



**2013 APS Cal/Nev Section Annual Meeting
1-2 November 2013
CSU Sonoma
Rohnert Park, CA**

**A DFT Study of Tetragonal Rocksalt Copper Monoxide:
A Proxy Structure for Understanding HTSC in the
Copper Oxide Perovskites**

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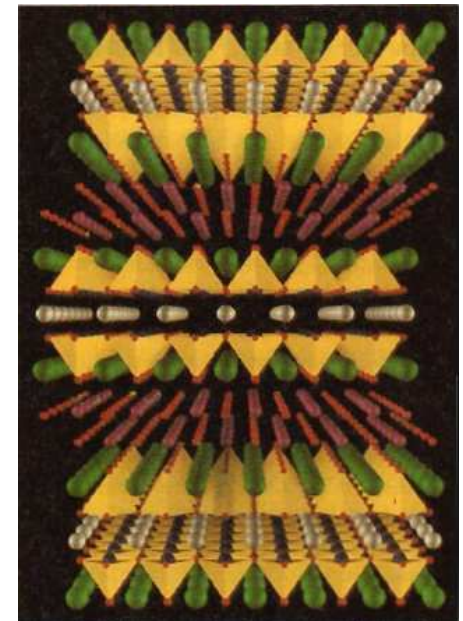
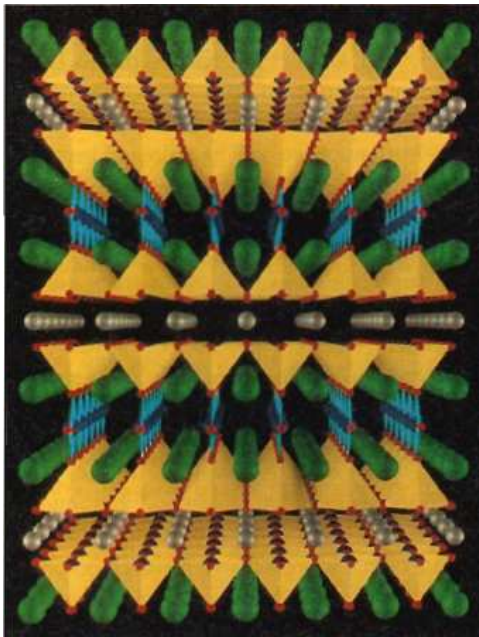
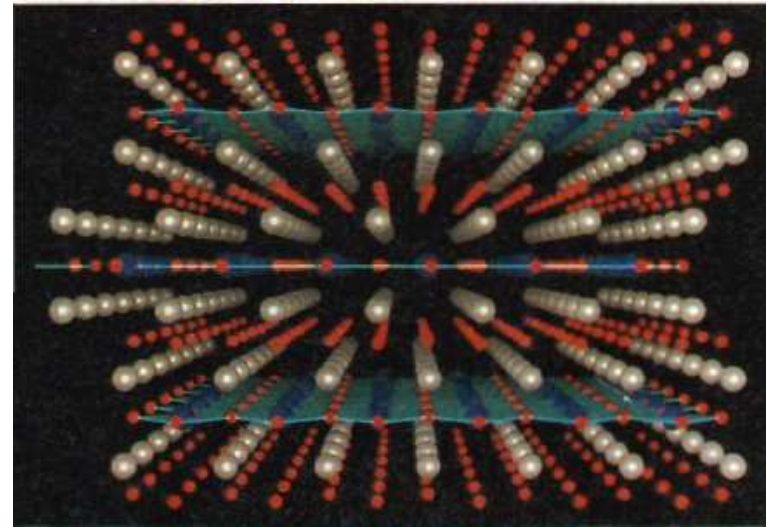
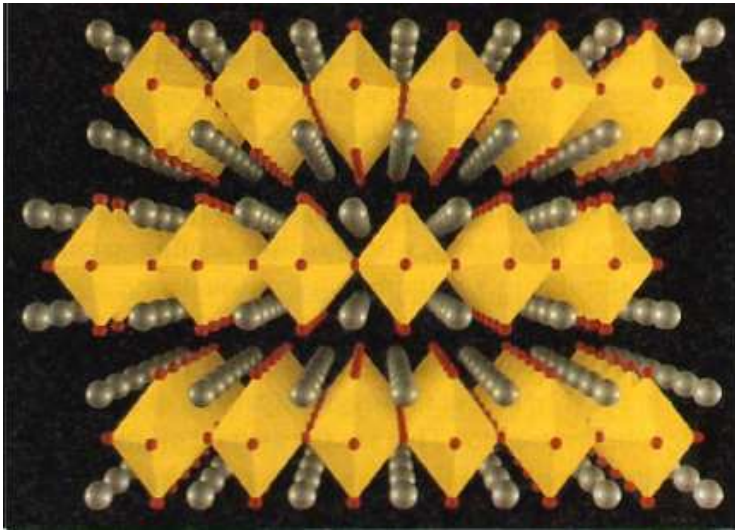
IBM Research Manager, Emeritus

...etc., etc., whatever...

