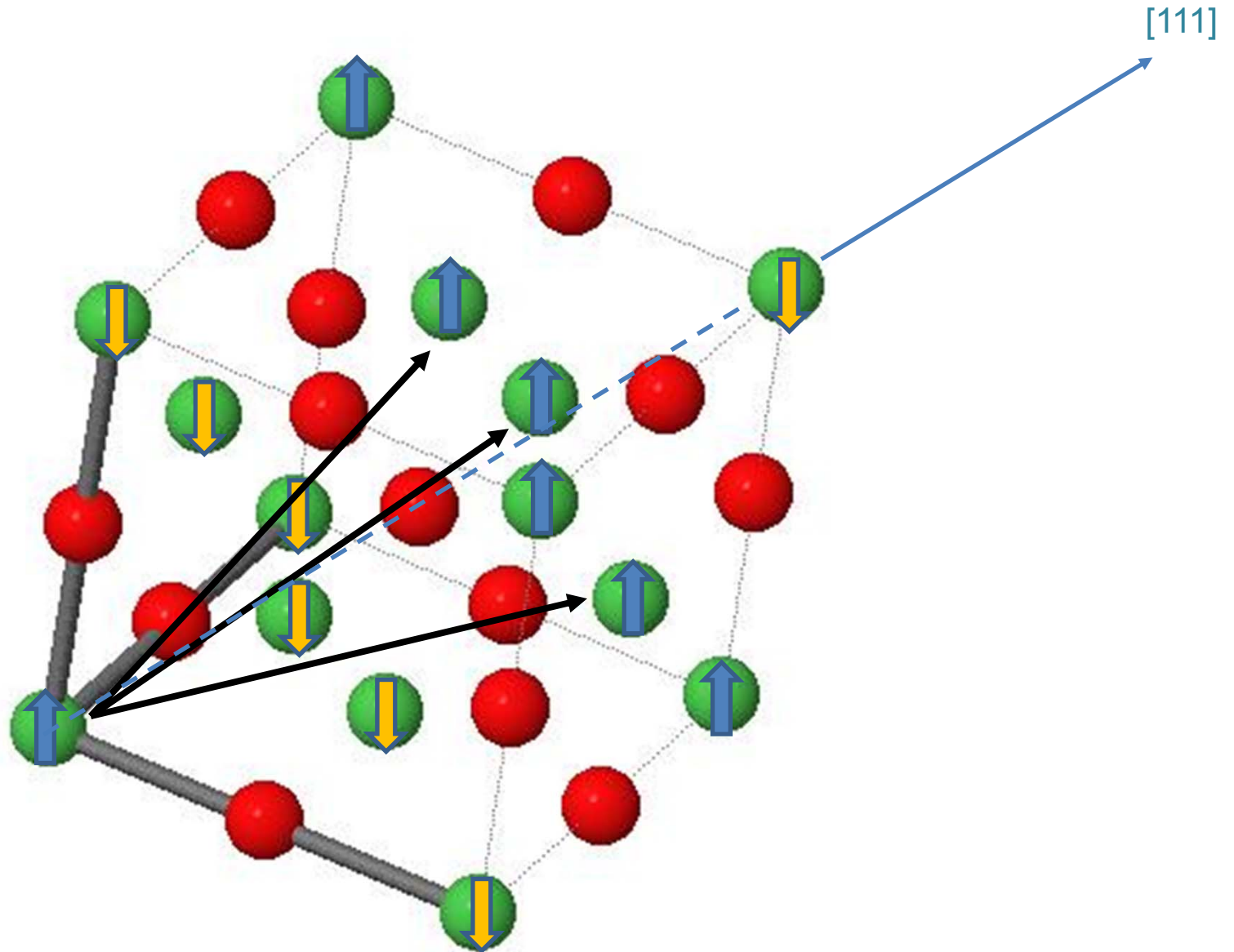
af-Tenorite DOS Plot

$U = 5$ $E_f = 10.1435$



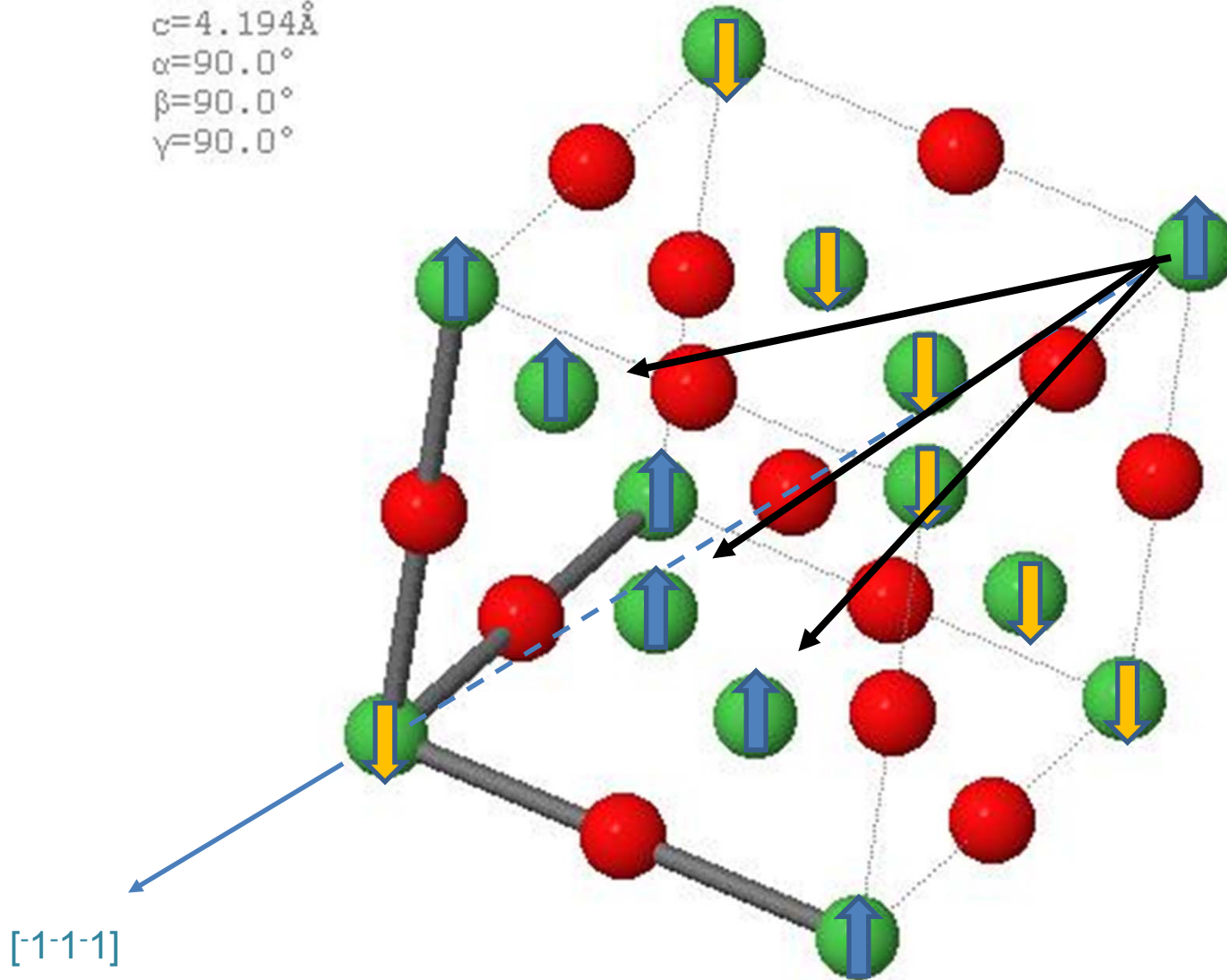
Proto-TMO AF Rock Salt

Fm-3m
a=4.194Å
b=4.194Å
c=4.194Å
α=90.0°
β=90.0°
γ=90.0°

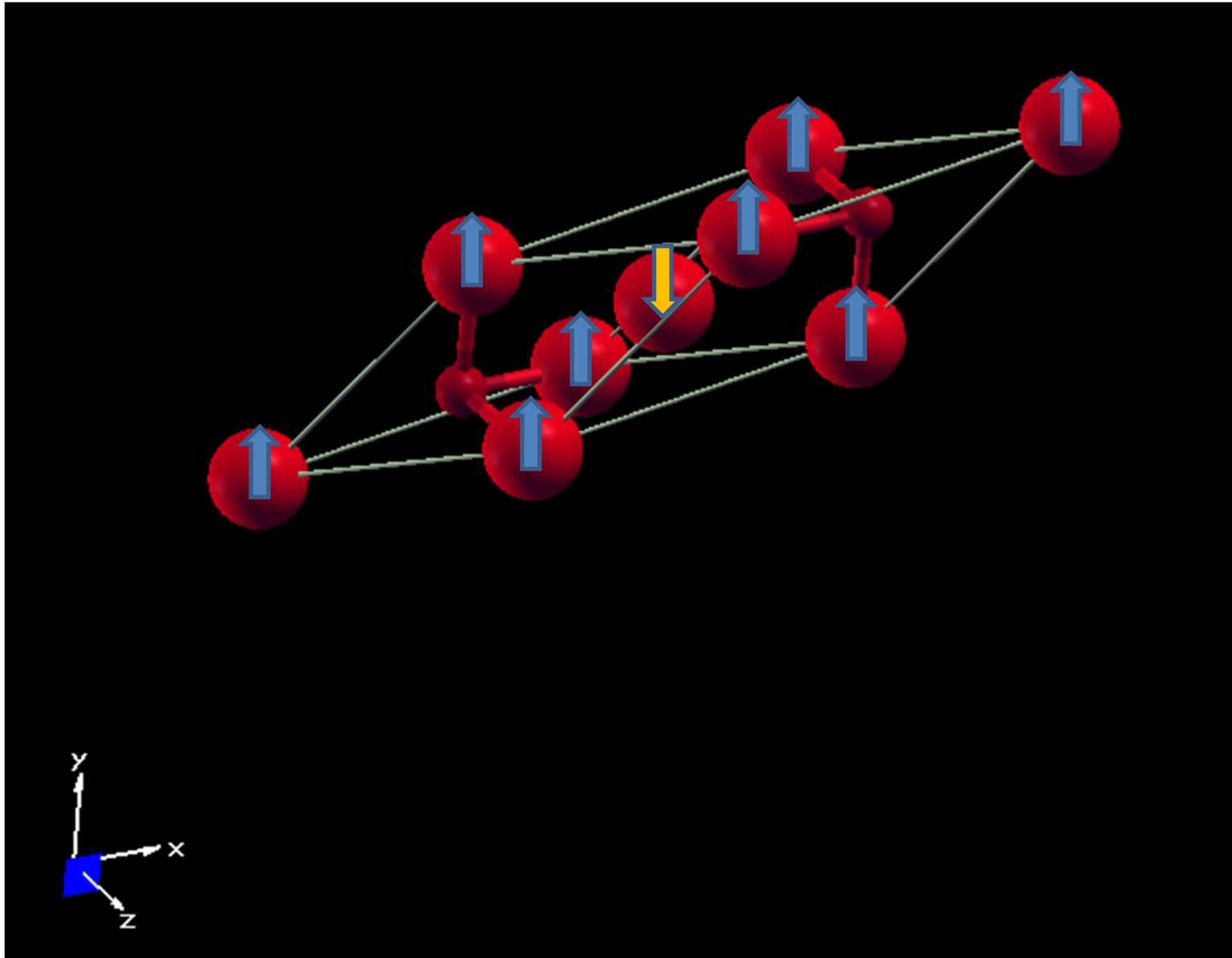


Proto-TMO AF Rock Salt

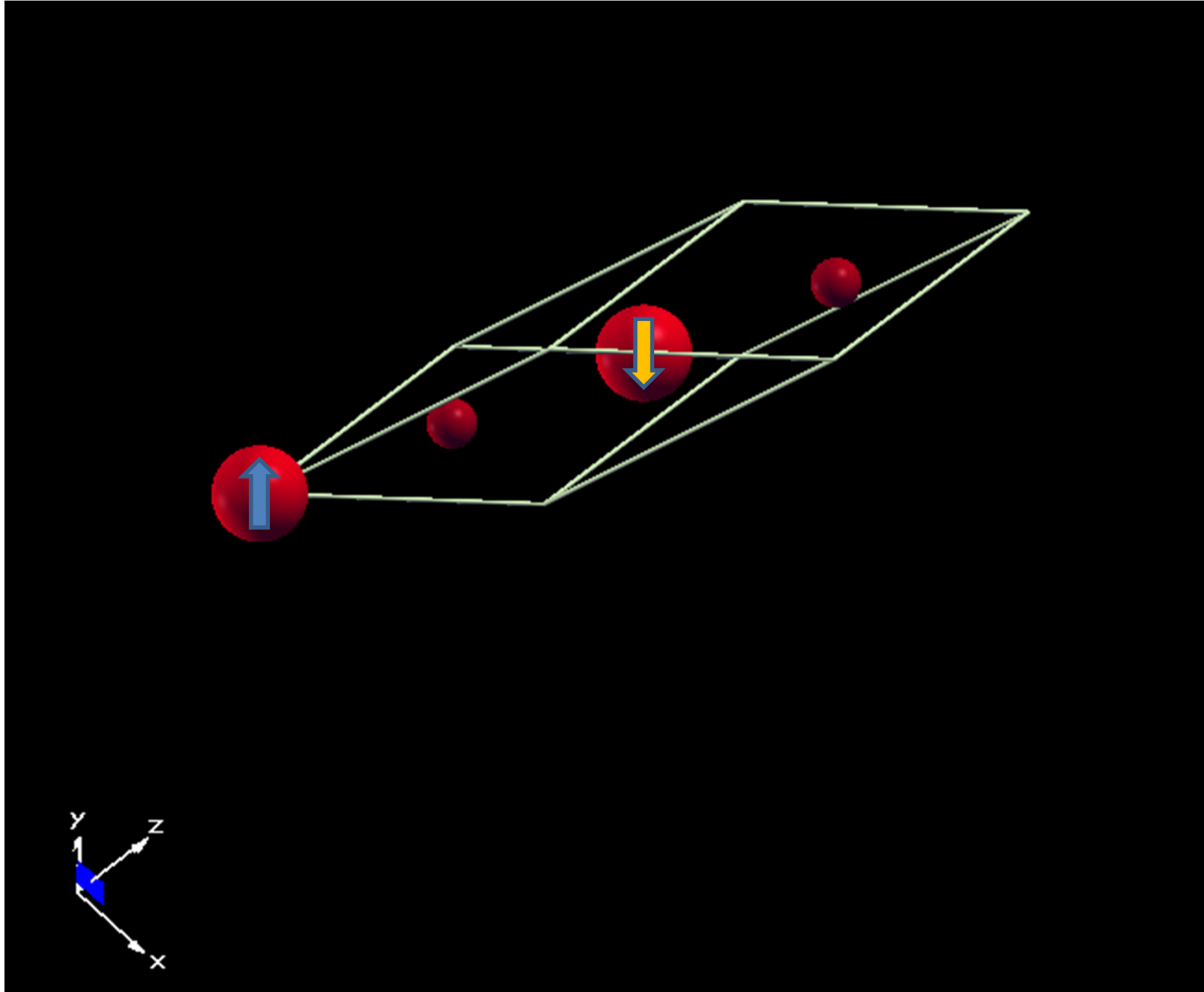
Fm-3m
a=4.194Å
b=4.194Å
c=4.194Å
 $\alpha=90.0^\circ$
 $\beta=90.0^\circ$
 $\gamma=90.0^\circ$



