## St. Patrick's Day - 2016



-2014-

**MPC** Accepted as a Dual National by the Republic of Ireland







### Paul Michael Patrick Grant Grandson of Two Proud Lands

# "Woodstock" (#30 Upcoming)



"Band of Brothers (and a Sister!)" - IBM Almaden, March 1987 -



#### "Infamous Irish-Jewish Catskill Borscht-Belt Comedy Team"



#### A DFT Study of Electron-Phonon Mediated Superconductivity in Doped Mott-Hubbard Proxy Cubic-Tetragonal Copper Monoxide

Paul M. Grant W2AGZ Technologies



## – Our Computational Tool Box –

- DFT
  - Quantum Espresso
    - Fermiologies, States (DOS), Phonons, e-p "Lambda"
  - Gibbs2
    - Debye Statistics
  - ELK
    - LDA + U
- Graphics
  - Xcrysden, XMGRACE
    - Fermi Surfaces, Projected DOS
- Modeling
  - Then e-p Superconductivity via Eliashberg/McMillan!

#### The Various Flavors of Copper "Monoxide"



**NB: All show attributes of Mott-Hubbard behavior** 

"Configuration/Coordination Space"

## Interesting...

- Lowest symmetry yields lowest ground state energy.
- Higher...at least in a computer...gives greater (localized around given "optimal lattice" constants).
- Why? Jahn-Teller "degeneracies"! Nature abhors them (Aristole).
- Were Bednorz-Mueller (Chakravarty & Hoecht) on the right path in 1986 after all?



### **Phonons are there!**



### Let's look at the "U = 0, Fermi Liquid" limit for doped proxy tet-CuO!





#### Electronic properties of rocksalt copper monoxide: A proxy structure for high temperature superconductivity

The International Conference on Theoretical Physics 'Dubna-Nano2008' IOP Journal of Physics: Conference Series 129 (2008) 012042 doi:10.1088/1742-6596/129/1/012042

### Superconductivity and Phonons BCS via Eliashberg-McMillan

$$H_{el-ph} = \sum_{\mathbf{k},\mathbf{q},\nu} g_{\mathbf{k}+\mathbf{q},\mathbf{k}}^{\mathbf{q}_{\nu,mn}} c_{\mathbf{k}+\mathbf{q}}^{\dagger m} c_{\mathbf{k}}^{n} (b_{-\mathbf{q},\nu}^{\dagger} + b_{\mathbf{q},\nu})$$

$$\lambda_{\mathbf{q},\nu} = \frac{2}{N(\varepsilon_F)\omega_{\mathbf{q},\nu}} \sum_{mn} \sum_{\mathbf{k}} \left| g_{\mathbf{k}+\mathbf{q},\mathbf{k}}^{\mathbf{q}_{\nu,mn}} \right|^2 \delta(\varepsilon_{\mathbf{k}+\mathbf{q},m} - \varepsilon_F) \delta(\varepsilon_{\mathbf{k},n} - \varepsilon_F)$$

$$\alpha^{2}F(\omega) = \frac{1}{N(\varepsilon_{E})} \sum_{mn} \sum_{\mathbf{q}, \mathbf{v}} \delta(\omega - \omega)$$

$$\lambda = 2 \int_0^\infty \frac{\alpha^2 F}{\alpha}$$

NB! The "double deltas" will be approximated by two Gaussians of width "sigma (σ)" whose numerical convergence is governed by imposed precision limits and basis set symmetry. Con Quidado!

To get  $\lambda$ , need to compute  $g_{k+q,k}$ 

## e-p Interaction in the DFT/LDA Formalism

$$g_{\mathbf{k}+\mathbf{q},\mathbf{k}}^{\mathbf{q}_{\nu,mn}} = \sqrt{\hbar/2\omega_{\mathbf{q},\nu}} \left\langle \psi_{\mathbf{k}+\mathbf{q},m} \left| \Delta V_{KS}^{\mathbf{q},\nu} \right| \psi_{\mathbf{k},n} \right\rangle$$

$$\Delta V_{KS}^{\mathbf{q},\nu} = \sum_{\mathbf{R}} \sum_{s} \frac{\partial V_{KS}}{\partial \vec{u}_{s,\mathbf{R}}} \cdot \vec{u}_{s}^{\mathbf{q},\nu} \frac{e^{i\mathbf{q}\cdot\mathbf{R}}}{\sqrt{N}}$$

$$T_{C} = \frac{\Theta_{D}}{1.45} \exp\left(-\frac{1.04(1+\lambda)}{\lambda - \mu^{*}(1+0.62\lambda)}\right)$$



## CuO

(tetragonal) q = 0.15/CuO $T_c$ 

Ipso Facto... At least at optimum doping...

the holes are paired by lattice shakes...

with maybe a little help from their spins?



Min GSE at a0 = 3.9 Å, c/a = 1.15





T<sub>c</sub>(avg) ~ <u>75</u> K

### Voice from the Past!

AUGUST 1, 1941

PHYSICAL REVIEW

VOLUME 60

#### Paramagnetic Dispersion Measurements at 77.3°K\*

C. STARR Massachusetts Institute of Technology, Cambridge, Massachusetts (Received June 7, 1941)

The dispersion of the magnetic susceptibility of some paramagnetic compounds of Fe, Mn, and Cr, was studied at 77.3°K over a frequency range of 2 to 10 megacycles/sec. with magnetic fields up to 60,000 gauss. The results substantiate the theory of Casimir and du Pre, which is based upon the thermal coupling between the magnetic spin system and the lattice vibrations.



## So is it Shakes and/or Spins?



### Maybe it takes two to Tango!



## Five HTSC "In Your Face" Questions