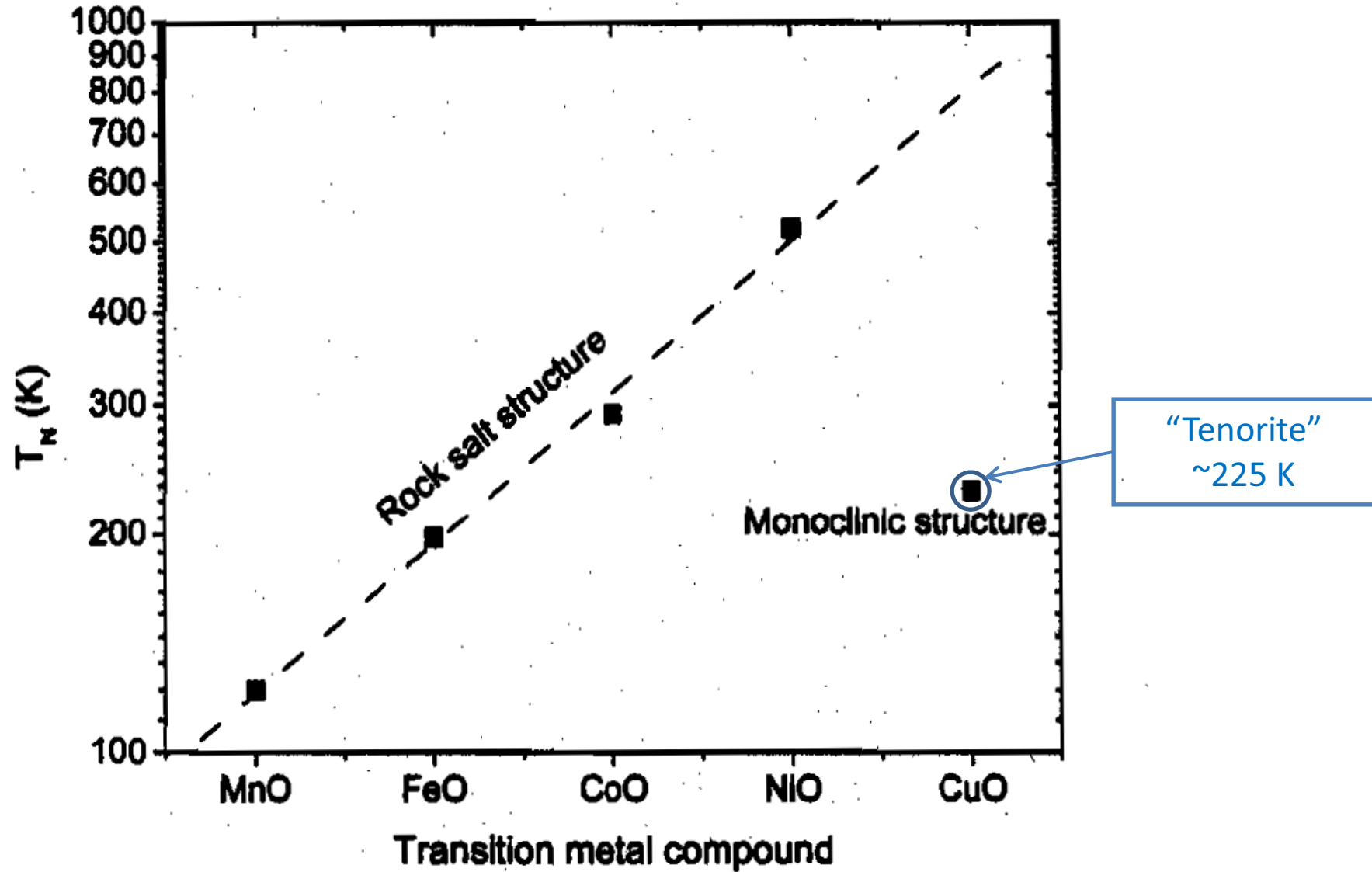
AGING IBM PENSIONER

The Homework Problem

Some Copper Oxide Superconductors

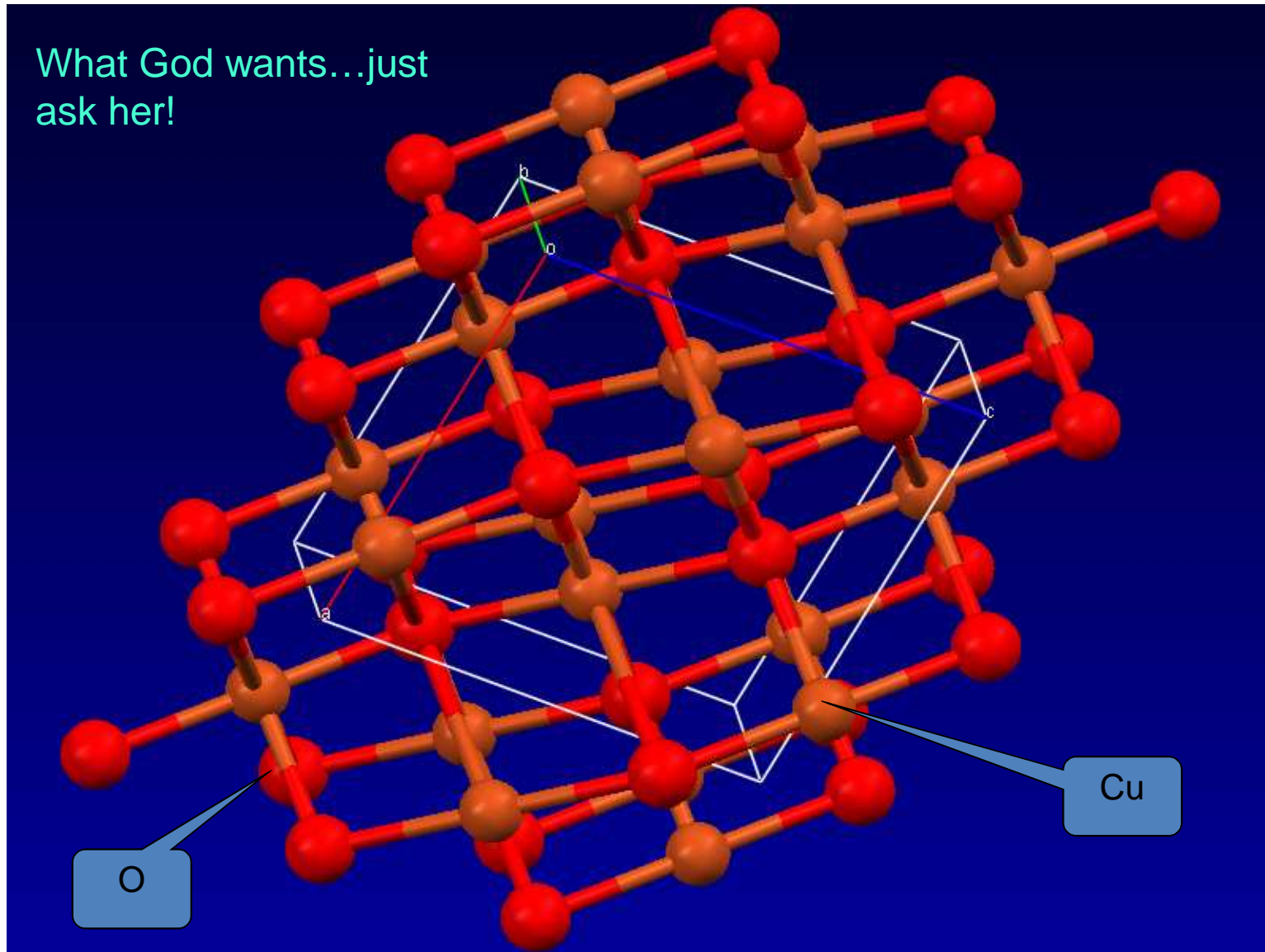


Néel Temperature vs. TMO Atomic Number



Tenorite (Monoclinic CuO)

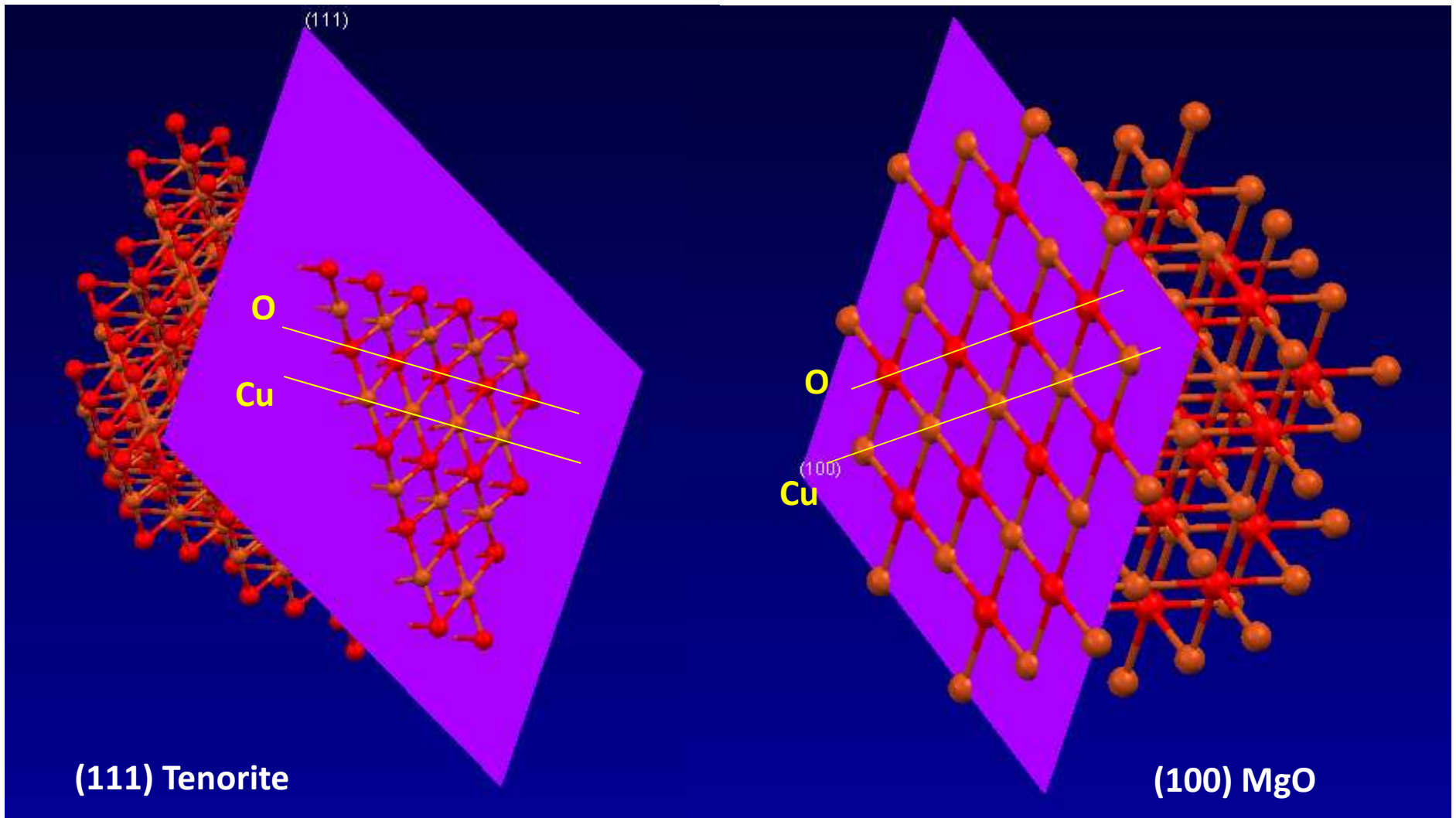
What God wants...just ask her!



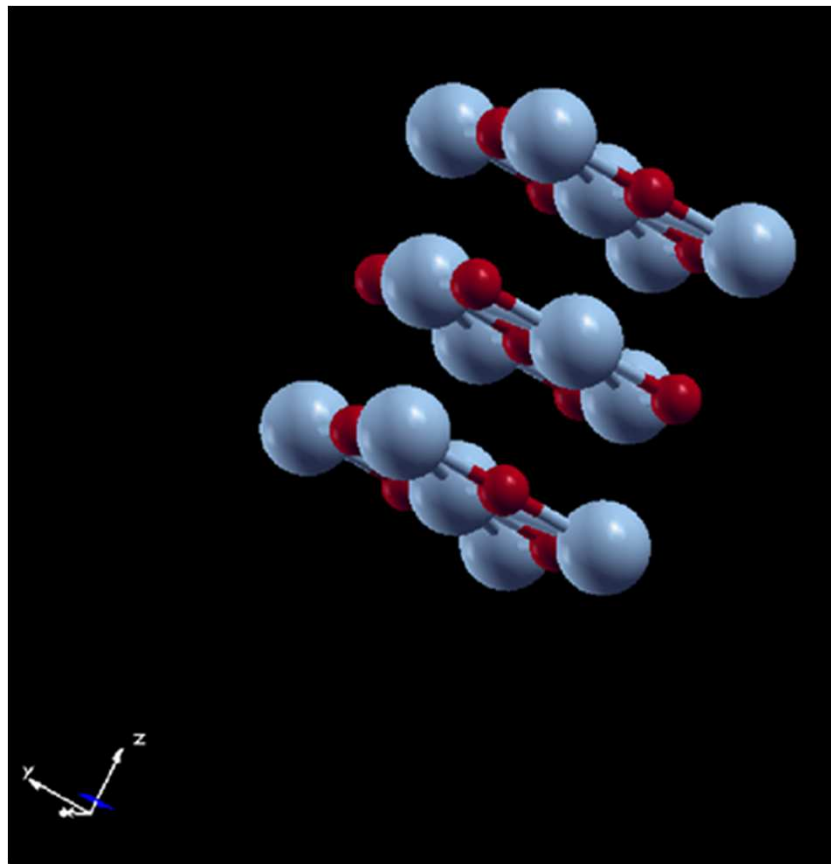
Tools

-Experimental-

Comparison of Tenorite (111) to CuO – MgO Proxy (100)



Attempt Growth by MBE Forced-epi on MgO or STO Substrates



You get 5-6
monolayers of
tetragonal CuO
($c/a = 1.36$)

Siemons, et al.