AF Type II Primitive Cell



Basic Asymmetric AF Cell

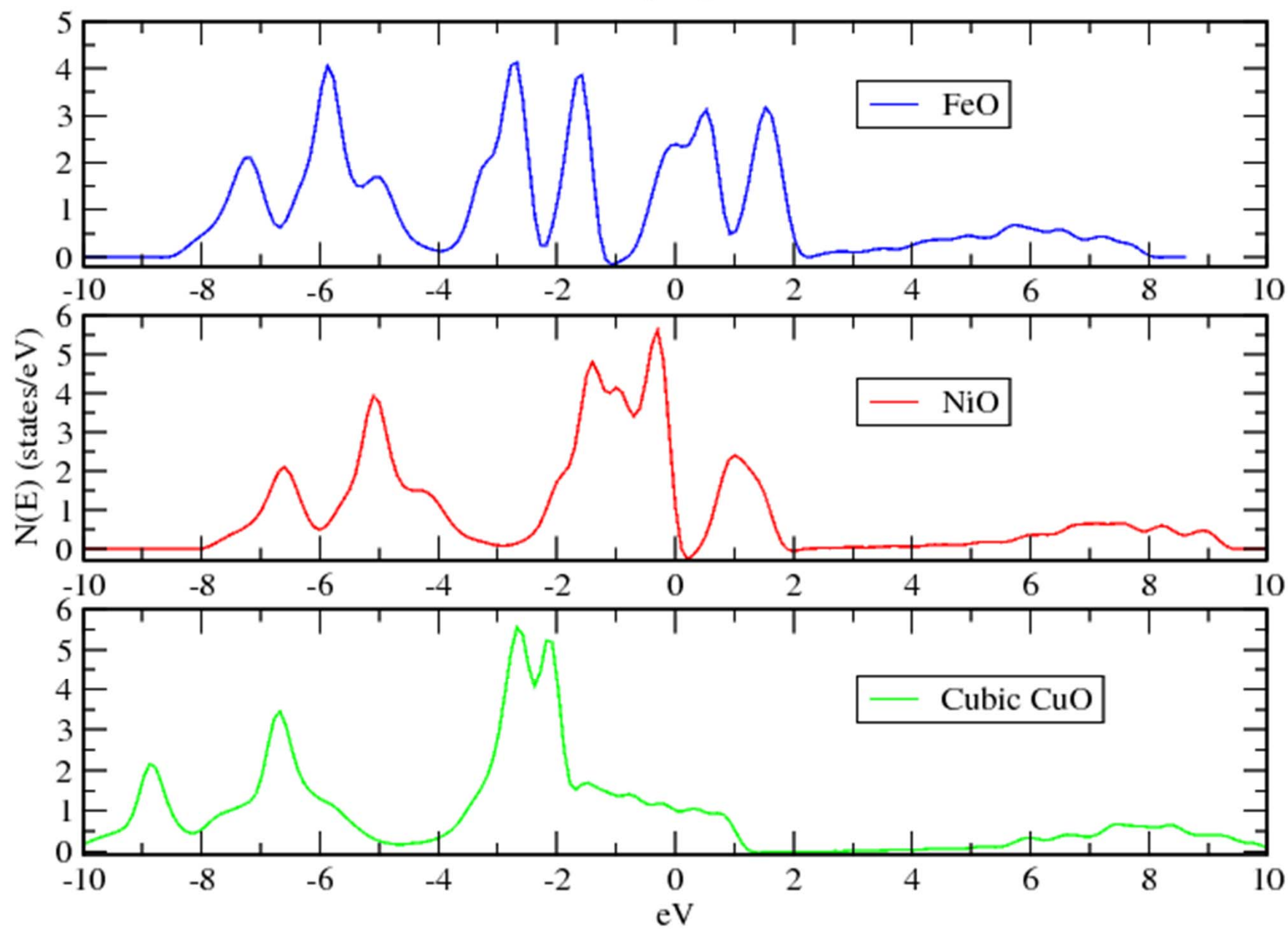


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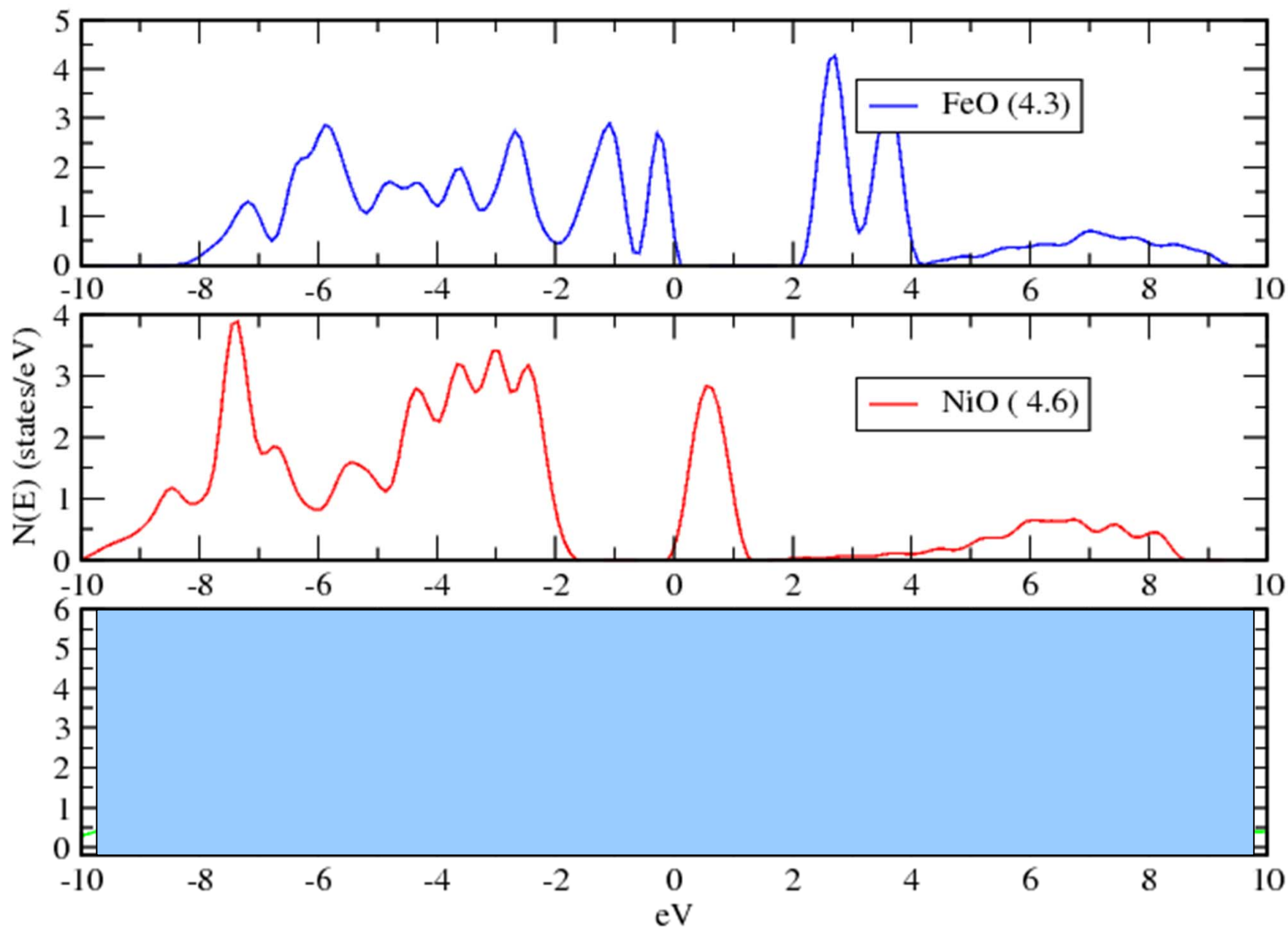
TMO_dos Plot

$U = 0$

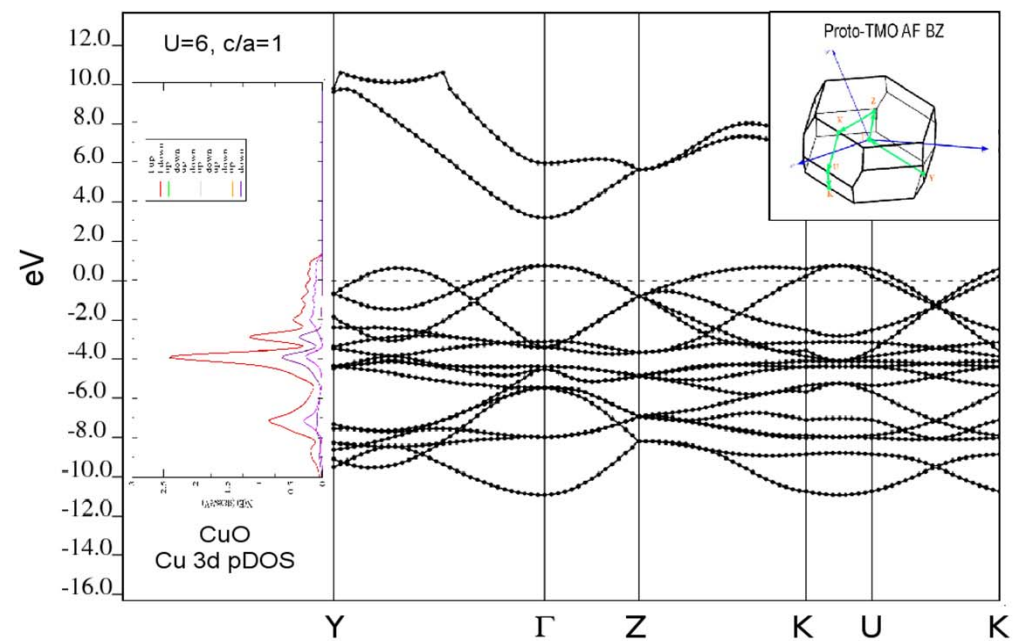
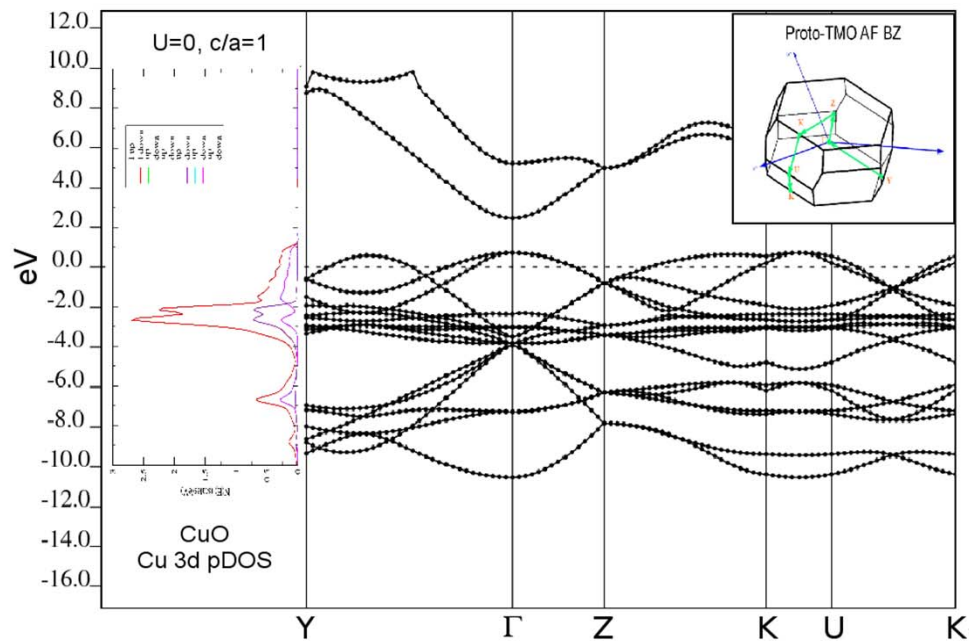
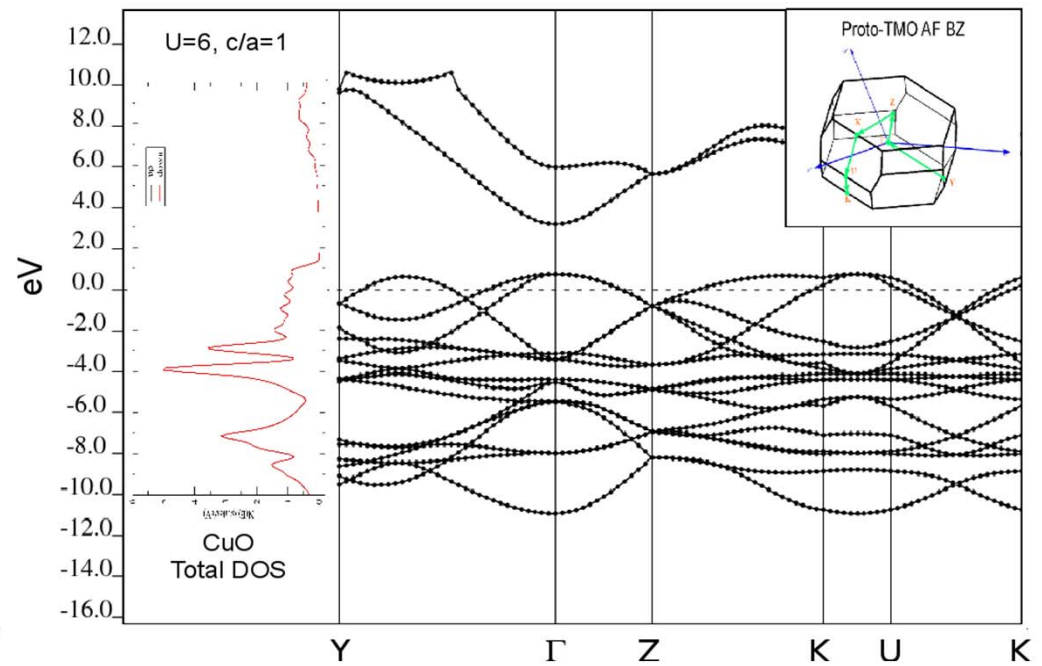
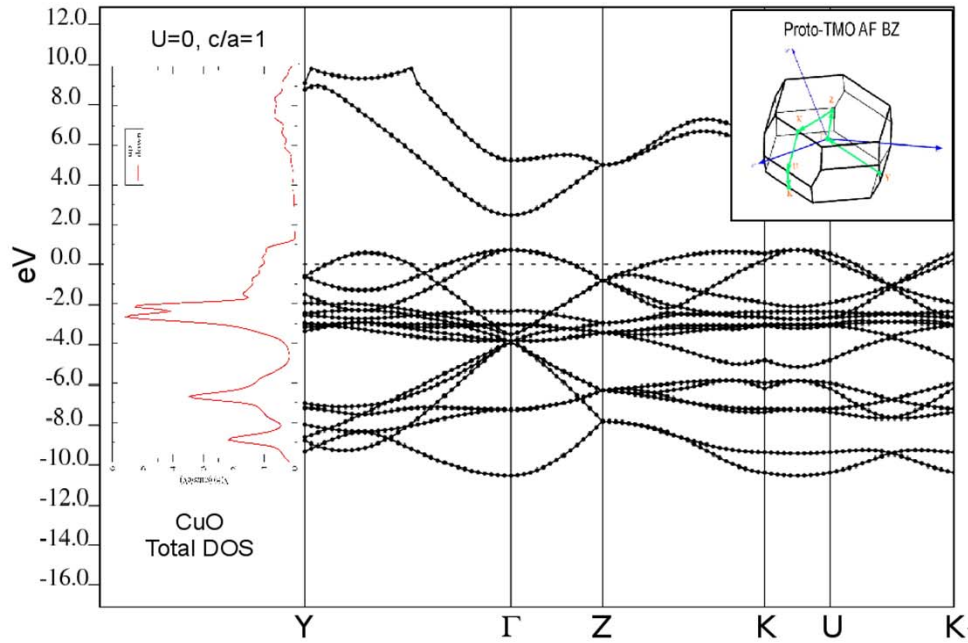