Tools

-Computational-

Bob Laughlin's "Theory of Everything" (that matters)

Theory of Everything

$$\mathcal{H} = - \sum_j \frac{\hbar^2}{2m_j} \nabla_j^2 - \sum_a \frac{\hbar^2}{2M_a} \nabla_a^2 - \sum_{j,a} \frac{Z_a e^2}{|r_j - R_a|} + \sum_{j,k} \frac{e^2}{|r_j - r_k|} + \sum_{a,b} \frac{Z_a Z_b e^2}{|R_a - R_b|}$$

Where's spin, Pauli and Darwin? Ya screwed up, Bob!
Oh yeah, how about Maxwell, Boltzmann, Gibbs, Fermi,...and finally, Newton's Apple.

- Hydrogen
- Proteins
- Flowers

$$\left[\frac{1}{2m} \left(\sum_{n=1}^3 (\sigma_n (-i\hbar \frac{\partial}{\partial x_n} - q A_n))^2 + q \phi \right) \right] \begin{pmatrix} \psi_0 \\ \psi_1 \end{pmatrix} = i\hbar \begin{pmatrix} \frac{\partial \psi_0}{\partial t} \\ \frac{\partial \psi_1}{\partial t} \end{pmatrix}$$

$$E_0 = \frac{Ze^2 \hbar^2}{8m^2 c^2} \delta^3(\vec{k})$$

$$\frac{4\pi}{c} J^\alpha = \partial_\alpha F^{\alpha\beta} + \Gamma_{\mu\alpha}^\alpha F^{\mu\beta} + \Gamma_{\mu\alpha}^\beta F^{\alpha\mu}$$

$\Gamma_{\mu\alpha}^{\alpha(\beta)}$ ≡ christoffel symbol

$$S = k \log W; \quad G = U - TS + PV$$

$$f(\epsilon) = \frac{1}{e^{(\epsilon - \mu)/kT} + 1}$$

$$F = G \frac{m_1 m_2}{r^2}$$

B-

- Civilizations

The crunch comes when \sum_i with $i \geq 3 \rightarrow$ "thermodynamic limit."

"Van Vleck Catastrophe (1936)"

"Size Matters !"

Extended Hubbard Hamiltonian

Qualitative Description of the Physical Properties of Antiferromagnetic Insulators

$$H = \sum_{\langle ij \rangle, \sigma} t_{ij} c_{i\sigma}^\dagger c_{j\sigma} + U \sum_i n_{i\downarrow} n_{i\uparrow} + \frac{V}{2} \sum_{\langle ij \rangle, \sigma, s} n_{i\sigma} n_{js}$$

One-electron
“band” term

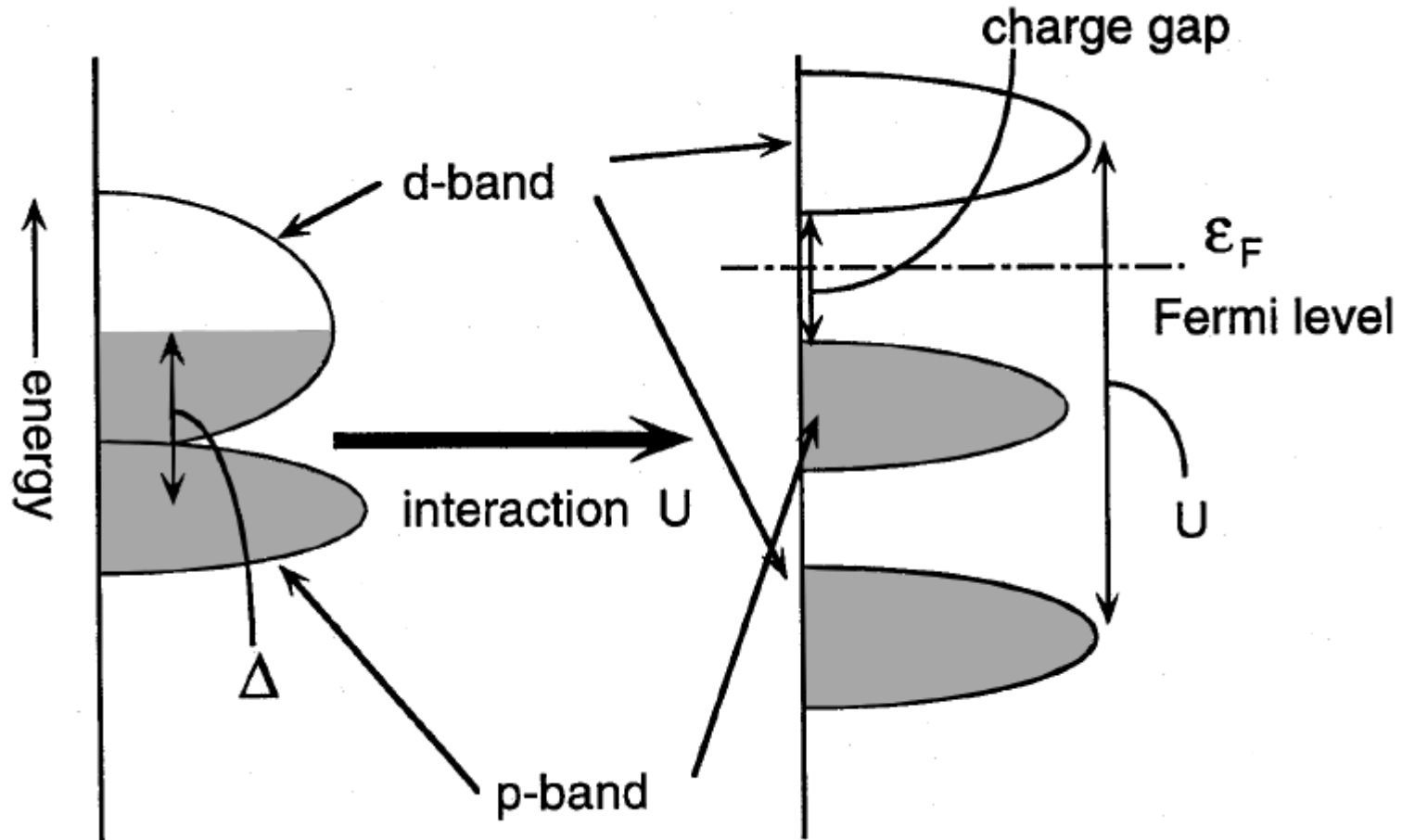
On-site “Hubbard”
double occupation
coulomb repulsion

Off-site repulsion

$$kT_N \approx 4t^2 / S^2 U$$

More Later!

Charge Transfer Insulator



After Imada, et al, RMP 70, 1039 (1998)

Density Functional Theory

Hohenberg – Kohn (NP Chemistry, 1998)

Kohn-Sham Equations (~1965)

$$(T + \hat{V} + V_H(n) + V_{xc}(n))\psi_i = \epsilon_i\psi_i$$

with charge density $n(\mathbf{r}) = \sum_i f_i |\psi_i(\mathbf{r})|^2$, $i =$ combined \mathbf{k} and band index,
 $f_i =$ occupancy of states, and orthonormality constraints $\langle \psi_i | \psi_j \rangle = \delta_{ij}$

Now minimize self-consistently:

$$E[\{\psi_i\}] = \sum_i f_i \langle \psi_i | T + \hat{V} | \psi_i \rangle + E_H + E_{xc}(n) + E_{ion-ion}$$

obtaining:

$$E = \sum_i f_i \langle \psi_i | T + \hat{V} | \psi_i \rangle + E_H + E_{xc}[n] + E_{ion-ion}$$

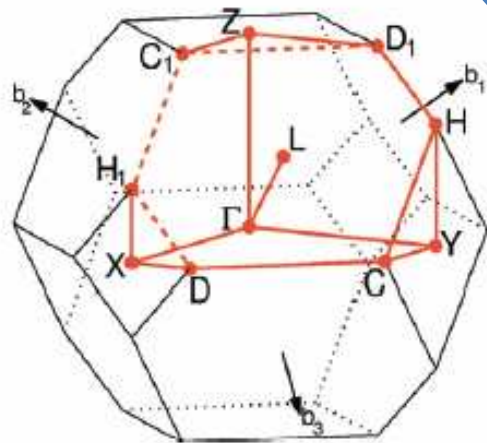
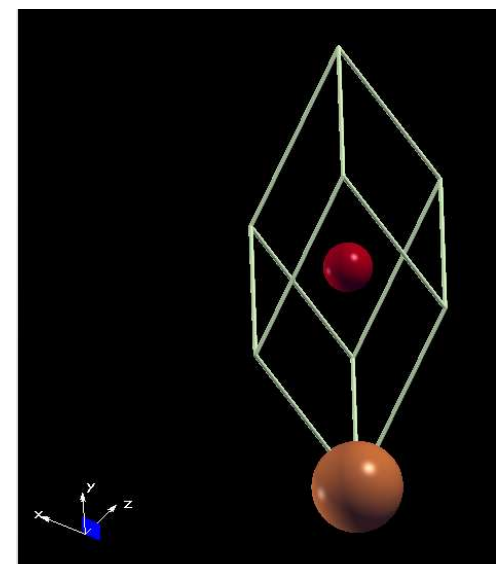
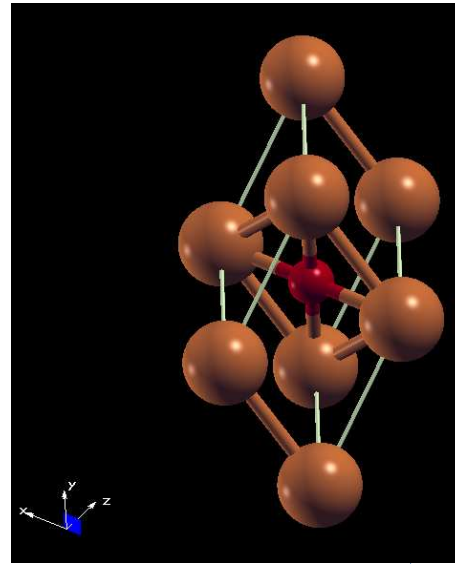
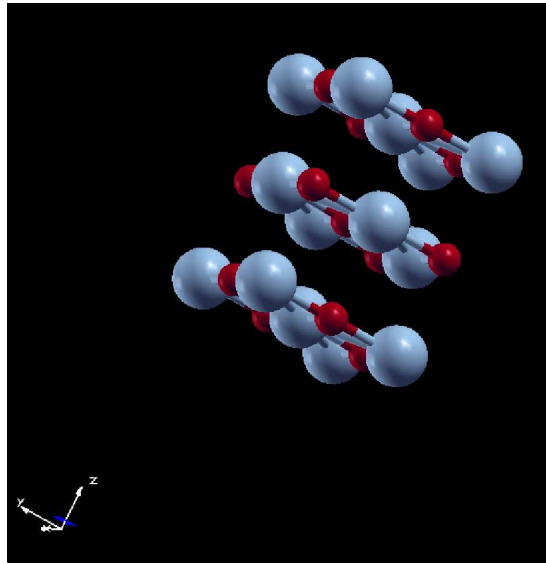
Looking into the future I expect that wavefunction-based and density-based theories will, in complementary ways, continue not only to give us quantitatively more accurate results, but also contribute to a better physical/chemical understanding of the electronic structure of matter. **W. Kohn**

So...

Let's "Shut up and start calculating."

*- David Mermin, Cornell, as quoted by yours truly in,
("The Great Quantum Conundrum," Nature 4 August 2011)*

“Zone-ology” of “nm_Tet-CuO”



Conventional lattice

$$\mathbf{a}_1 = (a, 0, 0)$$

$$\mathbf{a}_2 = (0, b, 0)$$

$$\mathbf{a}_3 = (0, 0, c)$$

Primitive lattice

$$\mathbf{a}_1 = (0, b/2, c/2)$$

$$\mathbf{a}_2 = (a/2, 0, c/2)$$

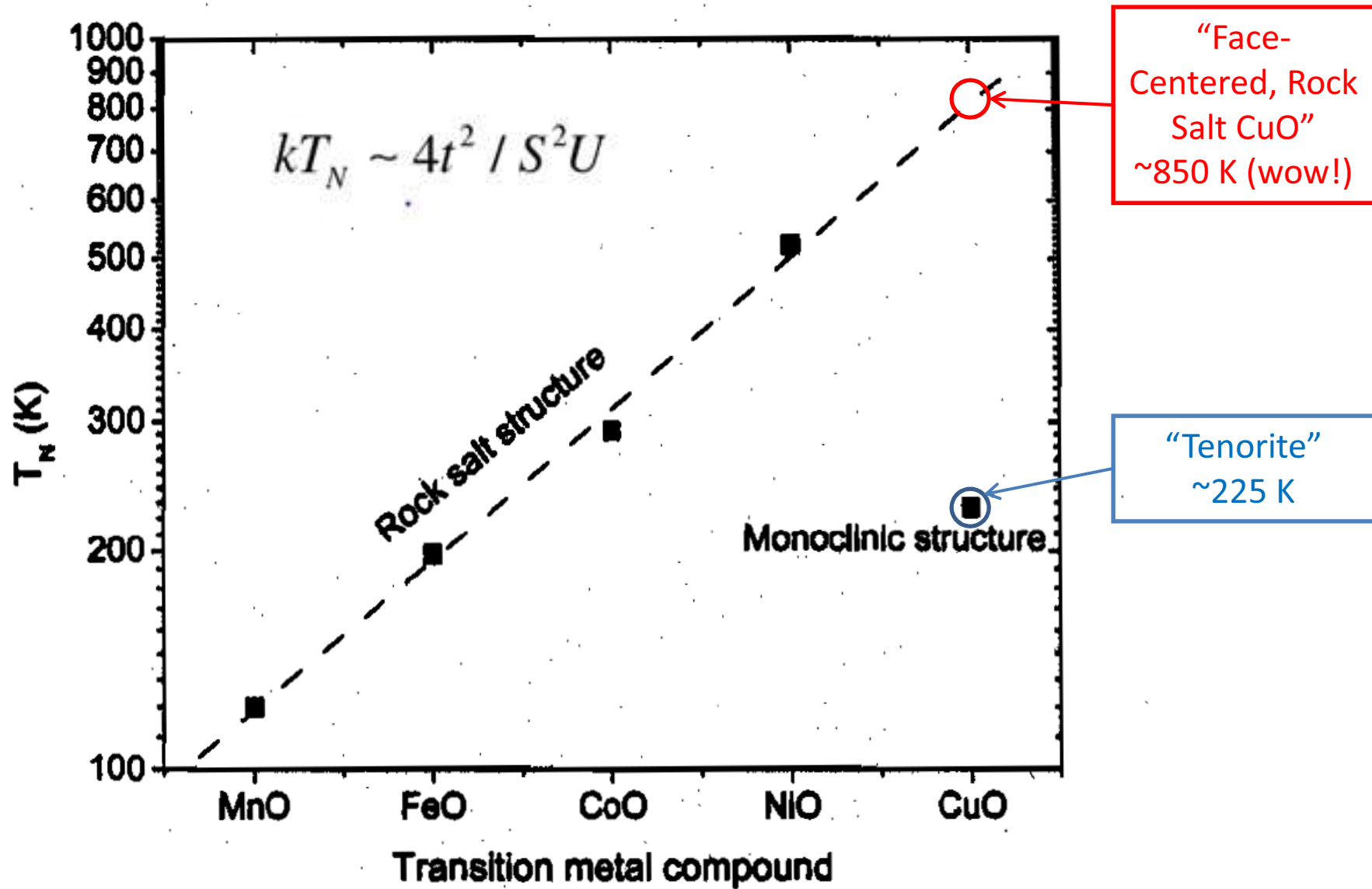
$$\mathbf{a}_3 = (a/2, b/2, 0)$$

Actually, “Tet-CuO” really
“Ortho-fcc CuO” with $a = b$

oh...btw...the red balls are O

Fig. 10. Brillouin zone of ORCF₂ lattice, Path: Γ -Y-C-D-X- Γ -Z-D₁-H-C|C₁-Z|X-H₁|H-Y|L- Γ . An example of band structure using this path is given in Fig. 34.

Néel Temperature vs. TMO Atomic Number



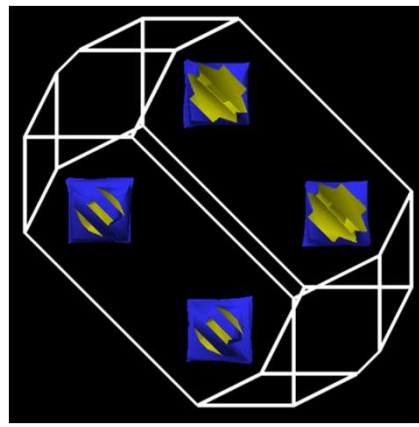
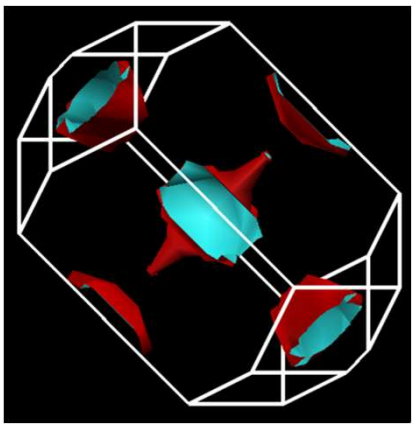
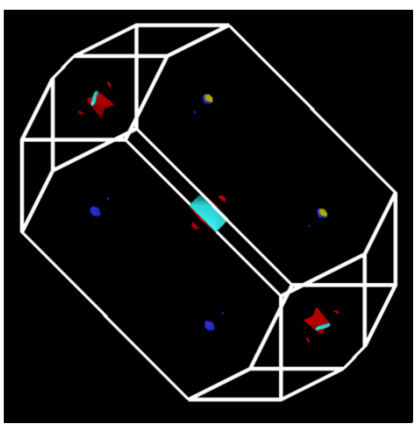
$\frac{n}{U}$