TMO_dos Plot

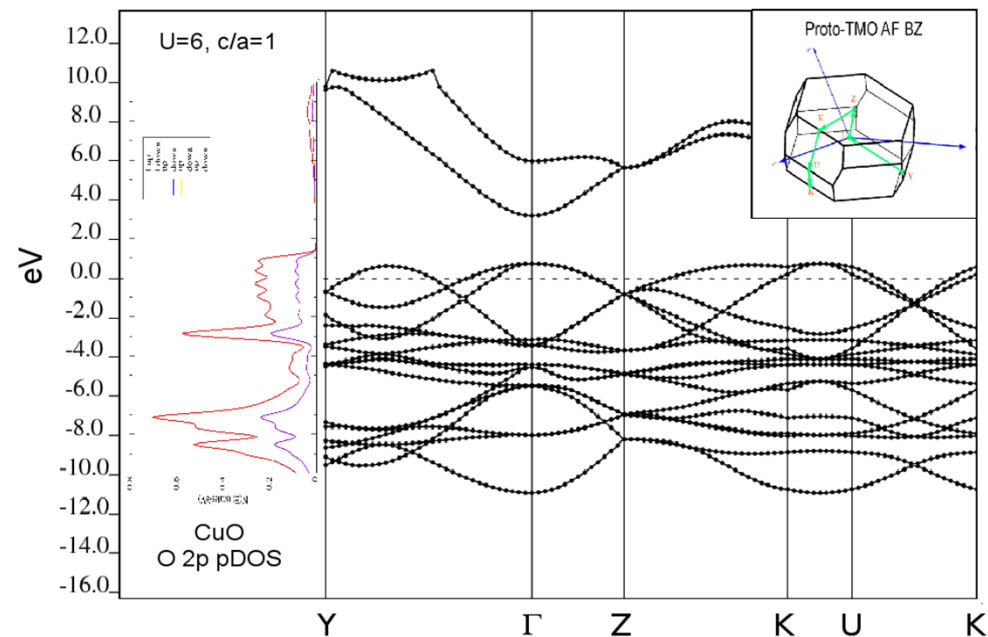
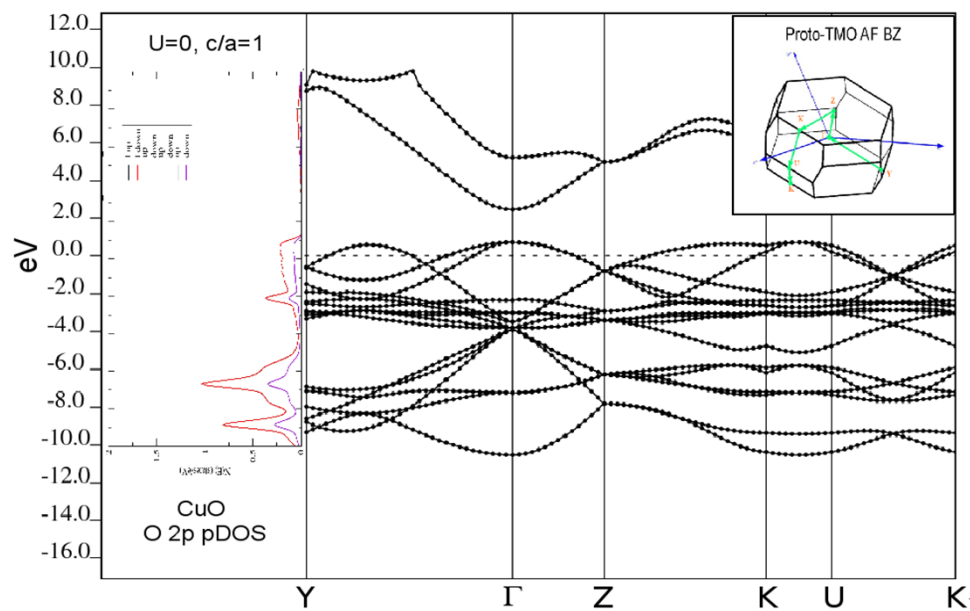
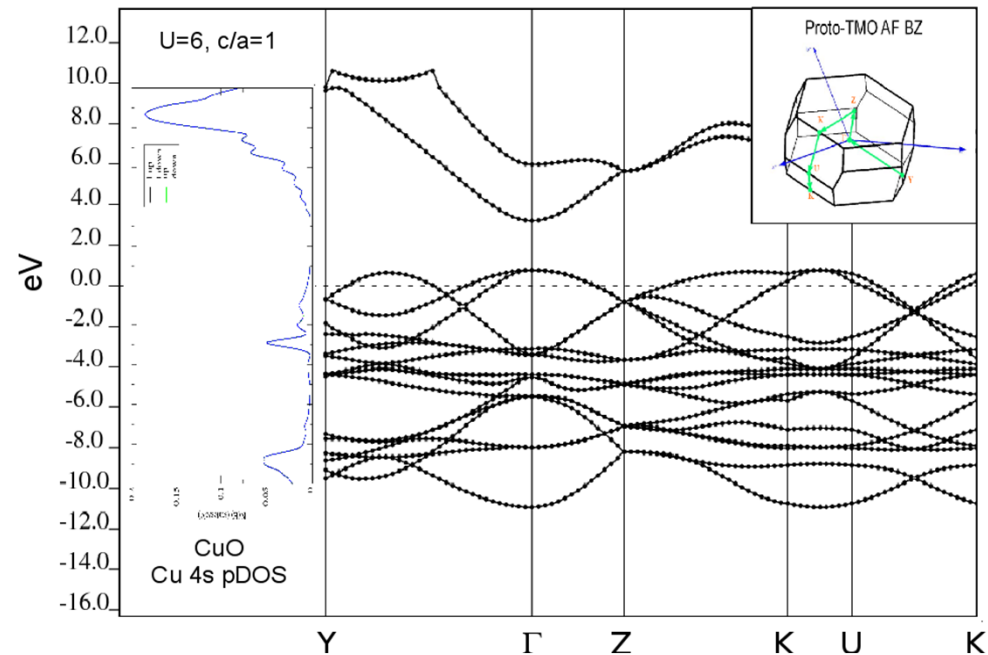
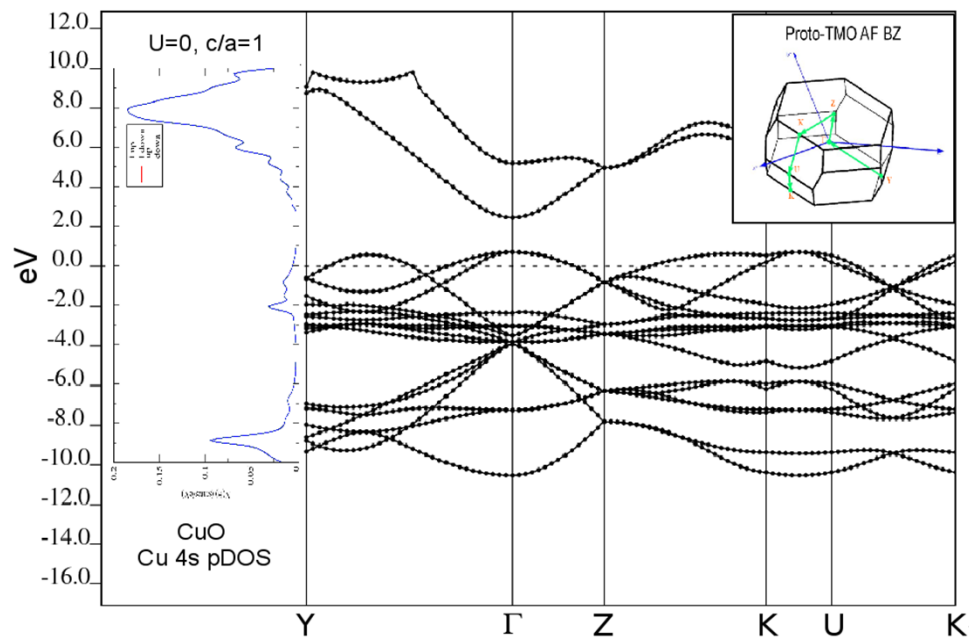
$U > 0$

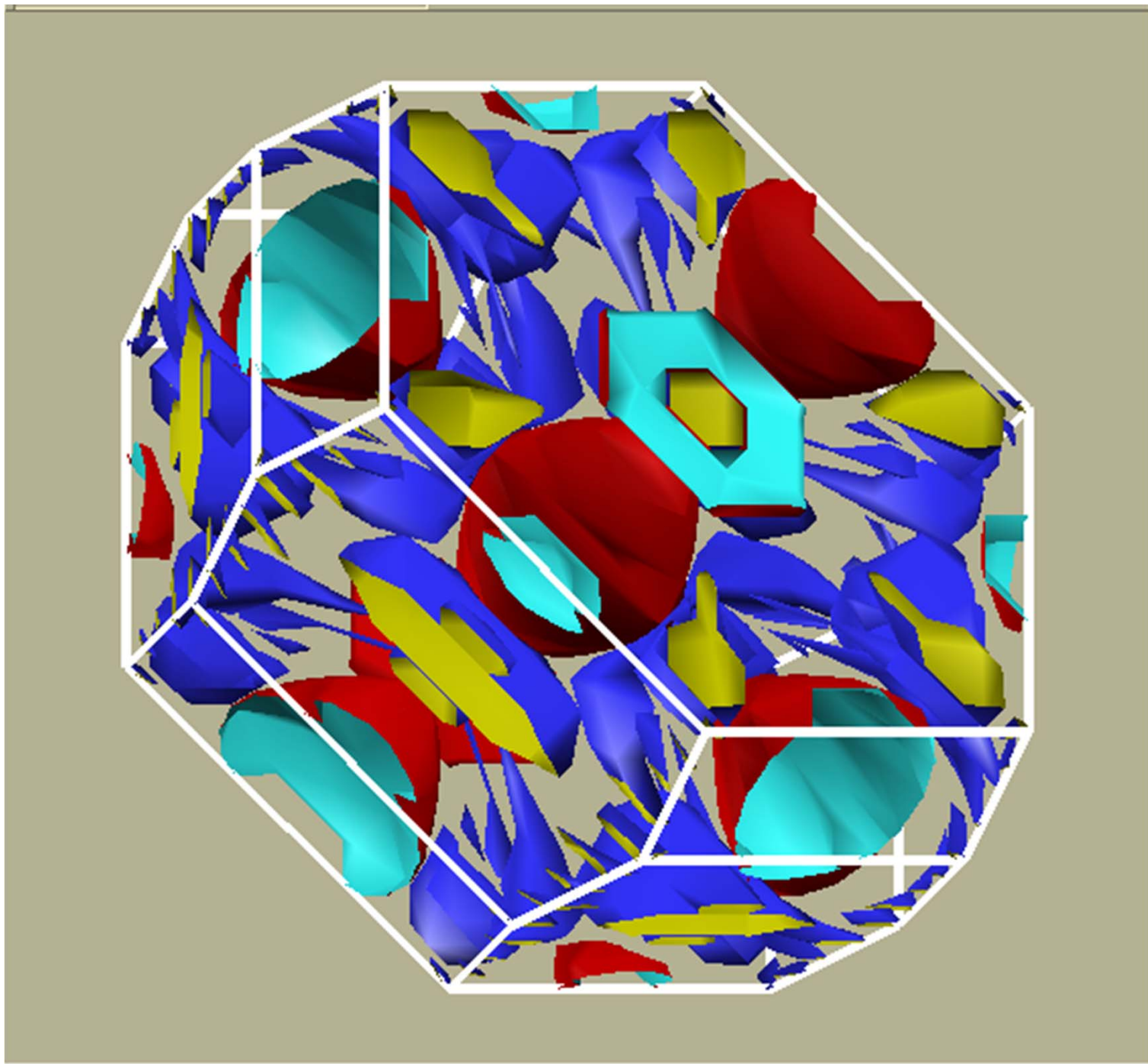


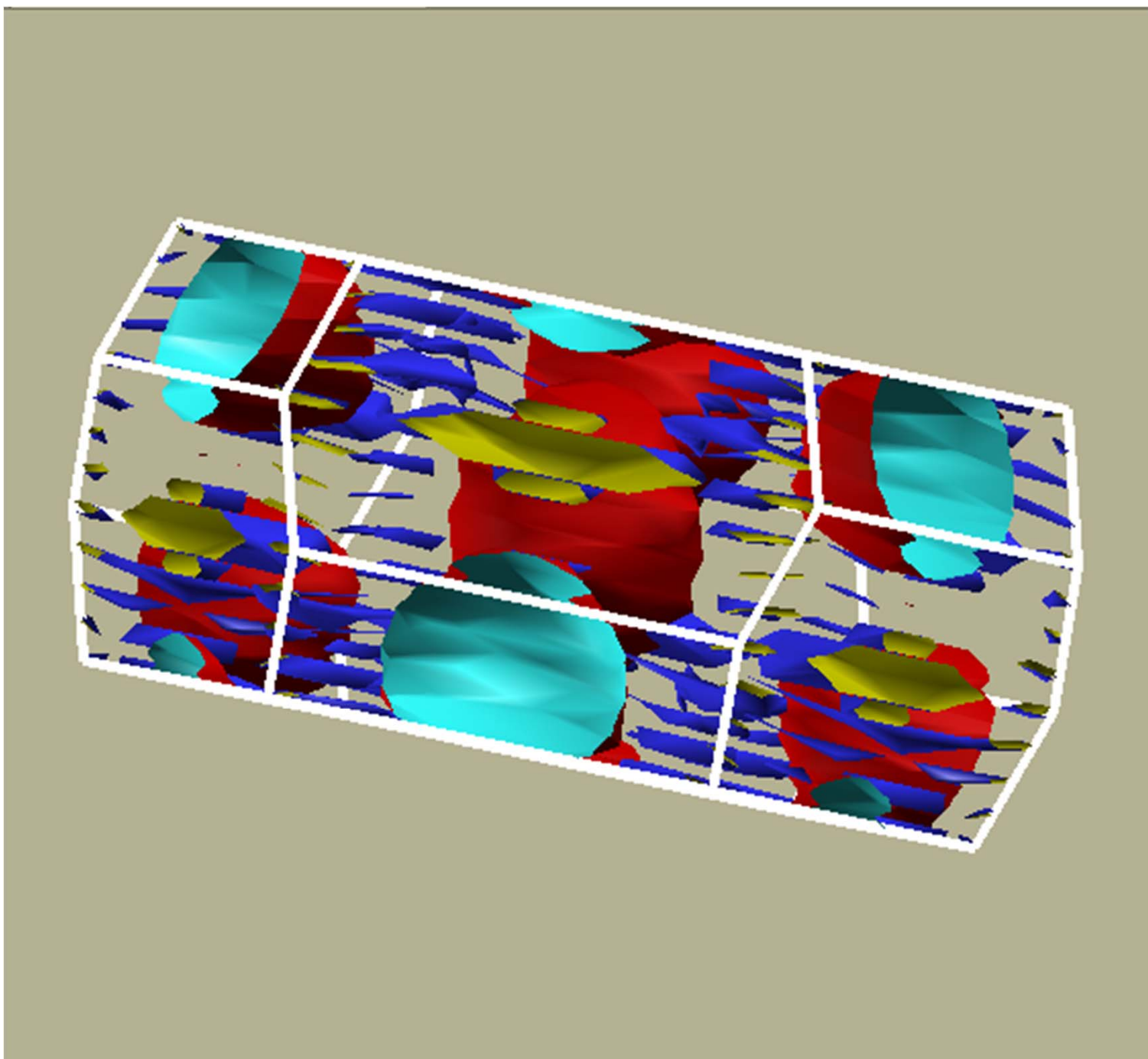
Cubic Rocksalt CuO



Cubic Rocksalt CuO (Cu 4s & O2p)