0.00

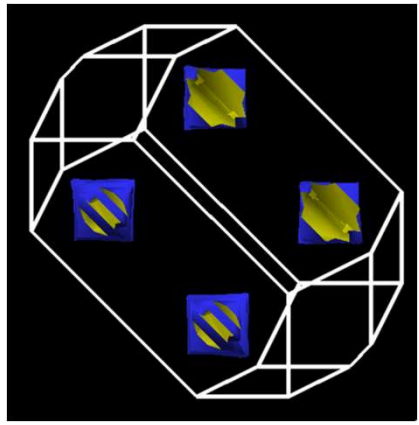
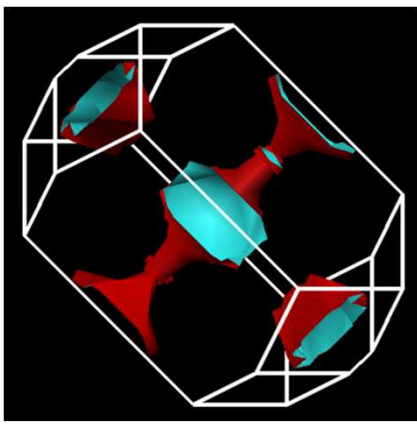
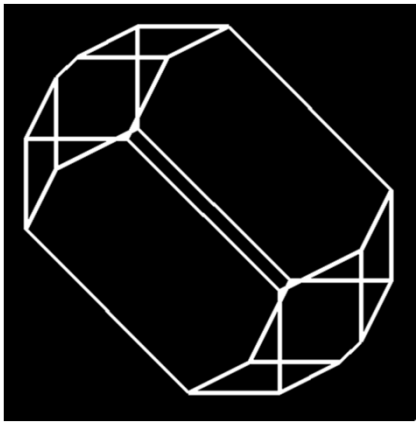
+0.15

-0.15

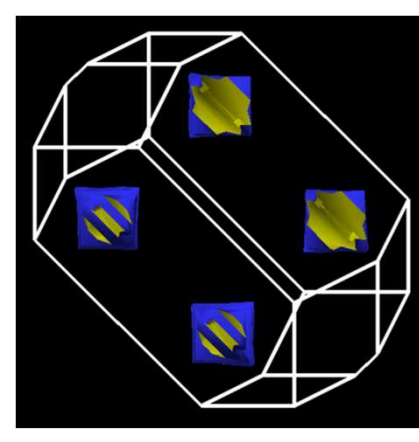
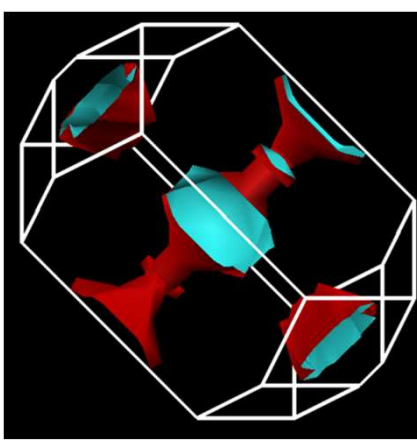
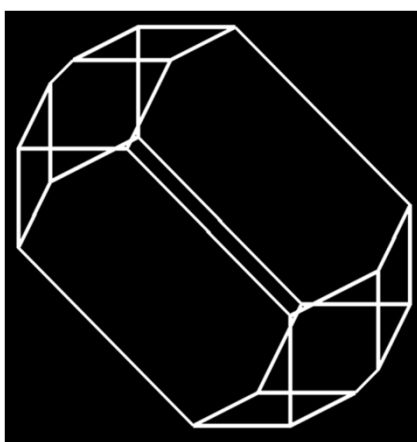
U



0

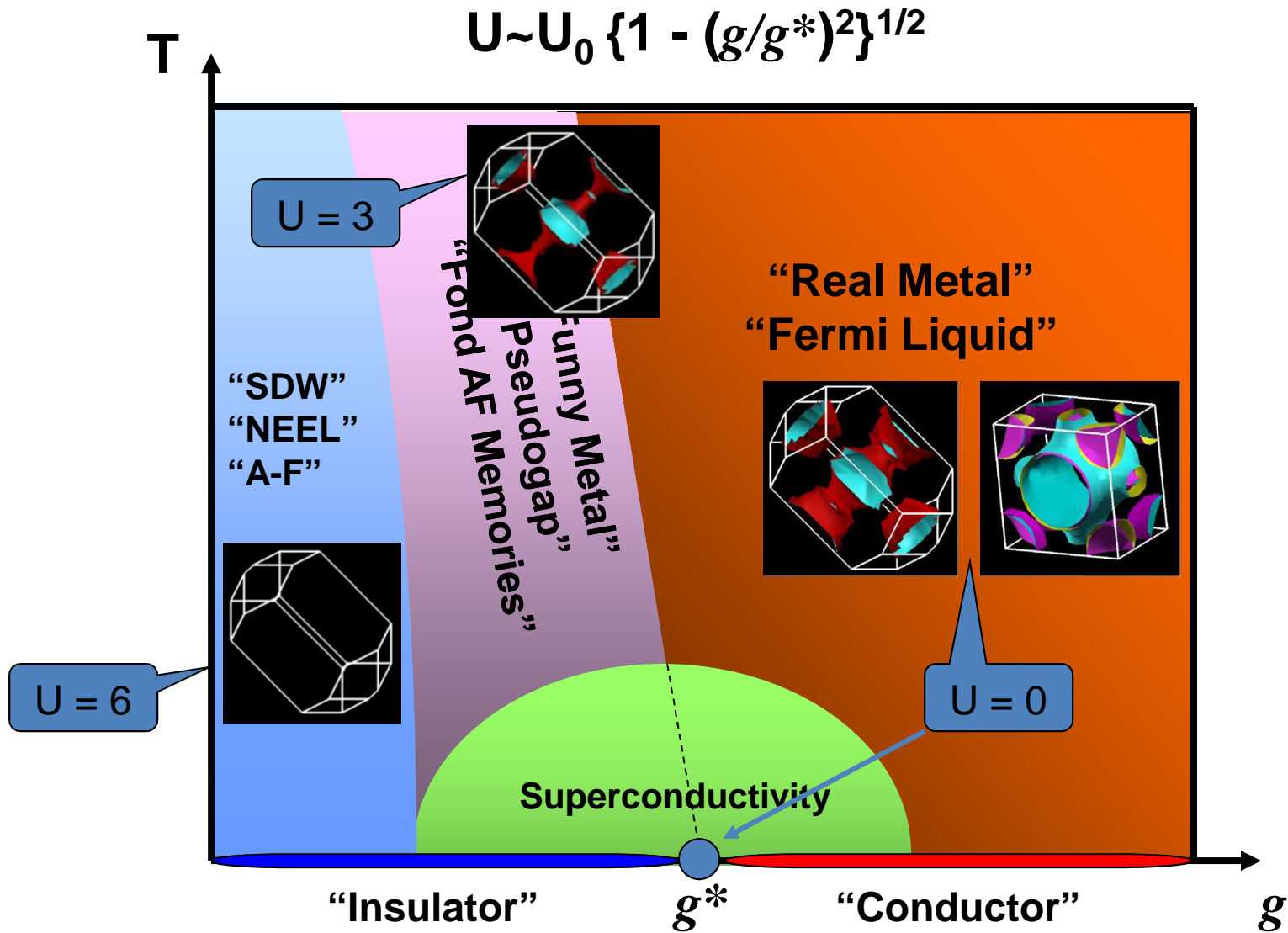


3



6

The Colossal Quantum Conundrum



Somewhere in here there has to be "BCS-like" pairing!

Shakes or Spins or Both?

Are They Copacetic, Competitive...or...

...just another Conundrum?

What formalism is the HTSC analogy to
Migdal-Eliashberg-McMillan?

(In other words, how do I calculate the value of the BCS gap?)