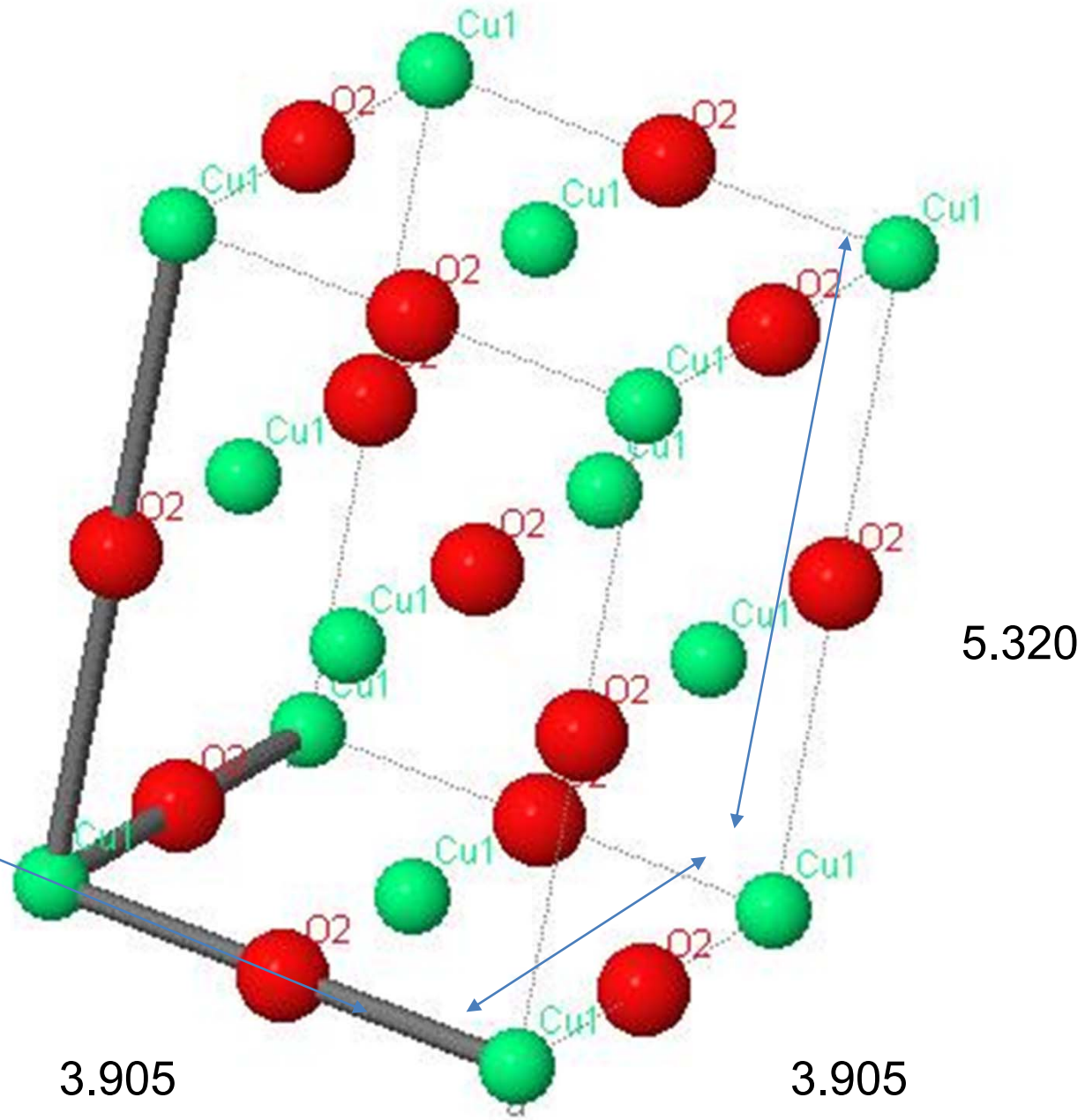
Tetragonal CuO

Fm-3m
a=3.905Å
b=3.905Å
c=5.320Å
α=90.0°
β=90.0°
γ=90.0°

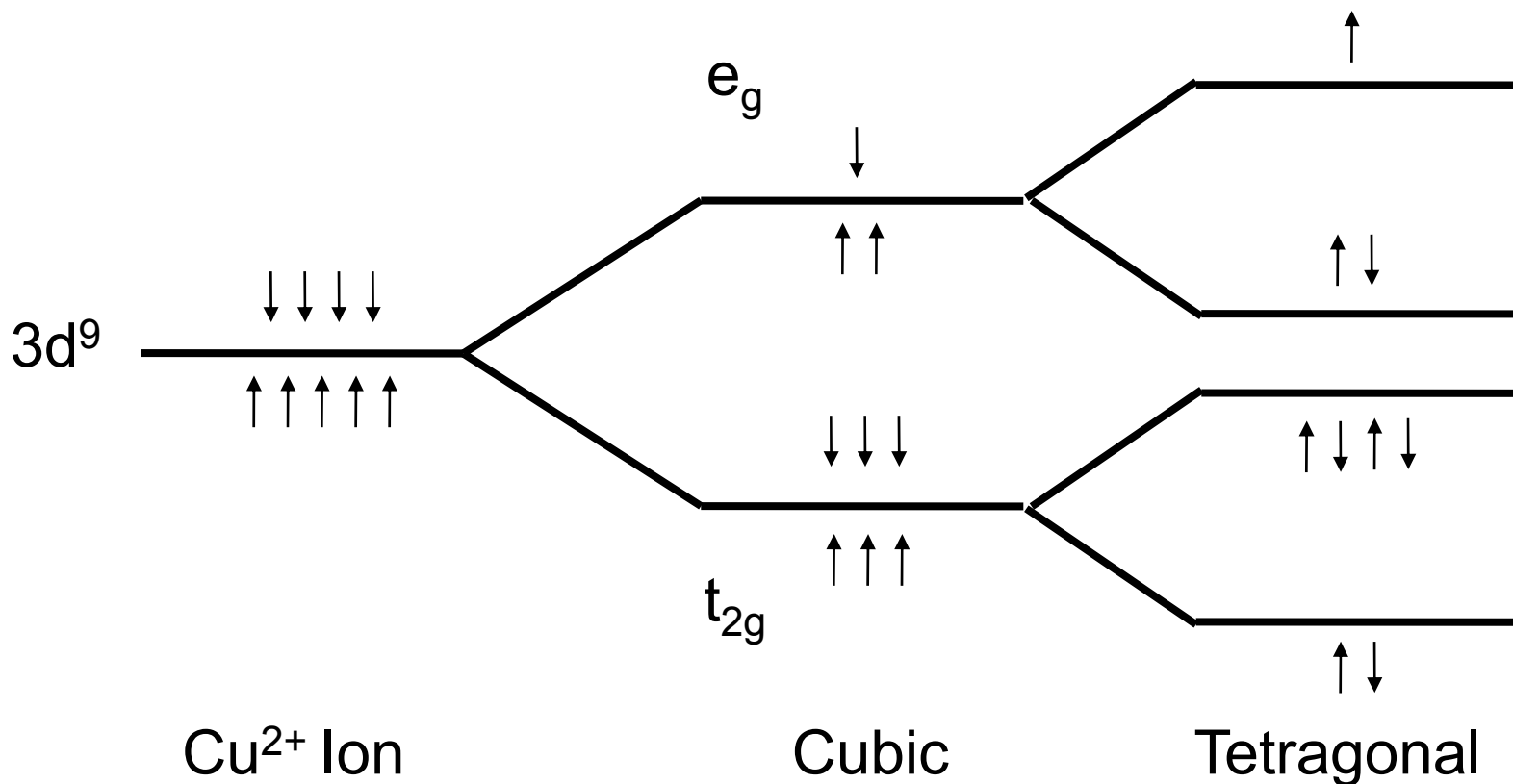
$$c/a = 1.36$$

Measurements (Wolter Siemons)

- 2-4 ML epi on STO
- No Fermi Edge
- No Exchange Bias on ferro-SRO (T_c ~ 100-150 K)

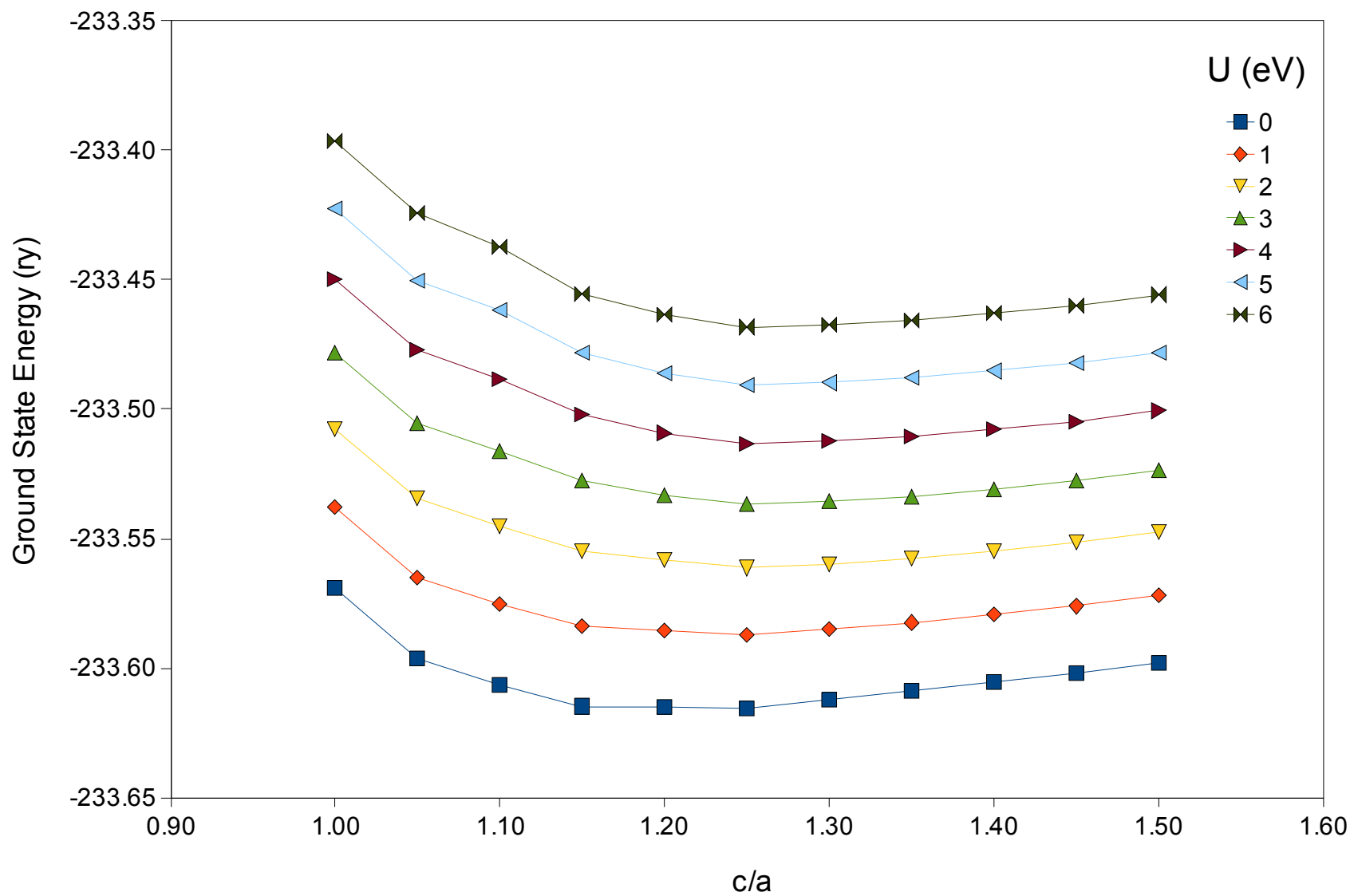


Cu²⁺ 3d Multiplet Splitting (Tetra)



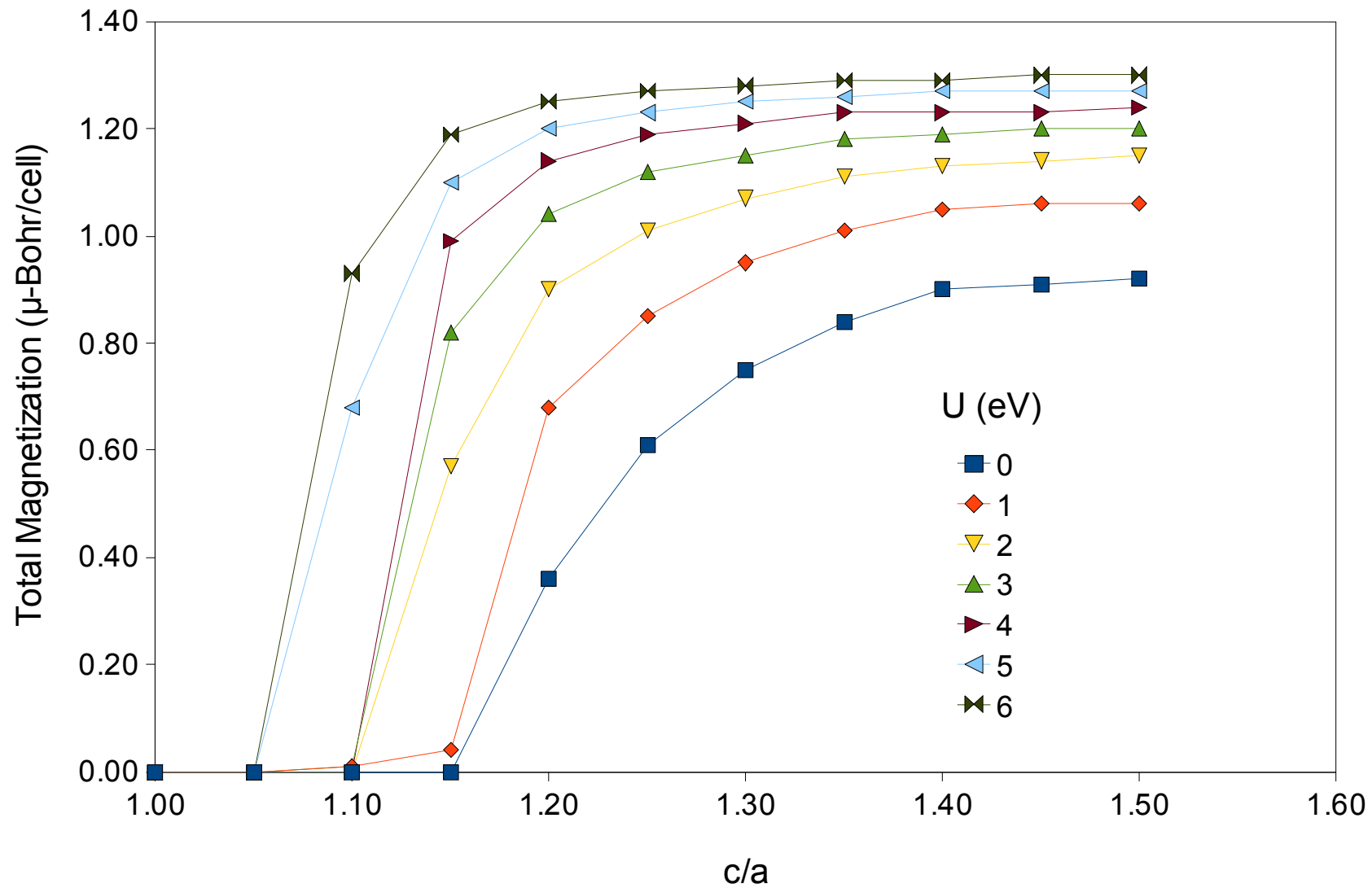
Rocksalt CuO - $a = 3.905$ Angstroms, PP = Cu.pz-3d9_4s2-rrkjus.UPF