- Original Strong Coupling, Eliashberg (*JETP*, 1960), McMillan (*PR*, 1968)
- Generalized Linhard Response Function (RPA + fluctuations) *Hu and O'Connell (PRB 1989)*
- Dielectric Response Function *Kirznits, Maximov, Khomskii (JLTP 1972)*

McMillan Strong Coupling

(Computationally implemented by Wierzbowska, et al., cond-mat/0504077, 2006)

$$T_c = \frac{\Theta}{1.45} \exp \left[- \frac{1.04(1+\lambda)}{\lambda - \mu^*(1+0.62\lambda)} \right]. \quad (18)$$

What's the HTSC equivalent?

$$\lambda = 2 \int \frac{d\omega}{\omega} \alpha^2(\omega) F(\omega) = \frac{N(0) \langle g^2 \rangle}{M \langle \omega^2 \rangle}, \quad (23)$$

$$\alpha^2(\omega) F(\omega) = \int_S \frac{d^2p}{v_F} \int_{S'} \frac{d^2p'}{(2\pi\hbar)^3 v_{F'}} \sum_{\nu} g_{pp'\nu}^2 \delta(\omega - \omega_{p-p'\nu}) \Big/ \int_S \frac{d^2p}{v_F}, \quad (19)$$

where the integral $\int d^2p$ is taken over the Fermi surface and the electron-phonon matrix elements are given by¹⁴

$$g_{pp'\nu} = (\hbar/2MNV\omega_{p-p'\nu})^{1/2} g_{\nu}(p, p'), \quad (20)$$

where $g_{\nu}(pp')$ is the electronic matrix element of the change in the crystal potential \mathcal{U} as one atom is moved:

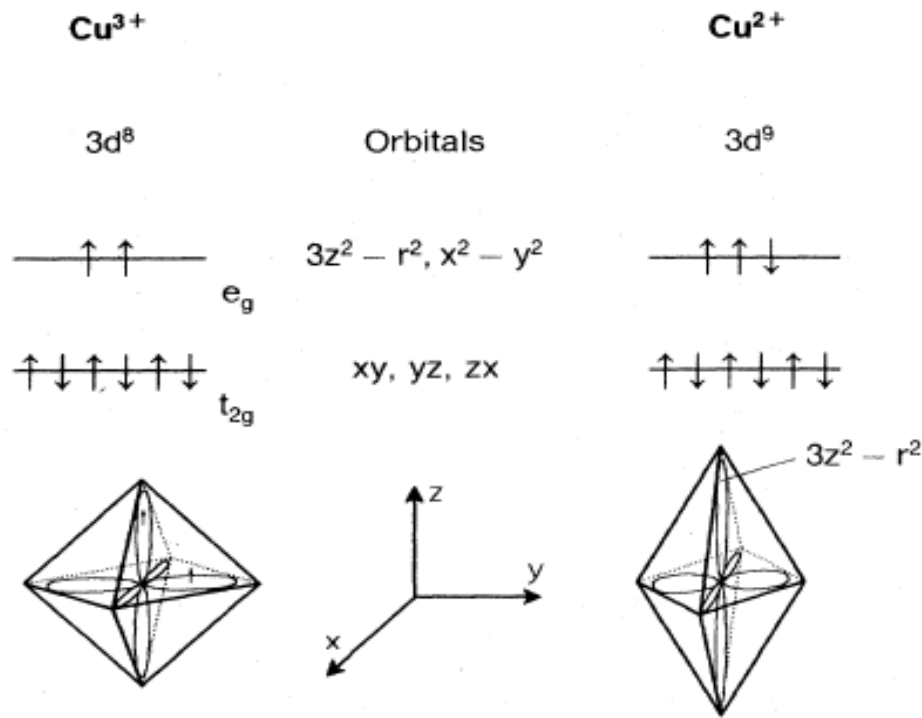
$$g_{\nu}(pp') = \int \psi_p^*(\mathbf{r}_{p-p'}) \nabla \mathcal{U} \psi_{p'} d\mathbf{r}. \quad (21)$$

Well!
What do I "move?"

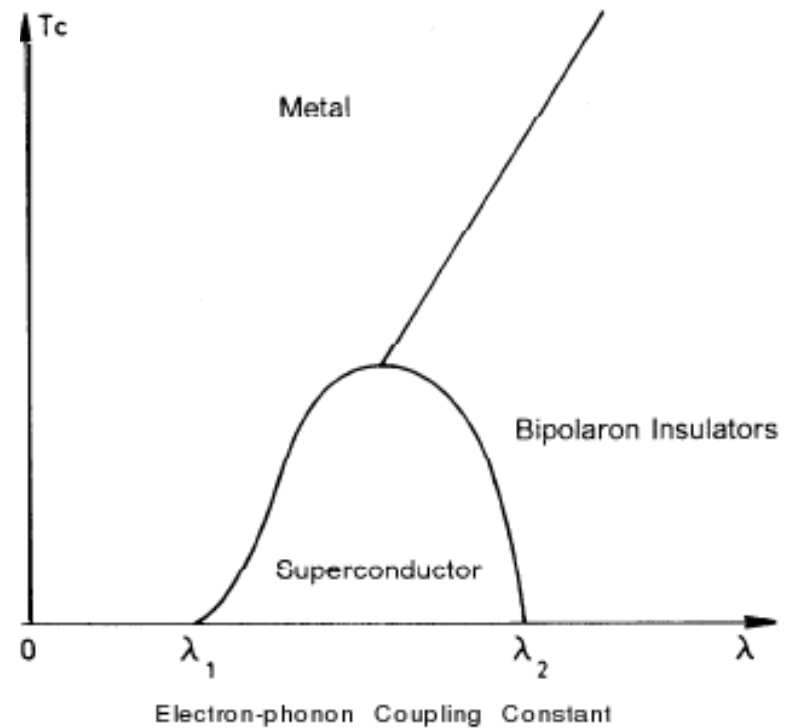
Phonons?

Bednorz-Mueller Nobel Lecture

Copper Ions in the Oxide Octahedron



*Jahn-Teller Effect:
Elongation of
the Octahedron*

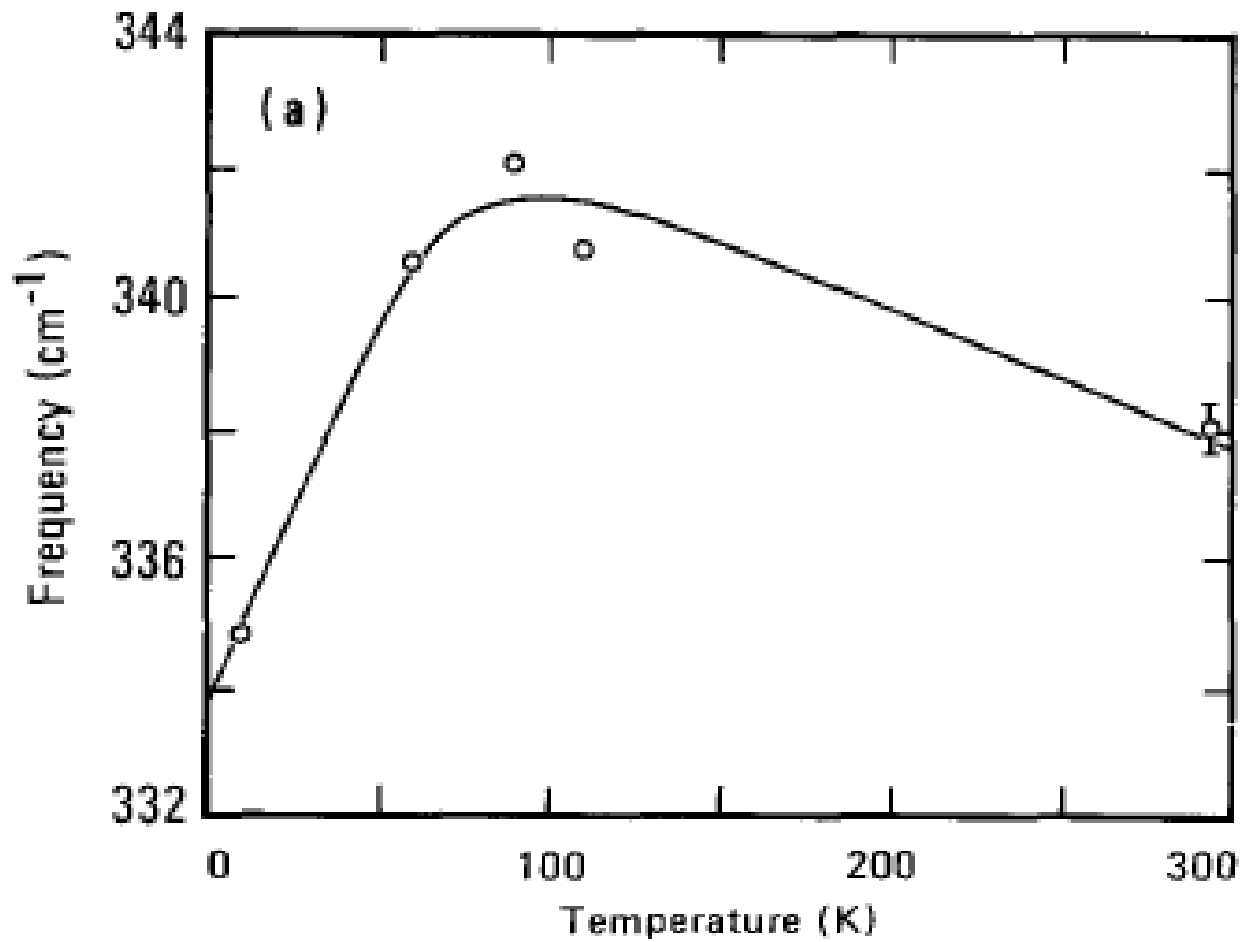


After Chakravarty, (1979)