Ground State Energy vs c/a & U (ev)

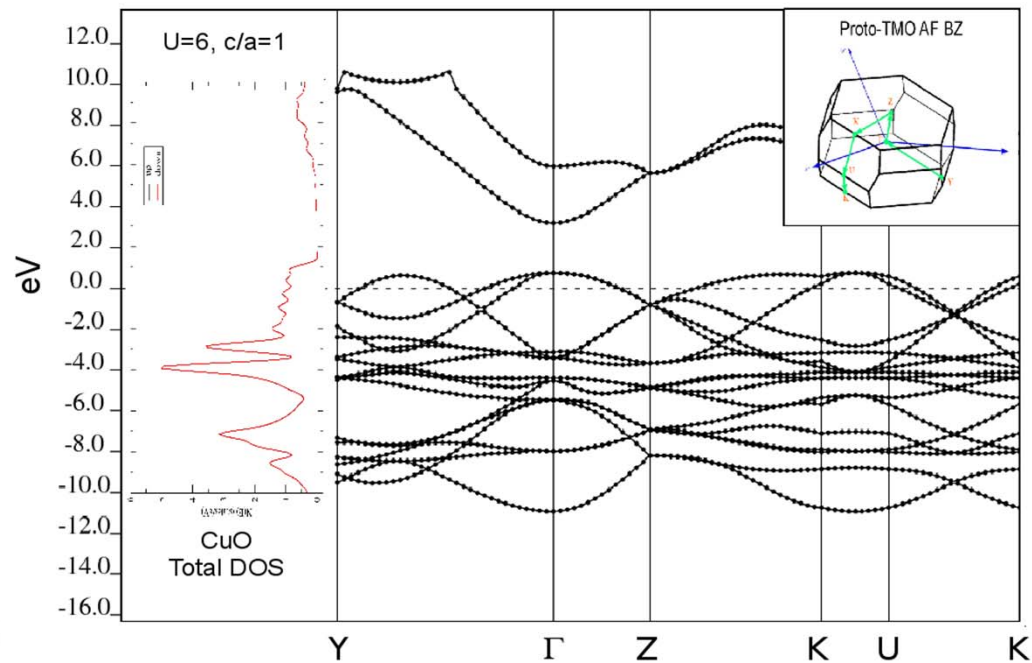
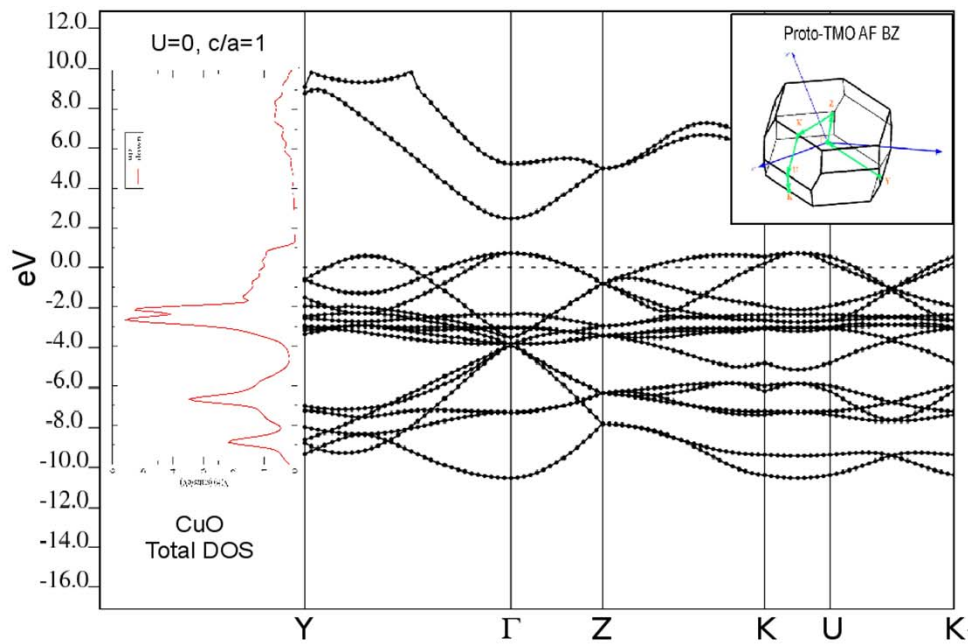


Rocksalt CuO - $a = 3.905 \text{ \AA}$, PP = Cu.pz-3d9_4s2-rrkjus.UPF

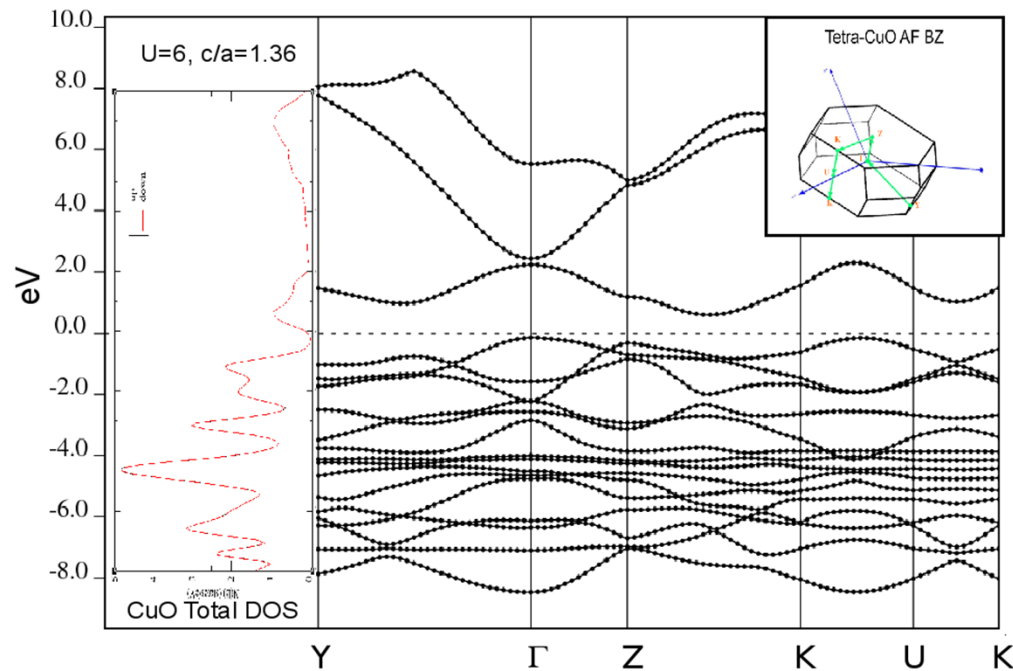
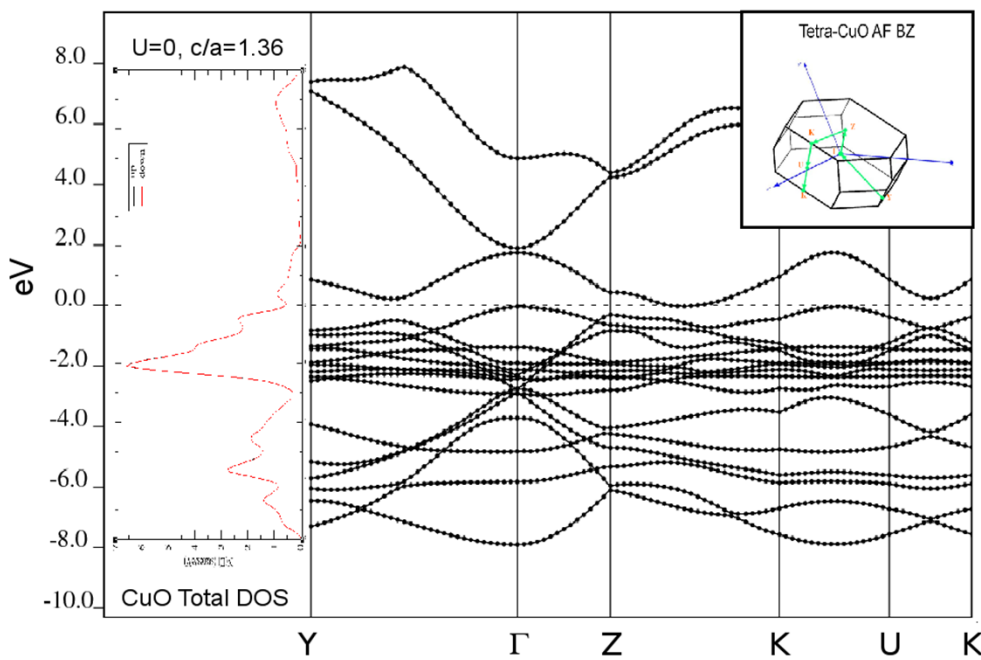
Total Magnetization vs c/a & $U(\text{eV})$