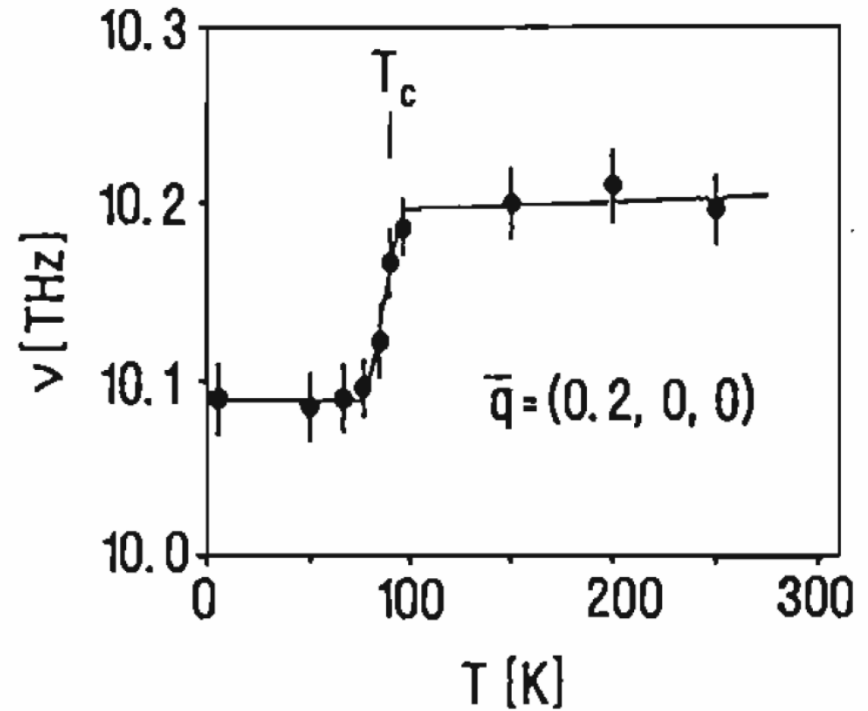
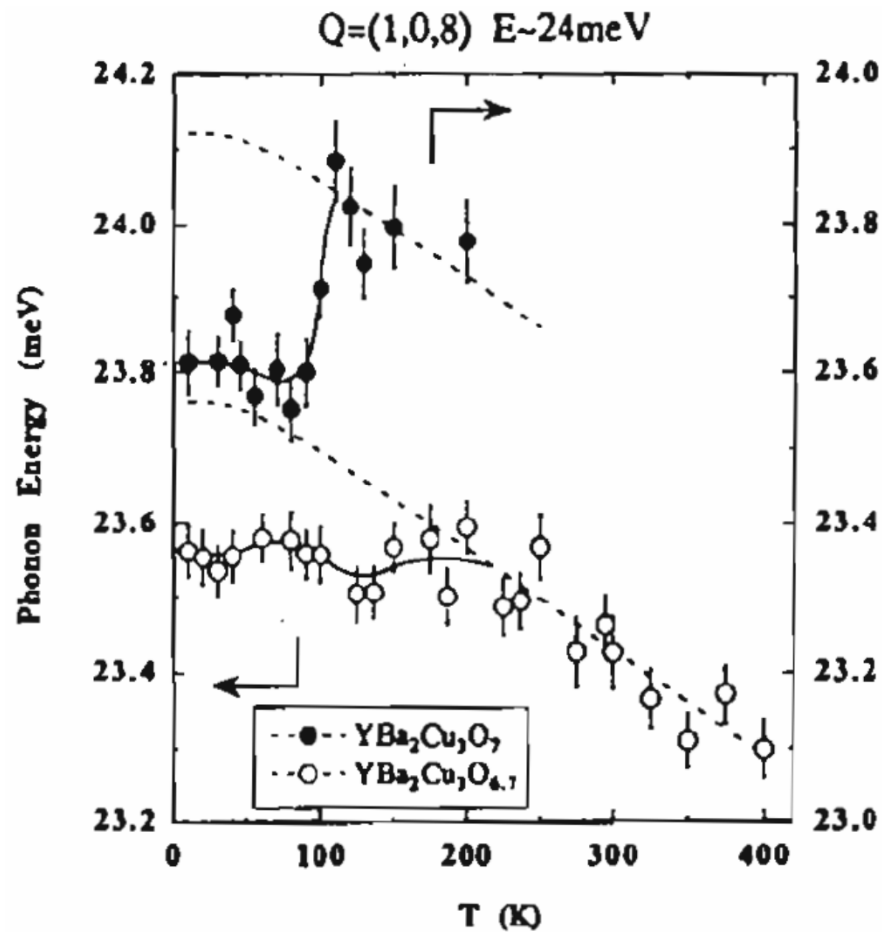
Indeed, they're there!

Macfarlane, Rosen, Seki, SSC 63, 831 (1987)