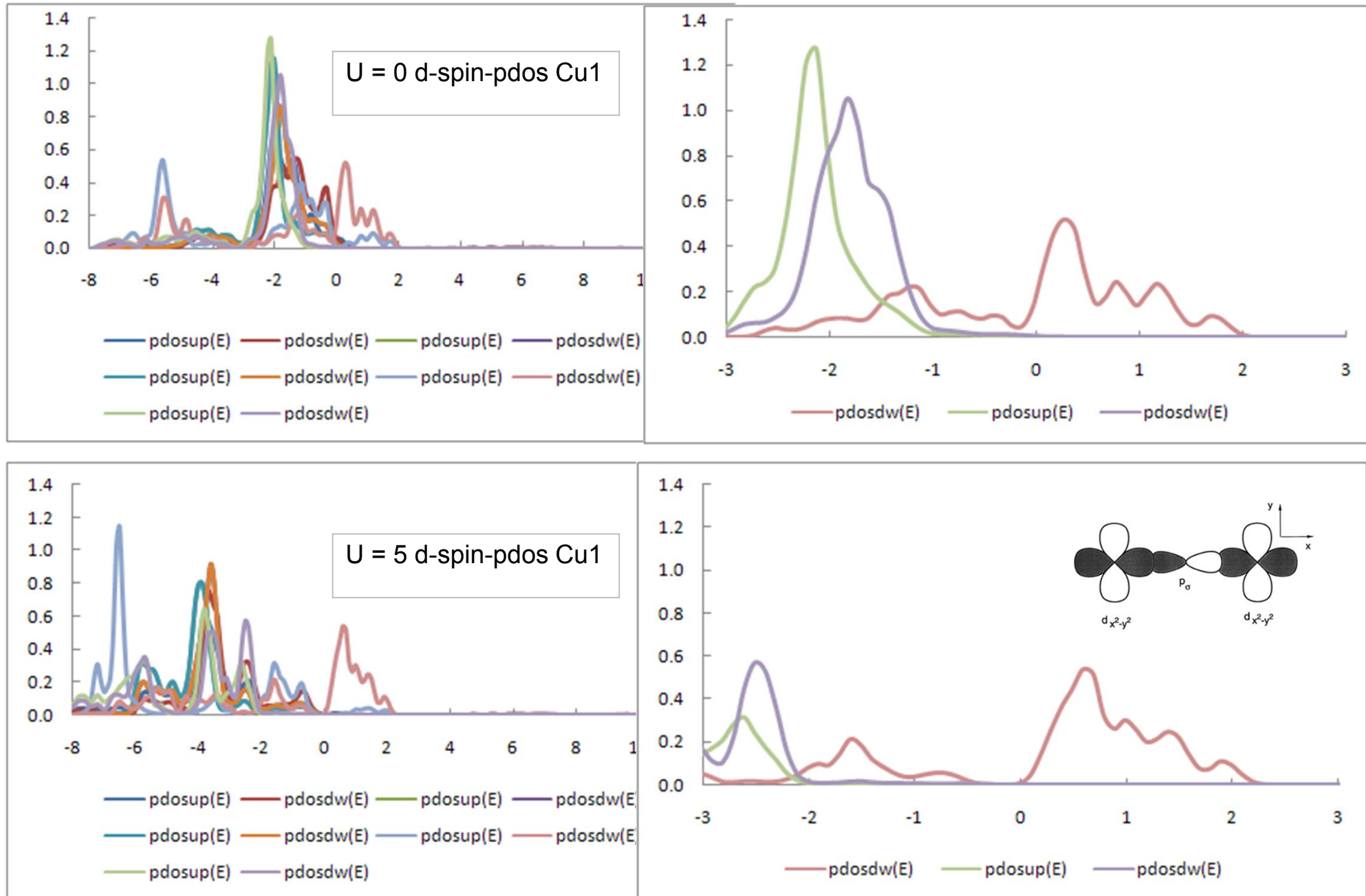
Cubic



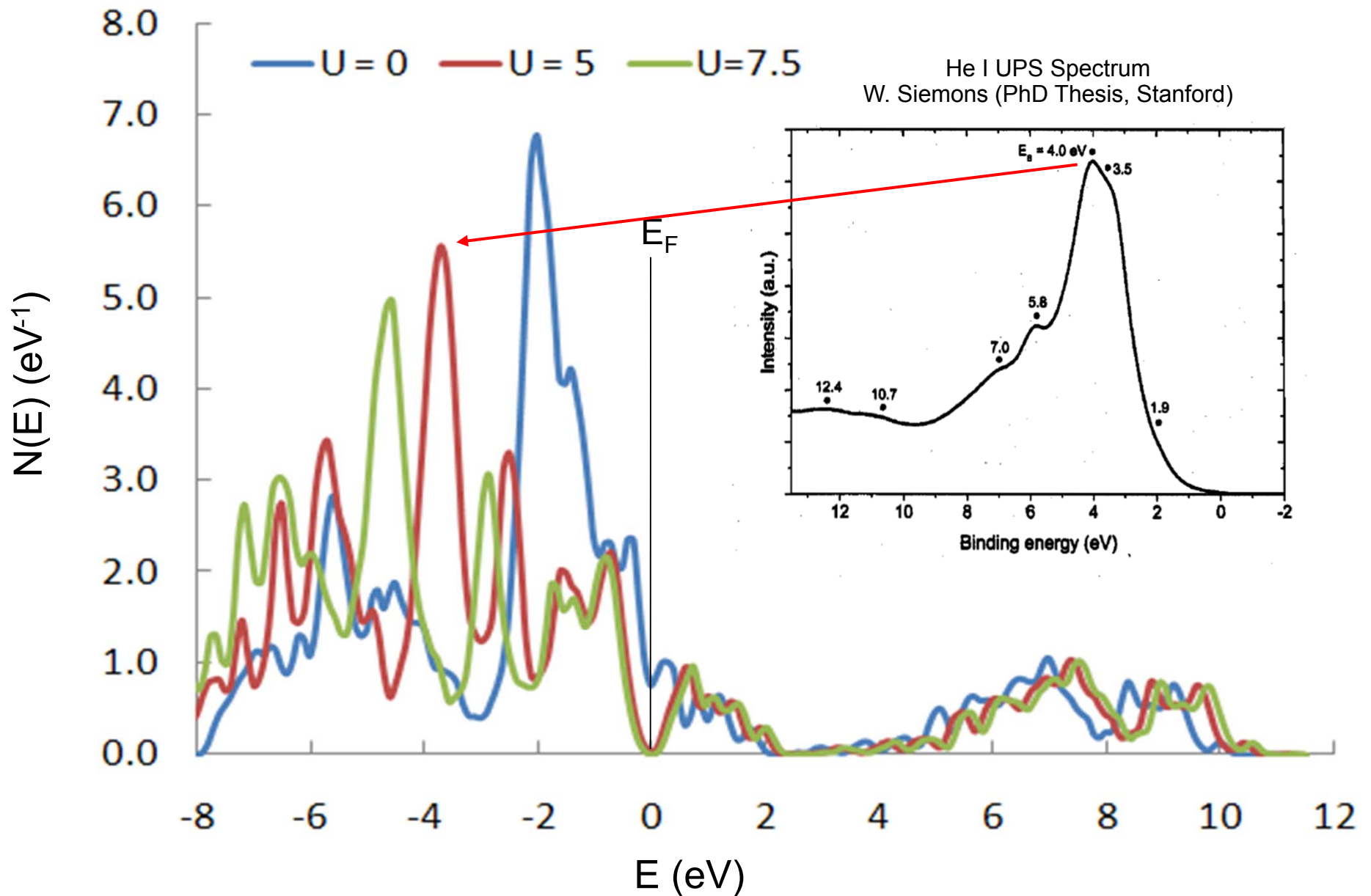
Tetragonal



Spin Composition of Cu 3d pDOS as fn(Hubbard): $c/a = 1.36$

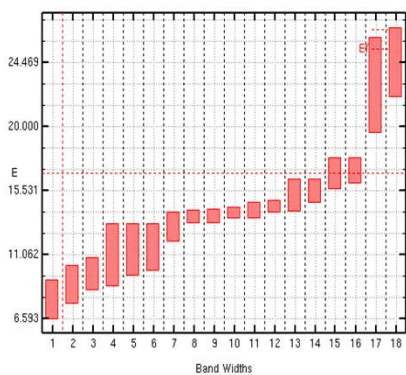


t-CuO Density-of-States

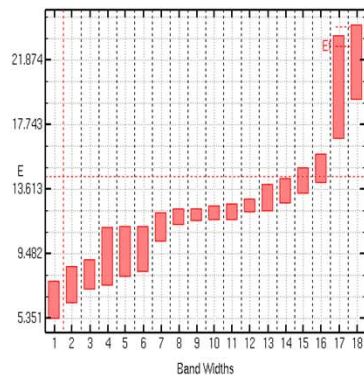


Af-CuO: Spin Up Bands

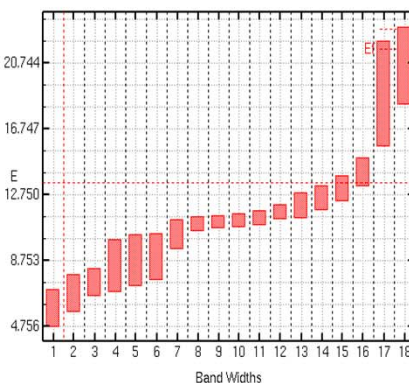
$$\underline{U = 0}$$



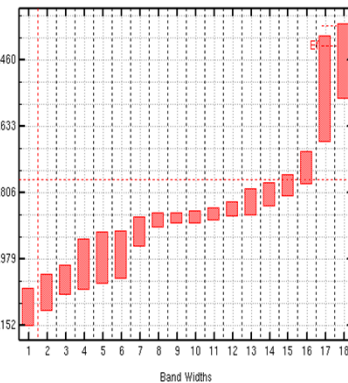
1.0



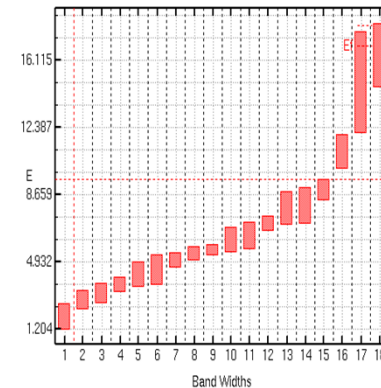
1.1



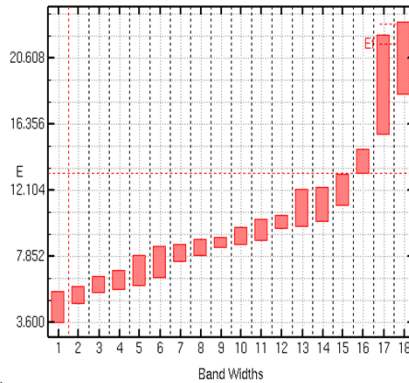
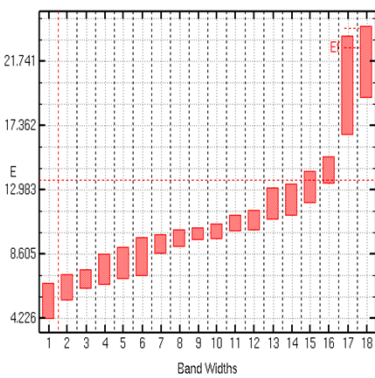
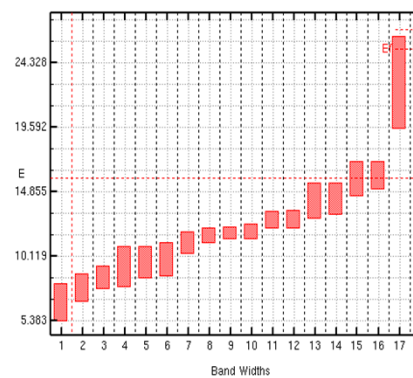
$\underline{c/a}$
1.115



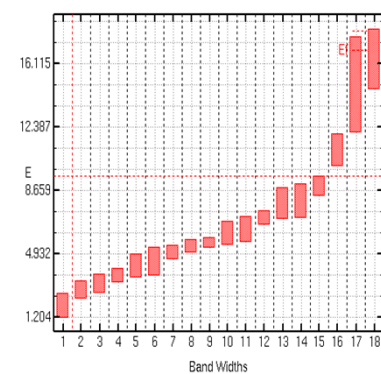
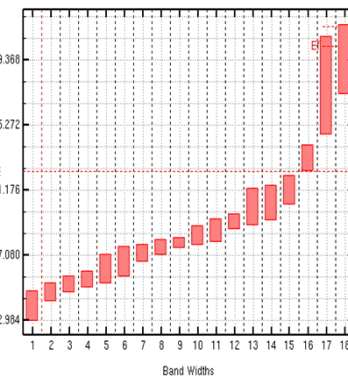
1.2



1.36

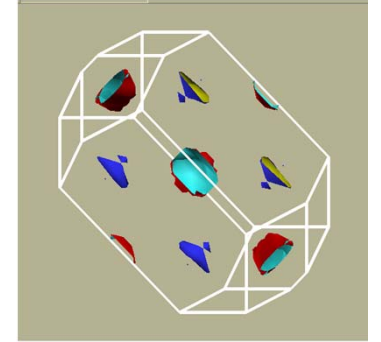
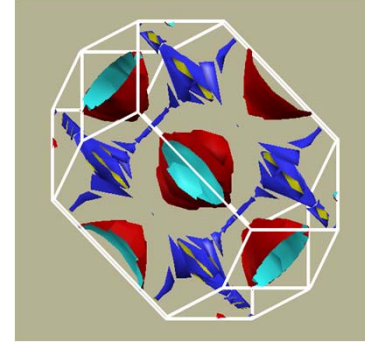
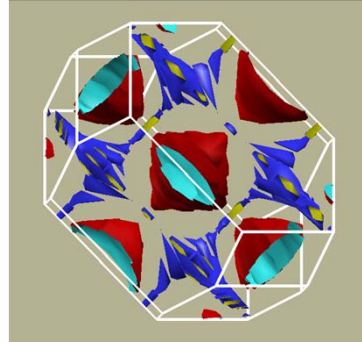
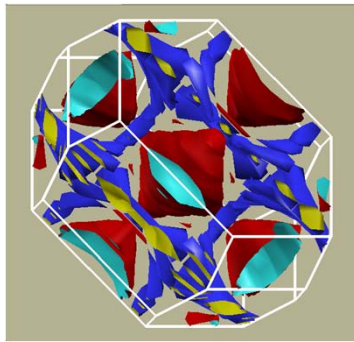
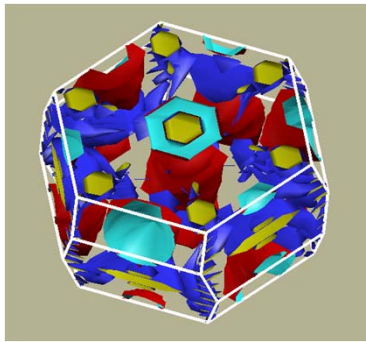


$$\underline{U = 6}$$



Af-CuO: FS Spin Up

U = 0



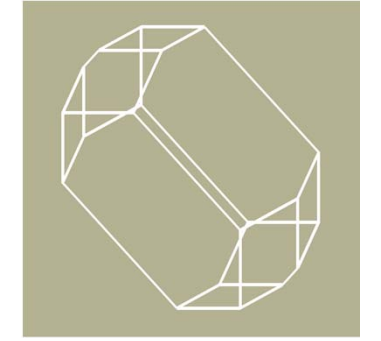
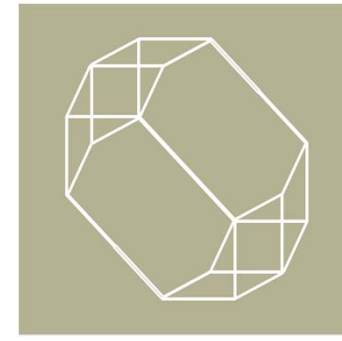
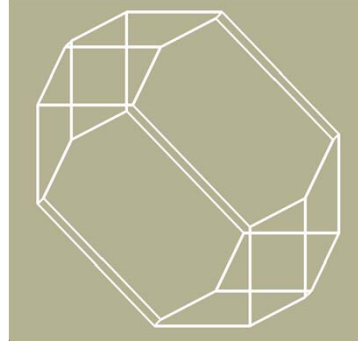
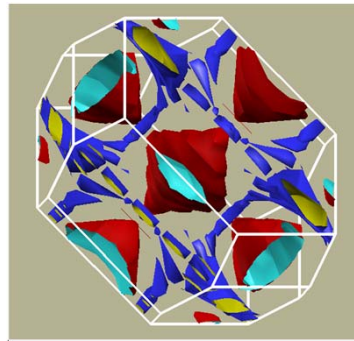
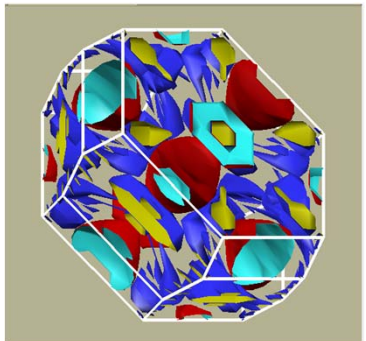
1.0