Raman Spectroscopy of YBCO

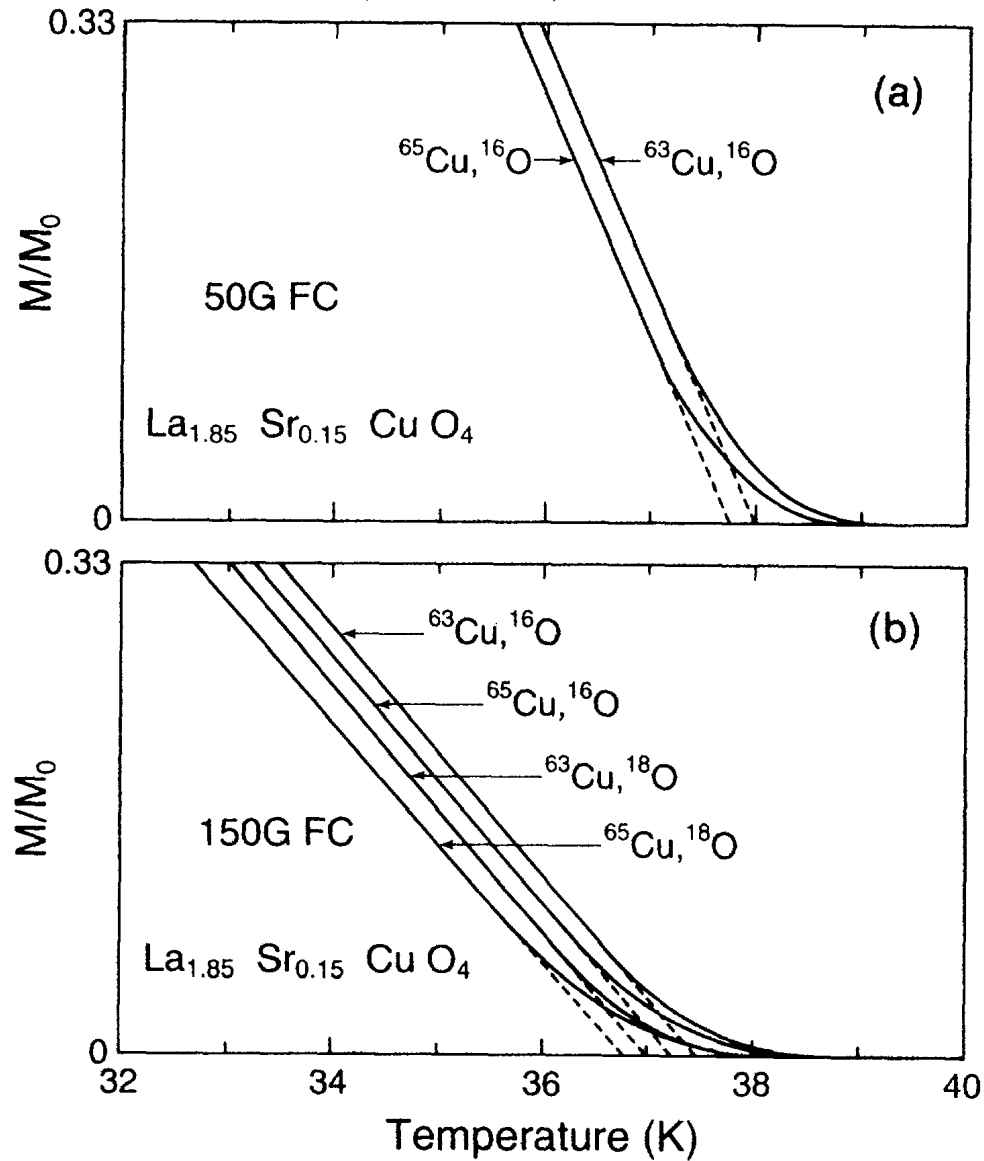


More Evidence

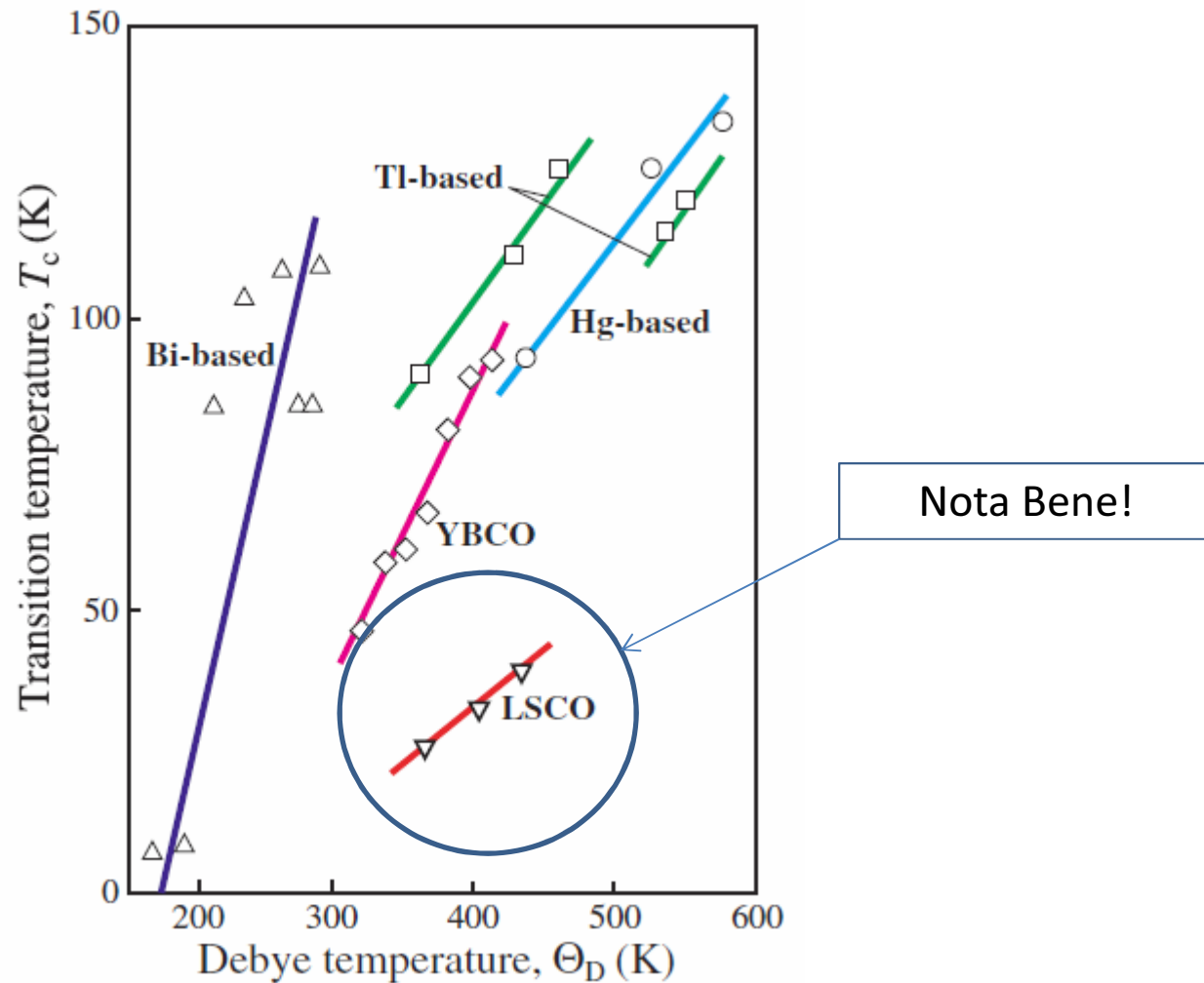


Pyka, et al., PRL 70, 1457, (1993)

Harashima, et al., Physica C263, 257 (1996)

Copper and Oxygen Isotope Effects in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ J. P. Franck,¹ S. Harker,¹ and J. H. Brewer²

Finally, T_c scales (roughly) with Θ_D

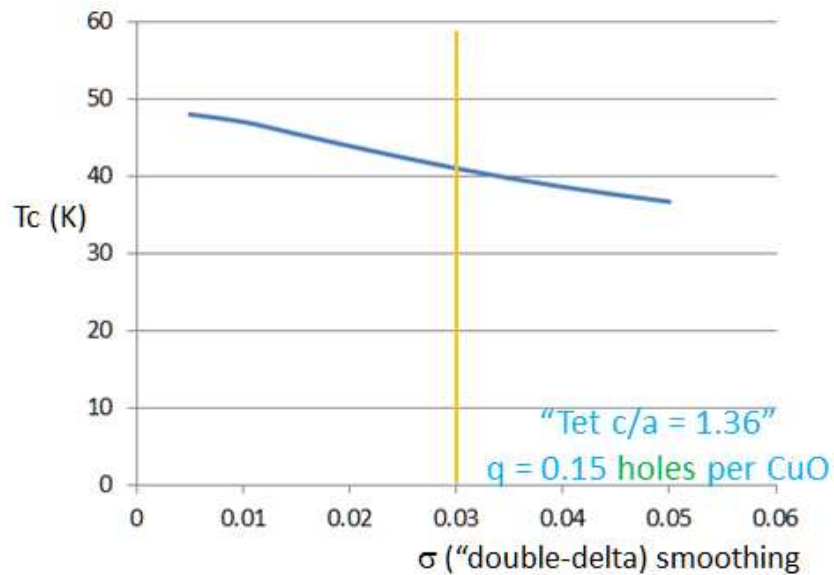


Ledbetter, Physica C 235, 1325 (1994)

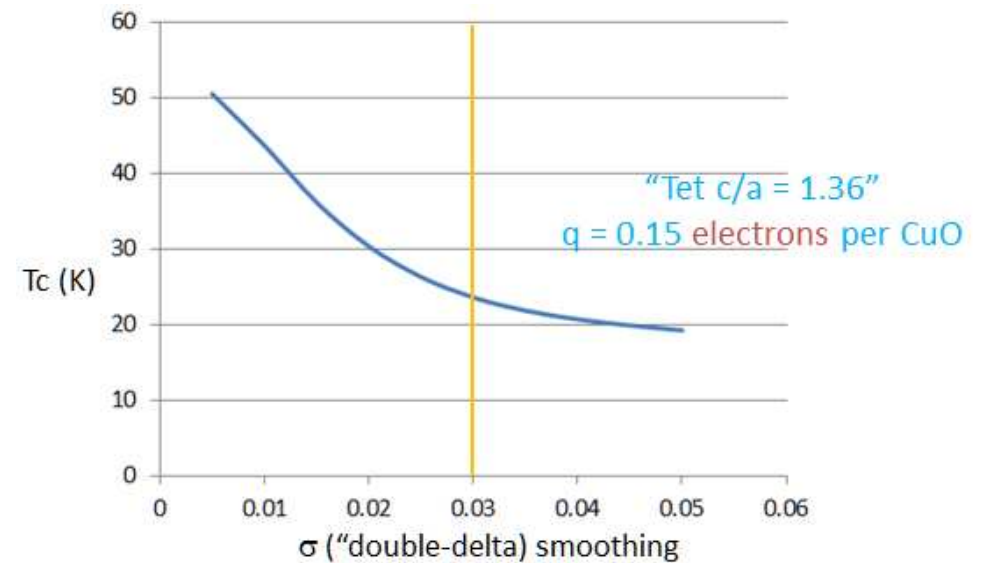
Eliashberg-McMillan-Allen-Dynes

$$\Theta_D \approx 440 \text{ K}, \mu^* \approx 0.05$$

Holes

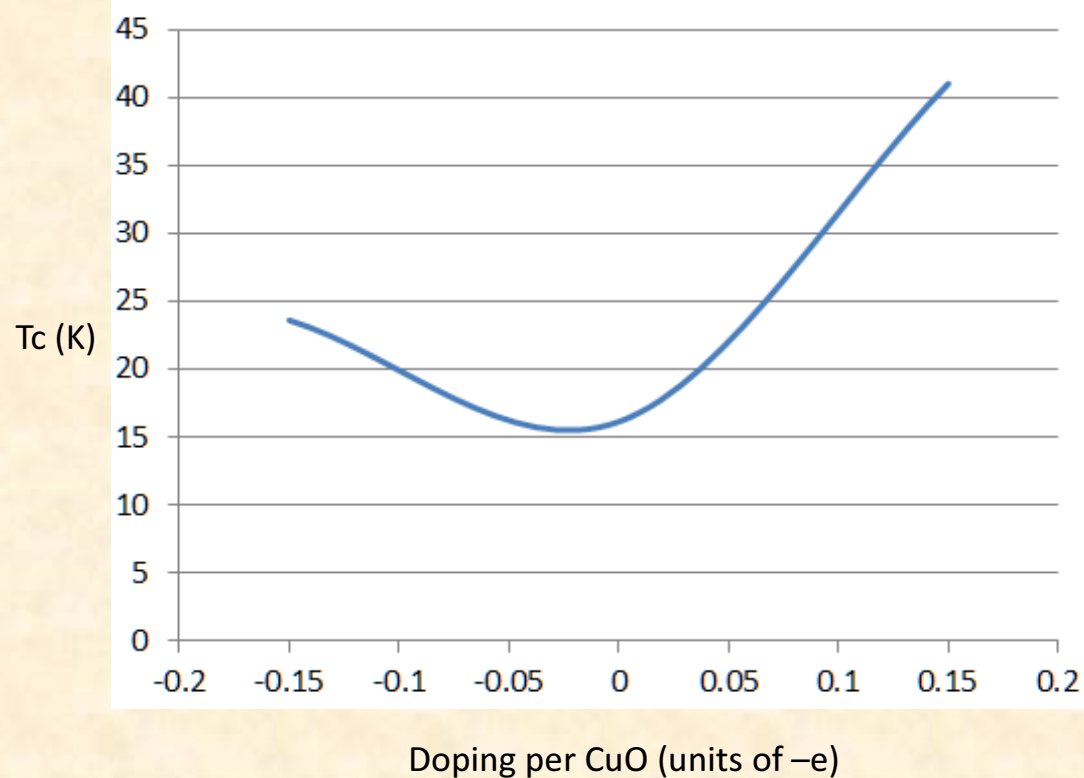


Electrons



Note Differences
in T_c Scale

Conclusions



- Phonons can yield “credible” values of T_c in the cuprates
- Holes are better than electrons
- Can’t account for higher T_c ’s in “1-2-3 +” layered compounds (Yet...but stay tuned!)

Computers and the Study of Proxy Structures may finally resolve the mystery of High- T_c ...a Future NP for someone in the audience...much younger than me!

The End