1.1

c/a
1.115

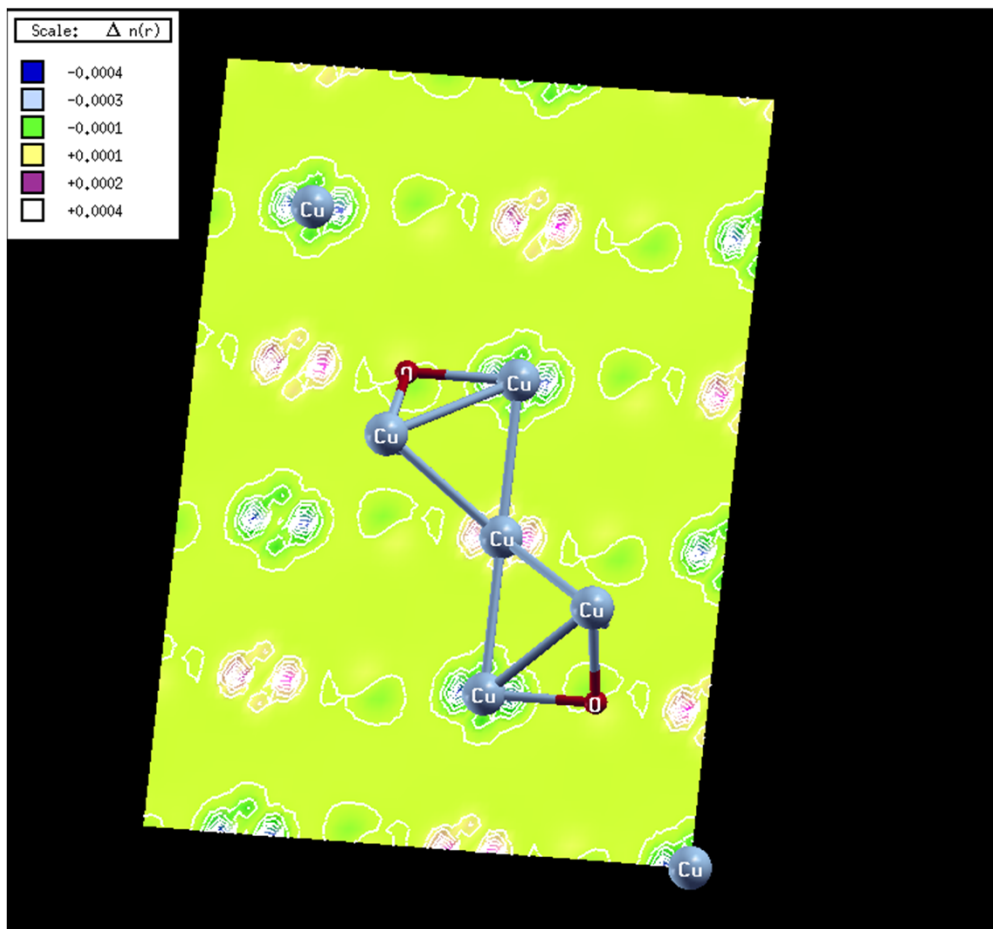
1.2

1.36

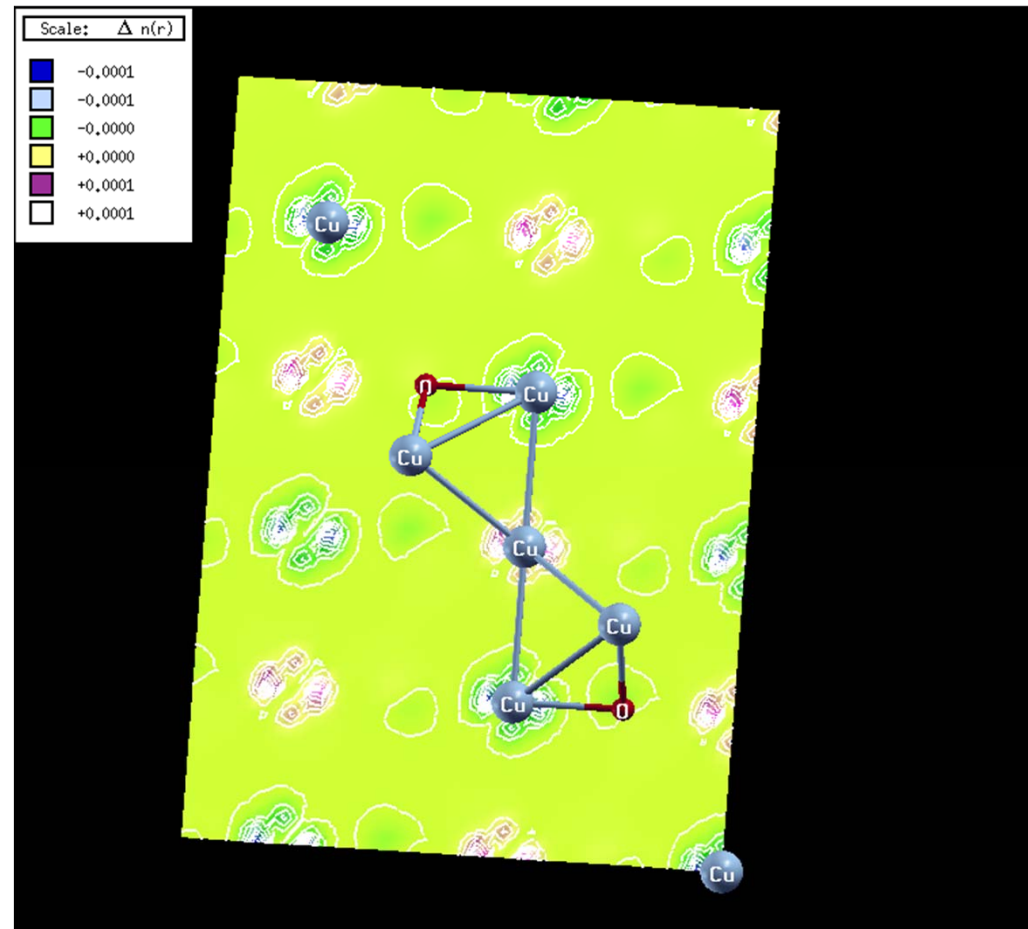


U = 6

$$c/a = 1.00$$

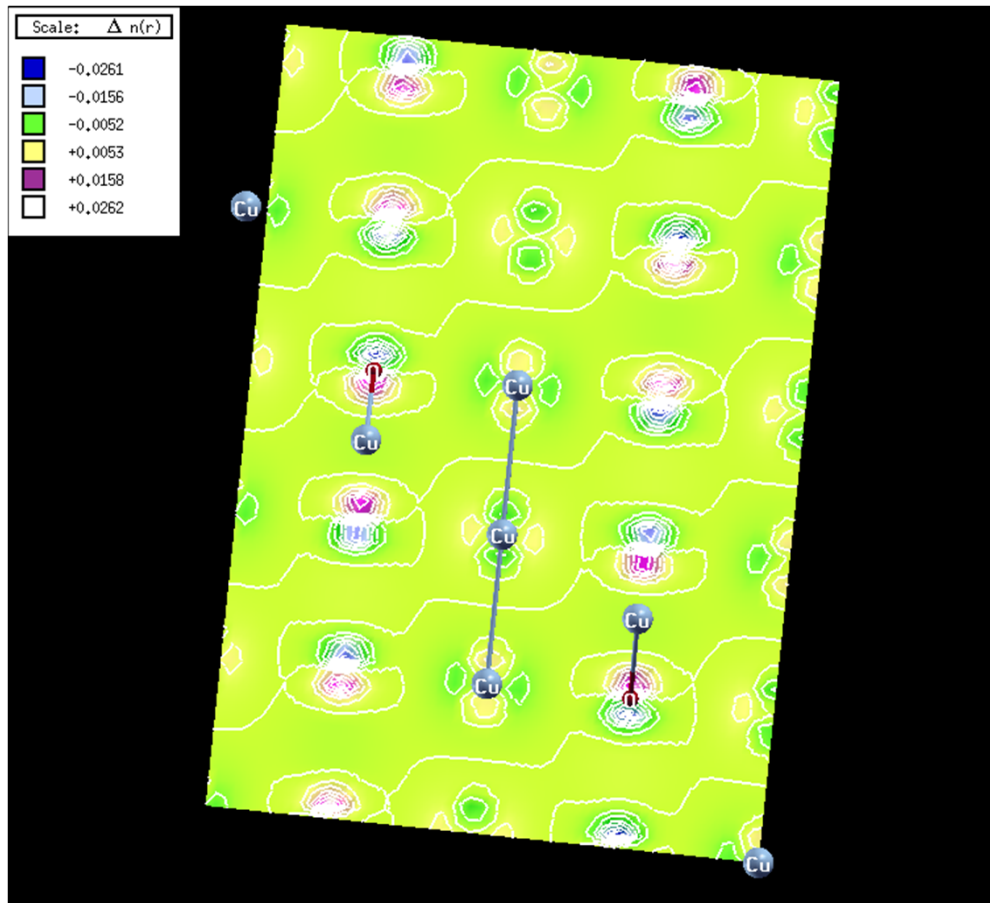


$$U = 0$$

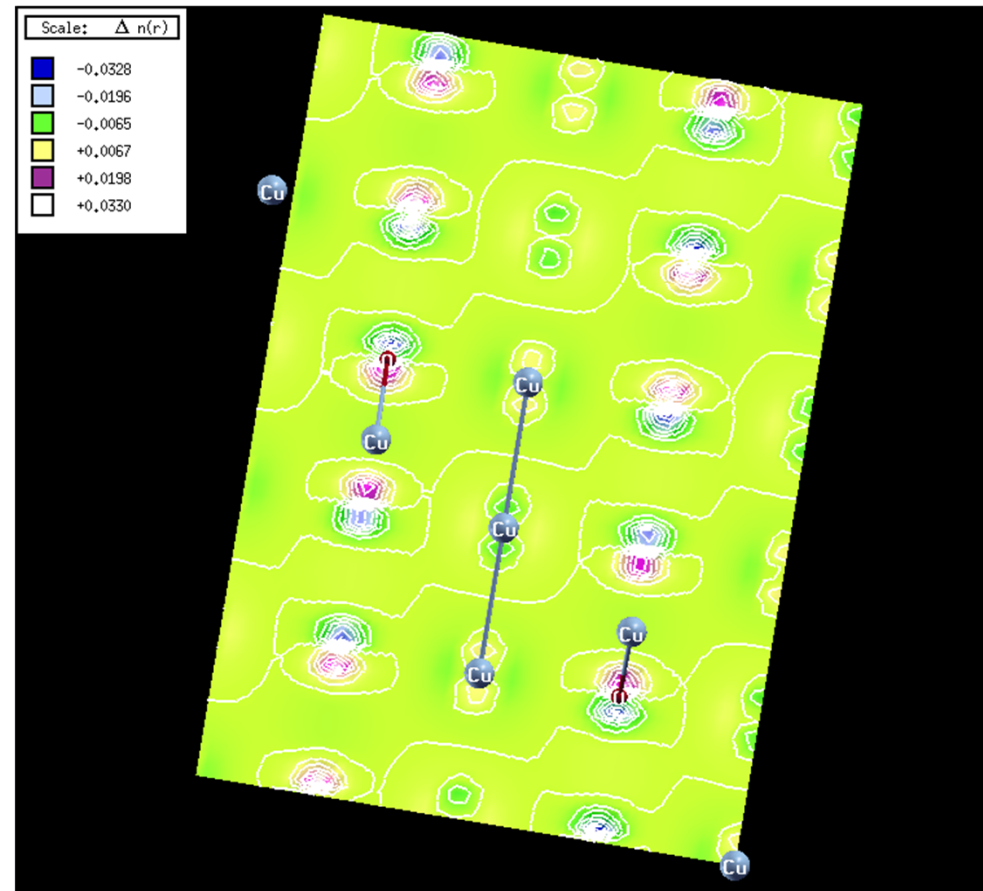


$$U = 6$$

$$c/a = 1.36$$



$$U = 0$$



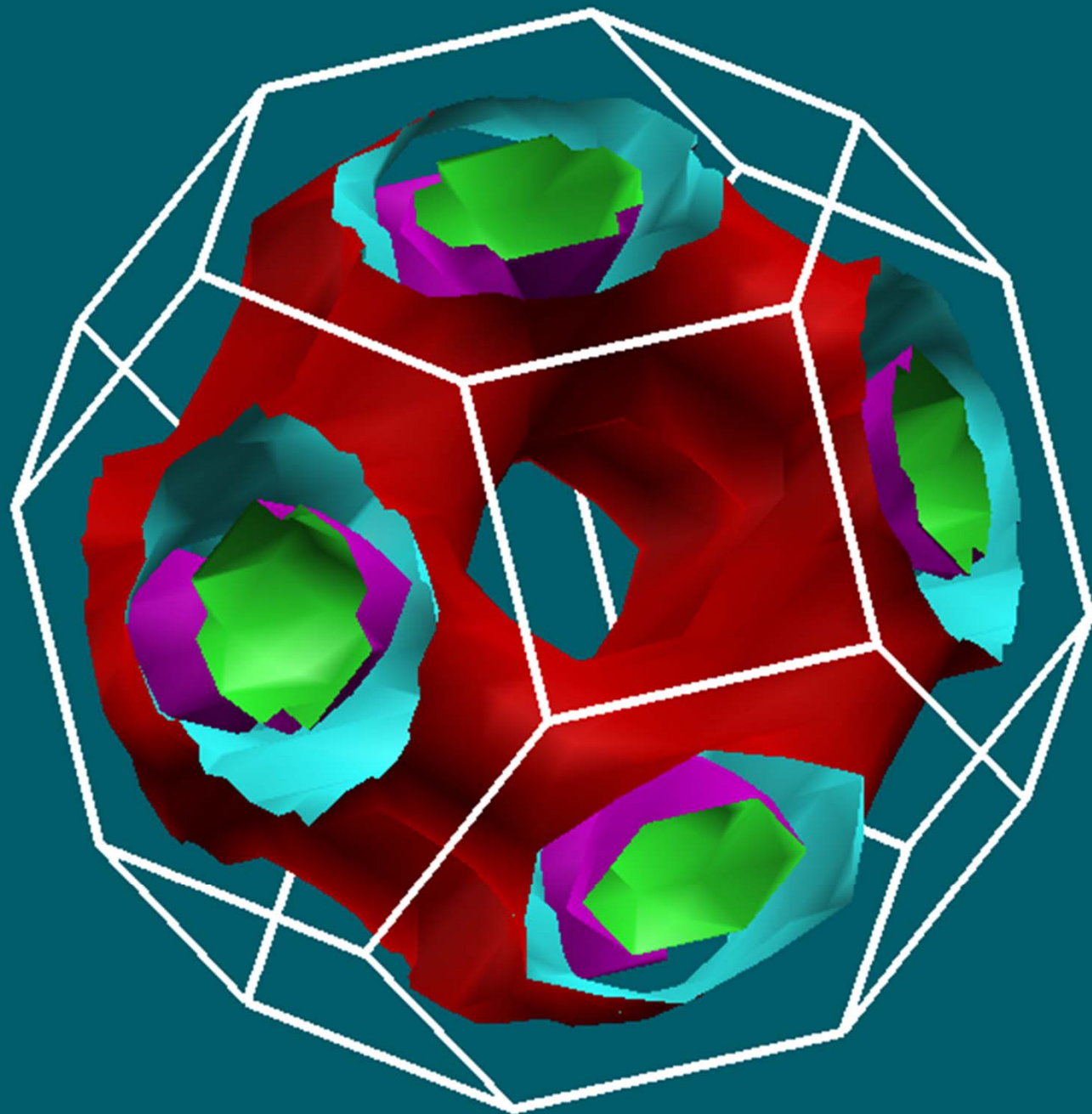
$$U = 6$$

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Electron-Phonon Coupling - Superconductivity -

- QE package for e-p coupling with spin-polarized bands still “under construction,” so...
- Since the bands near the Fermi level hardly change from $U = 0$ to $U = 6$, let's...
- Just ignore the AF II symmetry and see what happens!



Electron-Phonon Coupling a la Migdal-Eliashberg-McMillan

(plus Allen & Dynes)

$$H_{el-ph} = \sum_{\mathbf{k}q\nu} g_{\mathbf{k}+\mathbf{q},\mathbf{k}}^{q\nu,mn} c_{\mathbf{k}+\mathbf{q}}^{\dagger m} c_{\mathbf{k}}^n (b_{-\mathbf{q}\nu}^{\dagger} + b_{\mathbf{q}\nu}) \quad (1)$$

$$\alpha^2 F(\omega) = \frac{1}{N(\varepsilon_F)} \sum_{mn} \sum_{q\nu} \delta(\omega - \omega_{q\nu}) \sum_{\mathbf{k}} |g_{\mathbf{k}+\mathbf{q},\mathbf{k}}^{q\nu,mn}|^2 \\ \times \delta(\varepsilon_{\mathbf{k}+\mathbf{q},m} - \varepsilon_F) \delta(\varepsilon_{\mathbf{k},n} - \varepsilon_F), \quad (2)$$

$$\lambda = 2 \int \frac{\alpha^2 F(\omega)}{\omega} d\omega = \sum_{q\nu} \lambda_{q\nu}, \quad (3)$$

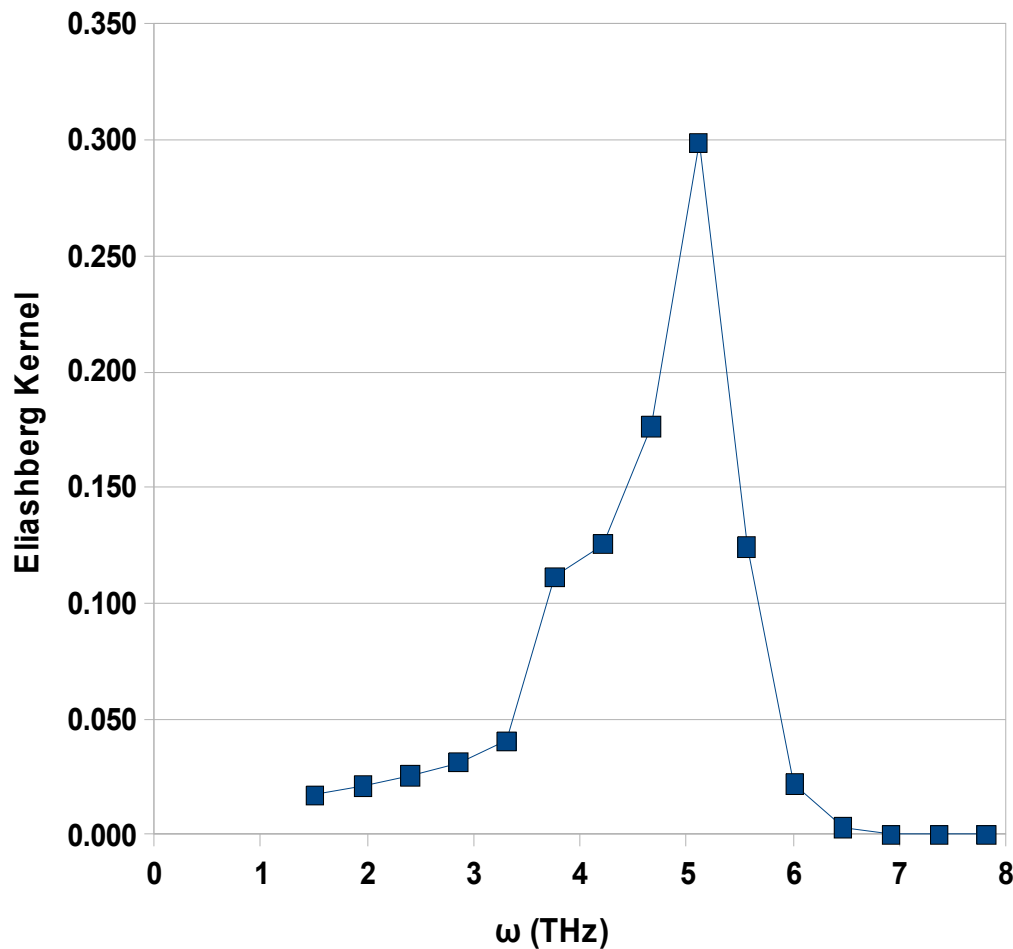
$$\lambda_{q\nu} = \frac{2}{N(\varepsilon_F)\omega_{q\nu}} \sum_{mn} \sum_{\mathbf{k}} |g_{\mathbf{k}+\mathbf{q},\mathbf{k}}^{q\nu,mn}|^2 \\ \times \delta(\varepsilon_{\mathbf{k}+\mathbf{q},m} - \varepsilon_F) \delta(\varepsilon_{\mathbf{k},n} - \varepsilon_F). \quad (4)$$

Wierzbowska, et al, arXiv:cond-mat/0504077 (2006) (Nb)

Non-Magnetic Cubic Rocksalt CuO

-- Electron-Phonon Properties --

$\alpha^2F(\omega)$



$\sigma = 0.04$

- $\lambda \sim 0.6 - 0.7$

- Other sc's...

$$T_C = a\Theta e^{-\frac{1}{\lambda - \mu^*}}$$

$$\lambda k\Theta \ll E_F$$

	T_C (K)	λ	μ^*
K_3C_{60}	16.3	0.51	-
Rb_3C_{60}	30.5	0.61	-
Cs_3C_{60}	47.4	0.72	-

Agenda

- ...Still No Theory
- Structural Issues
- “Experimental Apparatus”
- Band Structure, DOS and Fermiology
- Superconductivity
- **The da Vinci Code**
- Conclusions/Homework

Does the

DAVINCI CODE

Hold the Key to Room Temperature
Superconductivity?

Paul M. Grant

Visiting Scholar, Stanford

IBM Research Staff Member Emeritus

EPRI Science Fellow (Retired)

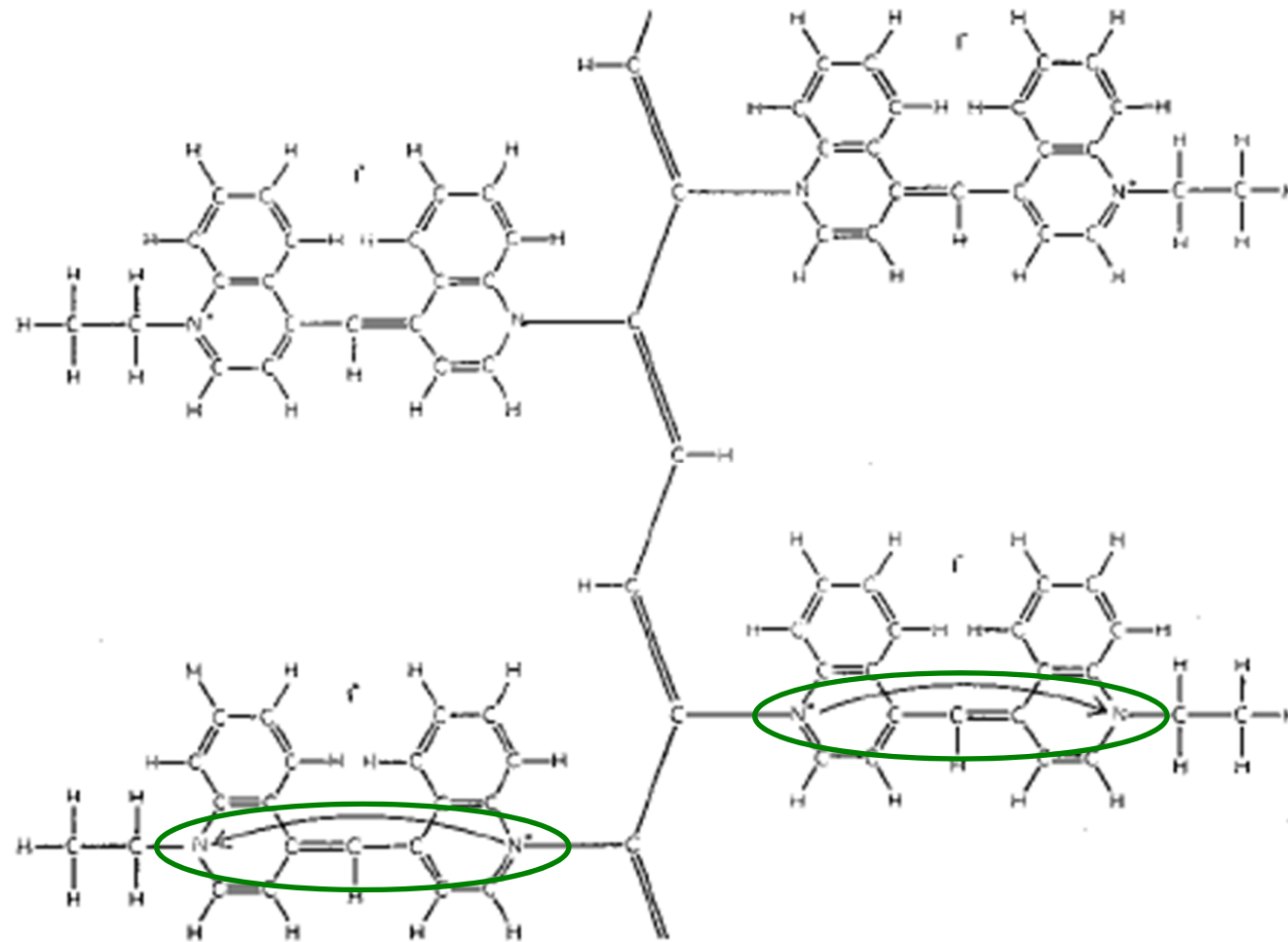
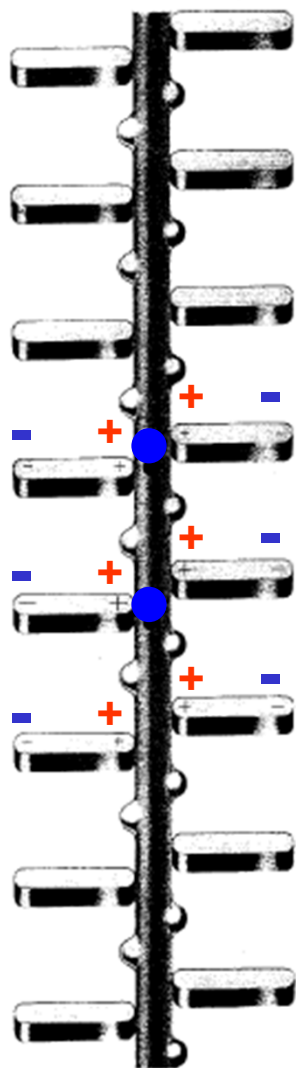
Principal, W2AGZ Technologies

The Road to Room Temperature Superconductivity

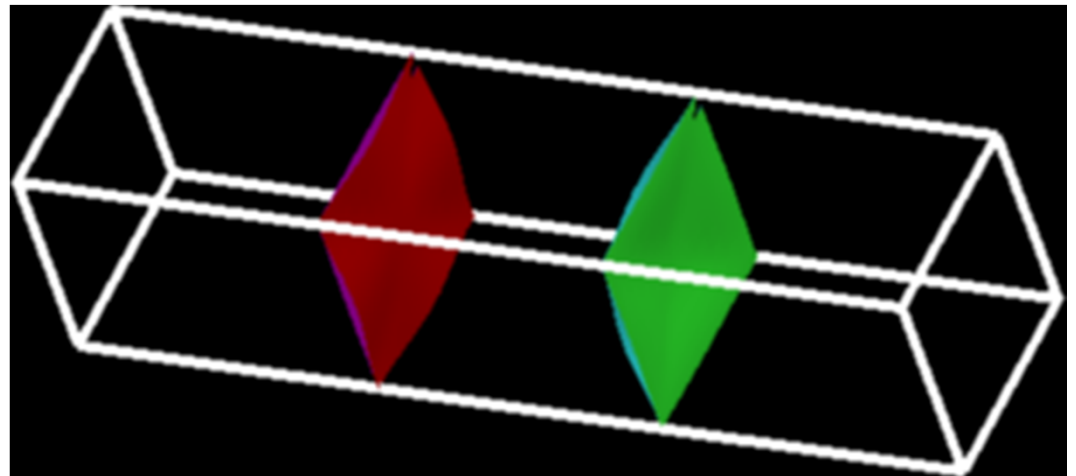
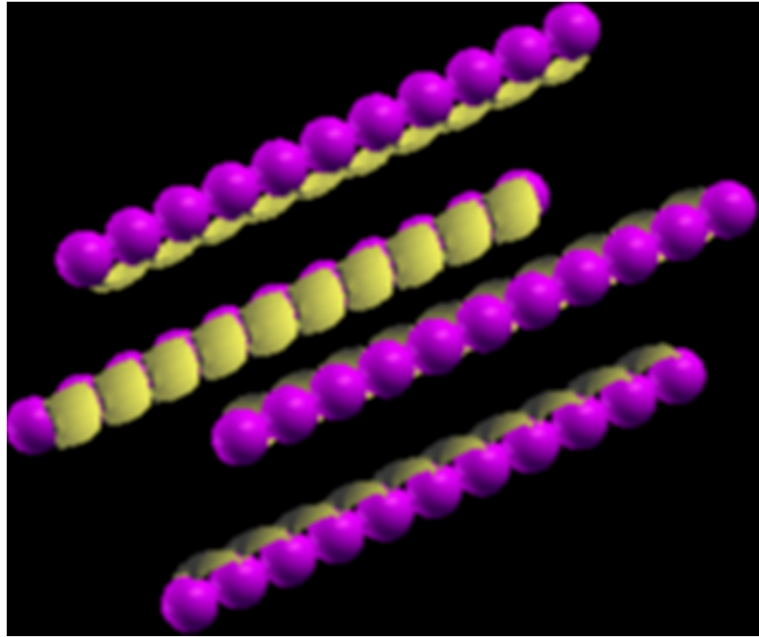
Loen, Norway

<http://www.road2rts.com>

Little, 1963



Diethyl-cyanine iodide



“Not So Famous Danish Kid Brother”



Harald Bohr

Silver Medal, Danish Football Team, 1908 Olympic Games

Fibonacci Chains

"Monte-Carlo Simulation of Fermions on Quasiperiodic Chains,"

P. M. Grant, **BAPS March Meeting** (1992, Indianapolis)

$$G_n \equiv G_{n-1} | G_{n-2}, \quad n = 3, 4, 5, \dots, \infty$$

Where $G_1 = a$, $G_2 = ab$

And $\lim_{n \rightarrow \infty} N_a(G_n) / N_b(G_n) \equiv \tau = (1 + \sqrt{5}) / 2 \approx 1.618\dots$

Example: $G_6 = abaababaab$ ($N = 13$)

Let $a = c\tau b$, subject to $\langle a, b \rangle$ invariant,

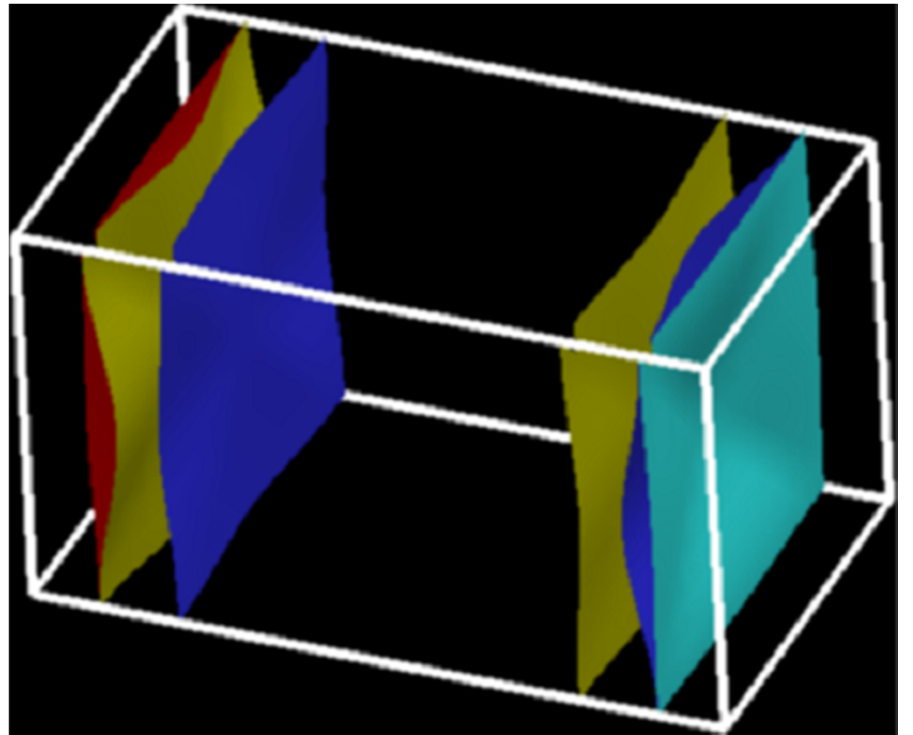
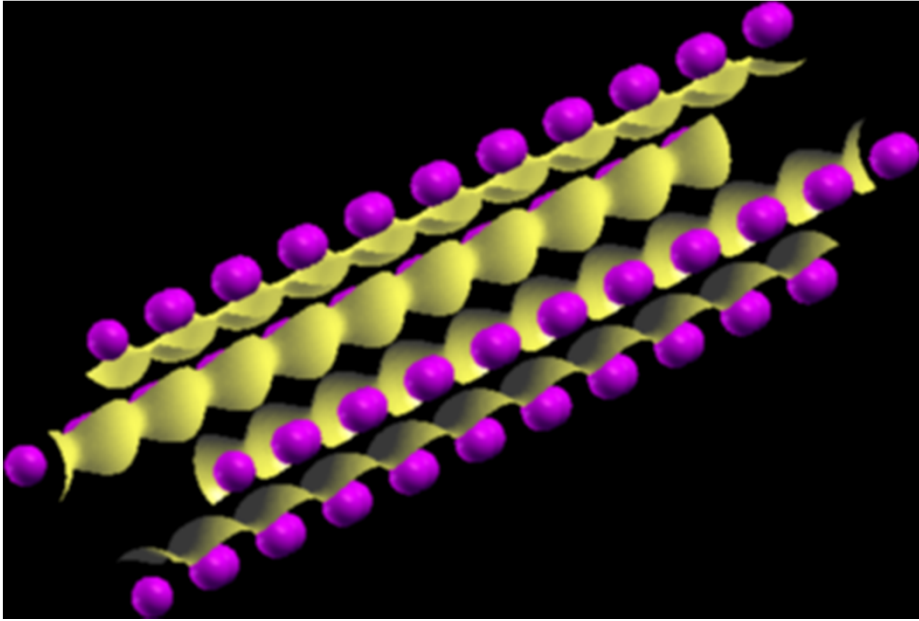
And take a and b

to be "inter-atomic n-n distances,"

Then $b = \tau \langle a, b \rangle / [(1 + c)\tau - 1]$.

Where c is a "scaling" parameter.





$$64 = 65$$

$$64 = 65 ?$$

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Conclusions & Homework

Conclusions

- c-rs-CuO is metallic and thus a proxy for HTSC cuprates.
- e-p $\lambda \sim 0.6 - 0.7$ consistent with $T_C \sim 20 - 50$ K.
- t-rs-CuO becomes a MH-CTI for $c/a > \sim 1.3$.
- $c/a < 1.3$, t-rs-CuO is “self-doped” metal.
- Exhibits “instabilities” in GSE possibly sc related.
- DFT (LDA+U) + proxy structures a useful exploratory tool for nano-material discovery.

Homework

- Compute e-p coupling λ as $f(c/a, U)$ for t-rs-CuO.
- Determine condensate symmetry.
- Compute T_N , μ^* , BCS prefactor, then T_C .
- Compute isotope shift.
- Calculate Lindhardt function.
- Look for anharmonicities a la Newns & Tsuei
- Calculate optical & transport properties as $f(c/a)$.

Supashi-bo !